



# **Fundamentals of Computer Graphics and Image Processing Shading and Lighting (04)**

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# Overview

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- ▶ **Direct Illumination**
  - ▶ **Emission at light sources**
  - ▶ Scattering at surfaces
  - ▶ Gouraud shading
- ▶ Global Illumination
  - ▶ Shadows
  - ▶ Refractions
  - ▶ Inter-object reflections



# How the lectures should look like #1

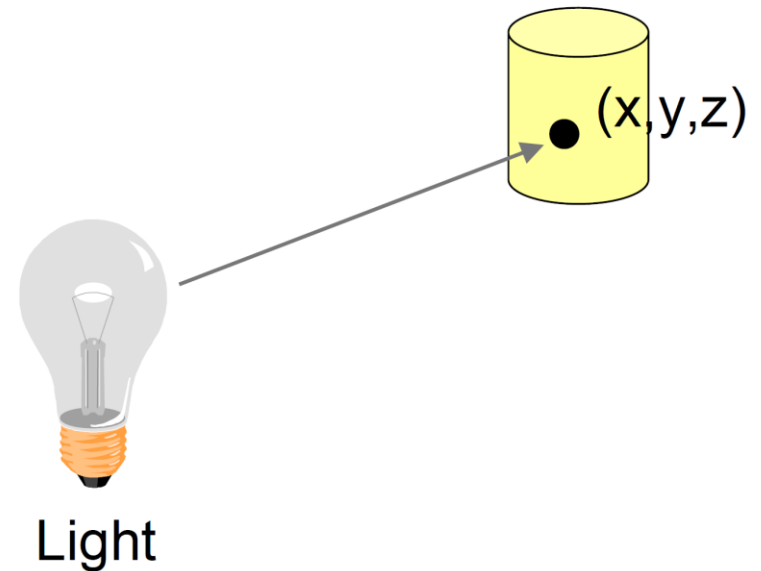
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- Ask questions, please!!!
- Be communicative
- More active you are, the better for you!



# Overview

- ▶  $I_L(x, y, z, \theta, \varphi, \lambda)$ 
  - ▶ describes intensity of energy,
  - ▶ leaving a light source, ...
  - ▶ arriving at location  $(x, y, z)$ , ...
  - ▶ from direction  $(\theta, \phi)$ , ...
  - ▶ with wavelength  $\lambda$



# Light Source types

- ▶ Omnidirectional
- ▶ Spotlight
- ▶ Area
- ▶ Directional
- ▶ Object



- what are the differences?



# Light Source Models

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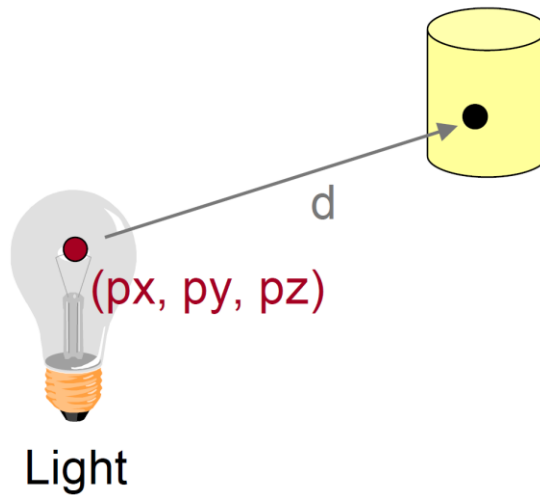
- ▶ Simple mathematical models
- ▶ OpenGL support
  - ▶ Point light
  - ▶ Directional light
  - ▶ Spot light



# Point Light Source

## ► Models omni-directional source

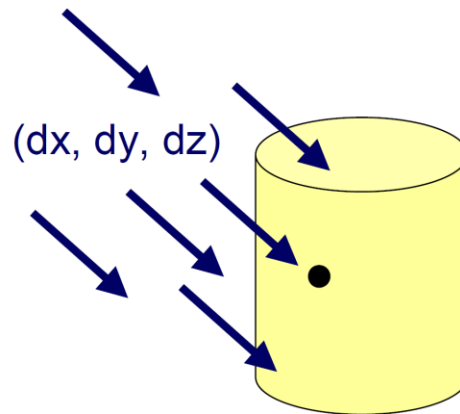
- intensity ( $I_0$ ),
- position ( $x, y, z$ ),
- factors ( $k_c, k_l, k_q$ ) for attenuation with distance ( $d$ )



$$I_L = \frac{I_0}{k_c + k_l d + k_q d^2}$$

# Directional Light Source

- ▶ Models point light source at infinity
  - ▶ intensity ( $I_0$ ),
  - ▶ direction ( $dx, dy, dz$ ),
  - ▶ no attenuation with distance



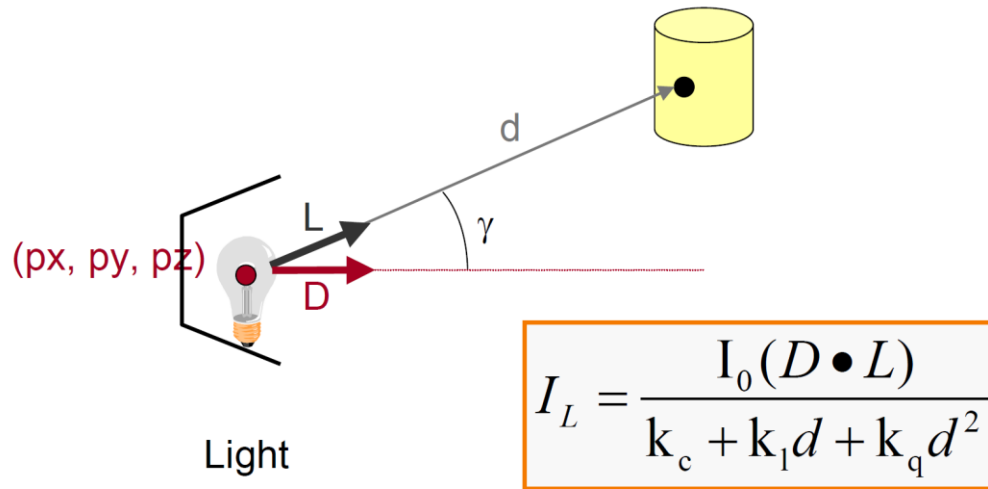
$$I_L = I_0$$





# Spot Light Source

- Models point light source with direction
  - intensity ( $I_0$ ),
  - position ( $x, y, z$ ),
  - direction ( $d$ ),
  - attenuation ( $k_c, k_l, k_q$ ).



# Overview

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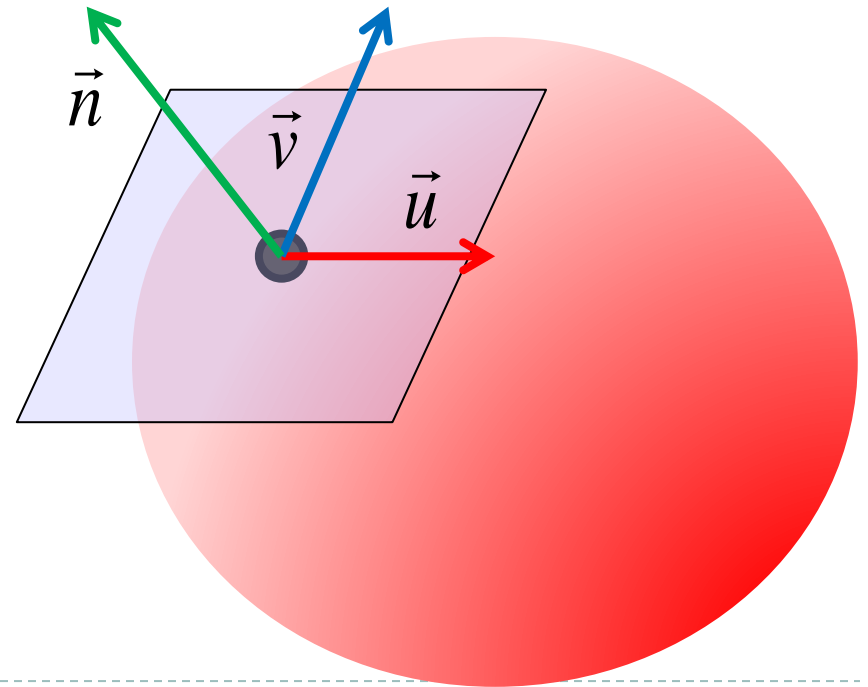
- ▶ Direct Illumination
  - ▶ Emission at light sources
  - ▶ **Scattering at surfaces**
  - ▶ Gouraud shading
- ▶ Global Illumination
  - ▶ Shadows
  - ▶ Refractions
  - ▶ Inter-object reflections

# Surface normal vector

- ▶ Perpendicular to the surface at the point
- ▶ Computation:
  - ▶ Usually from tangent vectors
  - ▶ Vector cross product  $\vec{n} = \vec{u} \times \vec{v}$
  - ▶ Depends on the object representation

- ▶ Vector normalization

$$\hat{n} = \frac{\vec{n}}{|\vec{n}|}$$



# Tangent vectors

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- ▶ Parametric representation

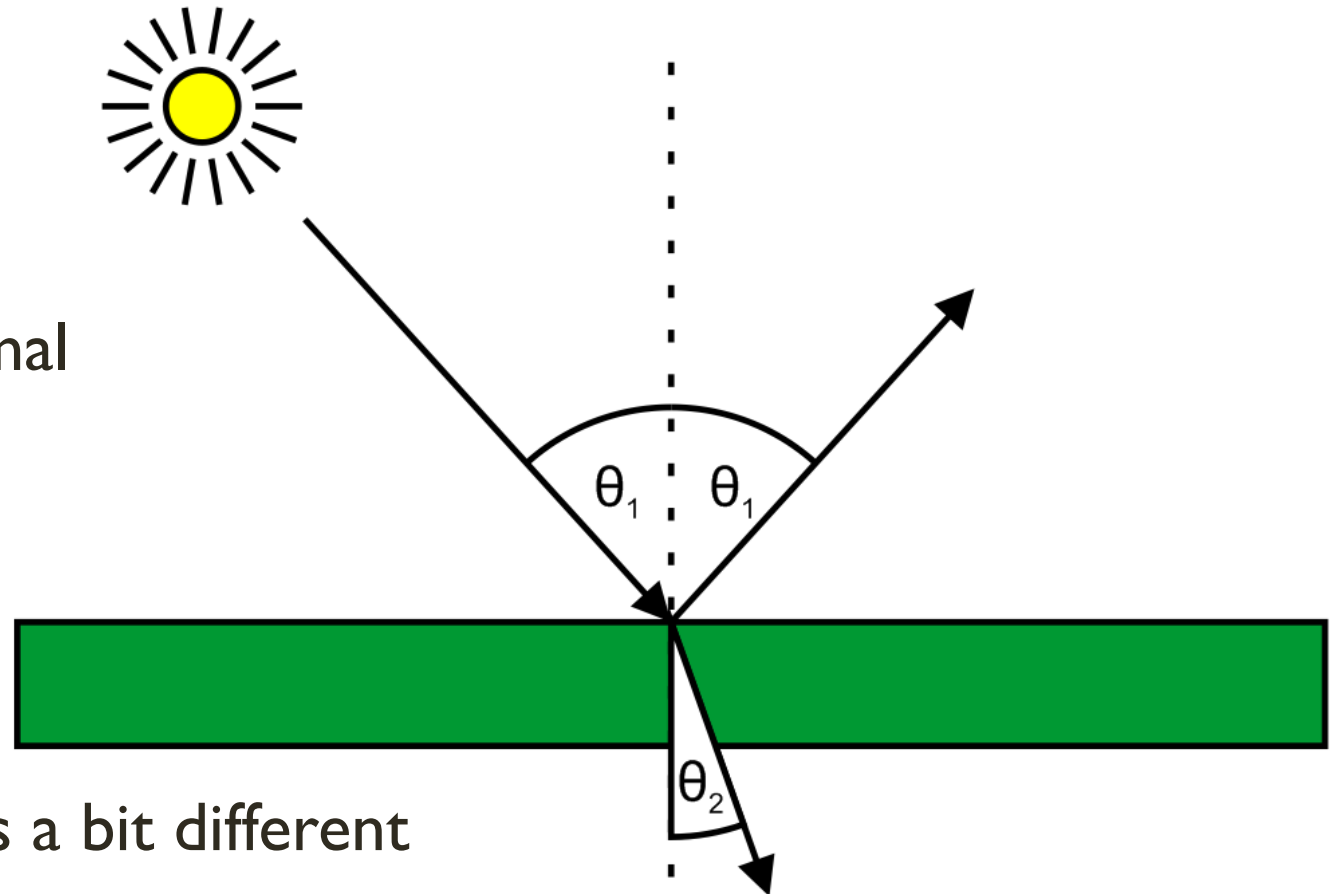
- ▶  $X = x(u,v)$
  - ▶  $Y = y(u,v)$
  - ▶  $Z = z(u,v)$
- ▶ Partial derivation by  $u,v \rightarrow$  vectors  $t_u, t_v$

- ▶ Polygonal representation

- ▶ Tangent vectors are edge vectors
  - ▶ Mind the orientation!

# Elementary theory

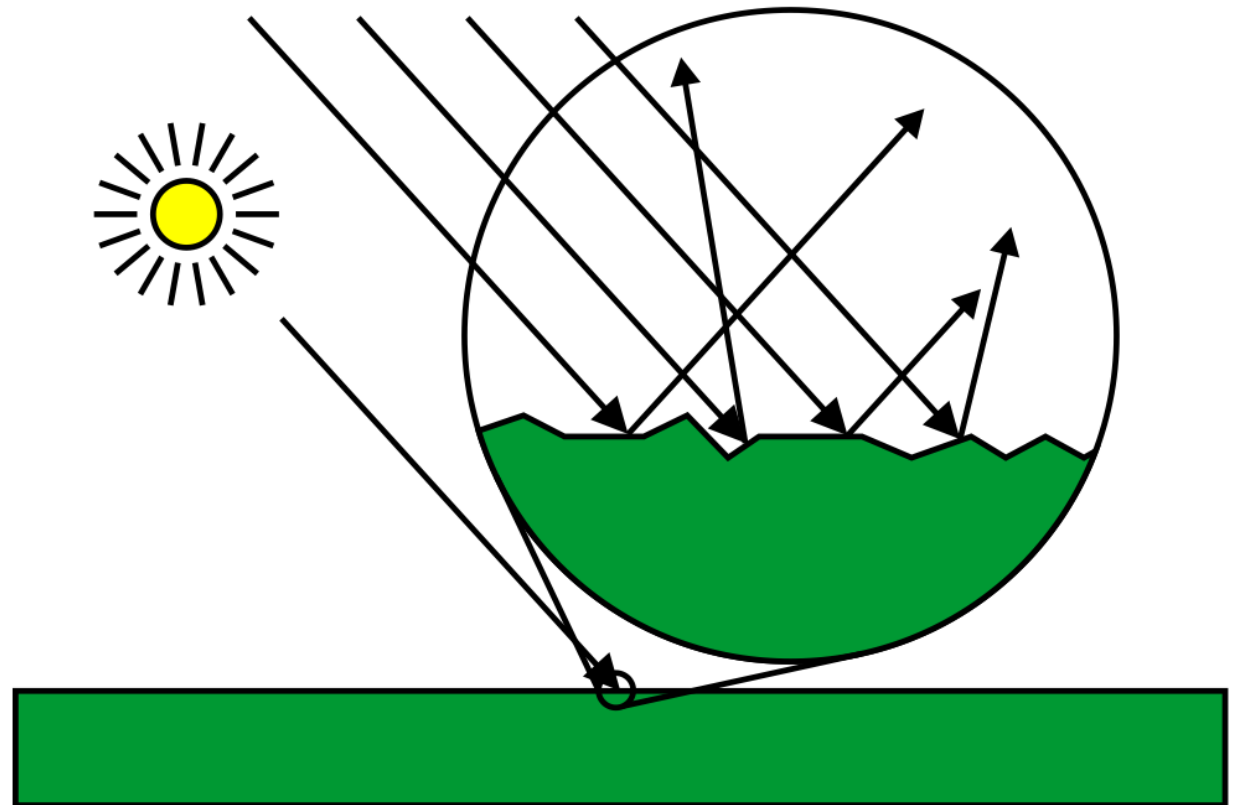
- ▶ Light-surface interaction
- ▶ Reflection
- ▶ Refraction
  - ▶ Snell's law
- ▶ Surface normal vector



- ▶ Real world is a bit different

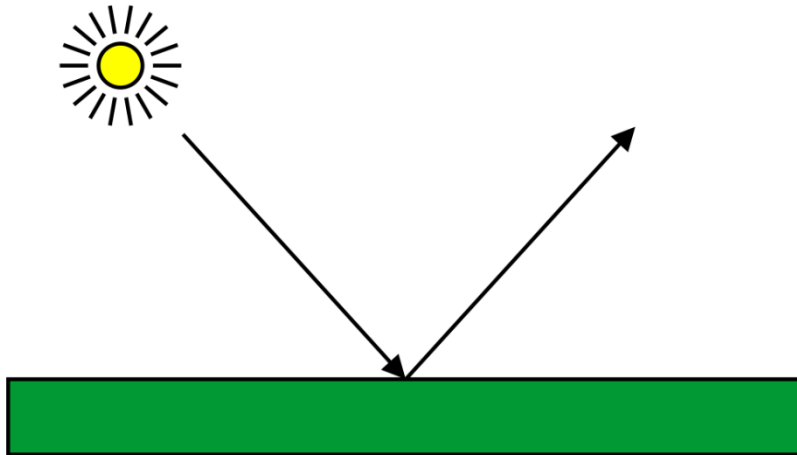
# Surface types

- ▶ Reflective
- ▶ Diffuse – Lambertian
- ▶ Both

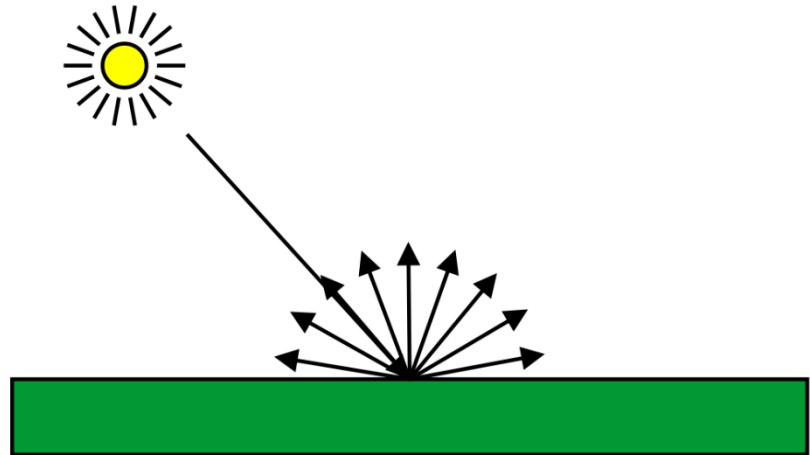


# Surface types

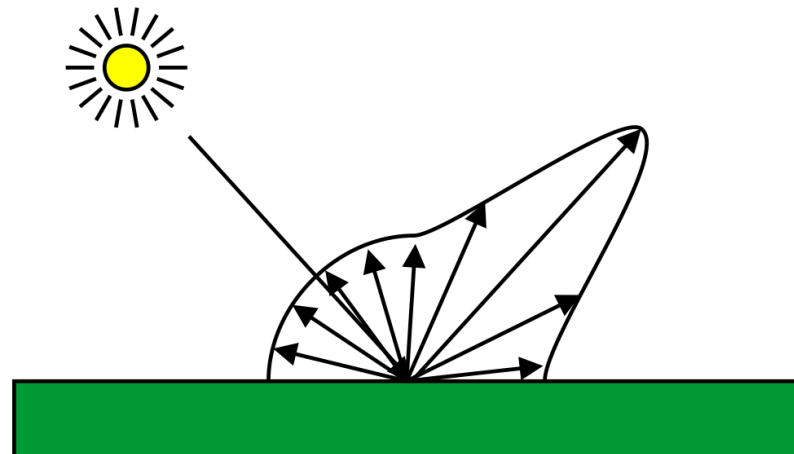
Mirror



Matte



directional  
component



indirectional  
component

# Light models

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- ▶ **Empiric – e.g. Phong lighting model**
  - ▶ cheap computation
  - ▶ physically incorrect
  - ▶ visually plausible
- ▶ **Physically-based**
  - ▶ energy transfer, light propagation
  - ▶ closer to real-world physics
  - ▶ expensive



# Local illumination models

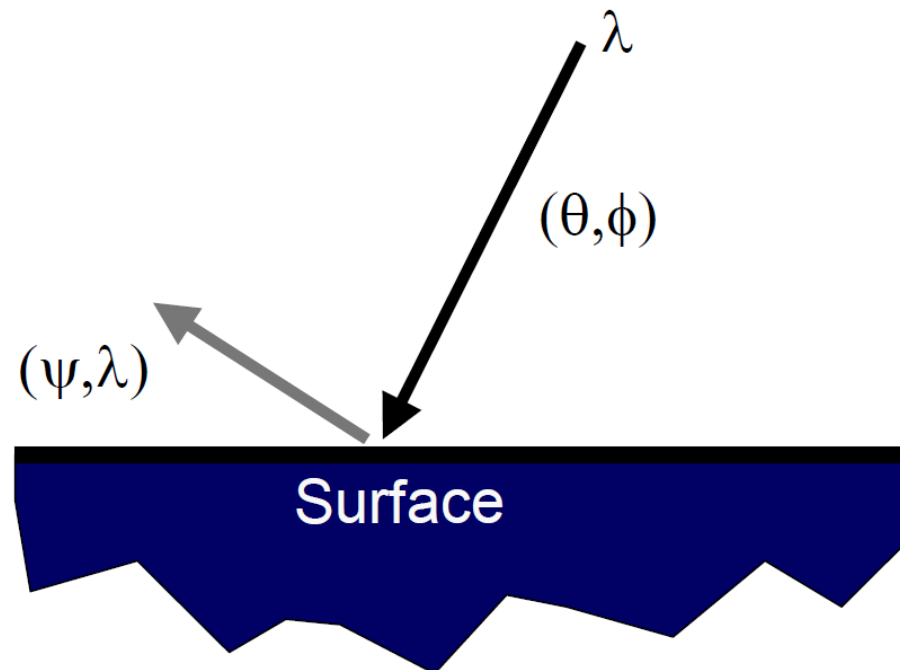
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- ▶ Fast but inaccurate
- ▶ Empirical (no physical background)
- ▶ Many physical effects are impossible to achieve
- ▶ Computer games, real-time rendering



# Modeling Surface Reflectance

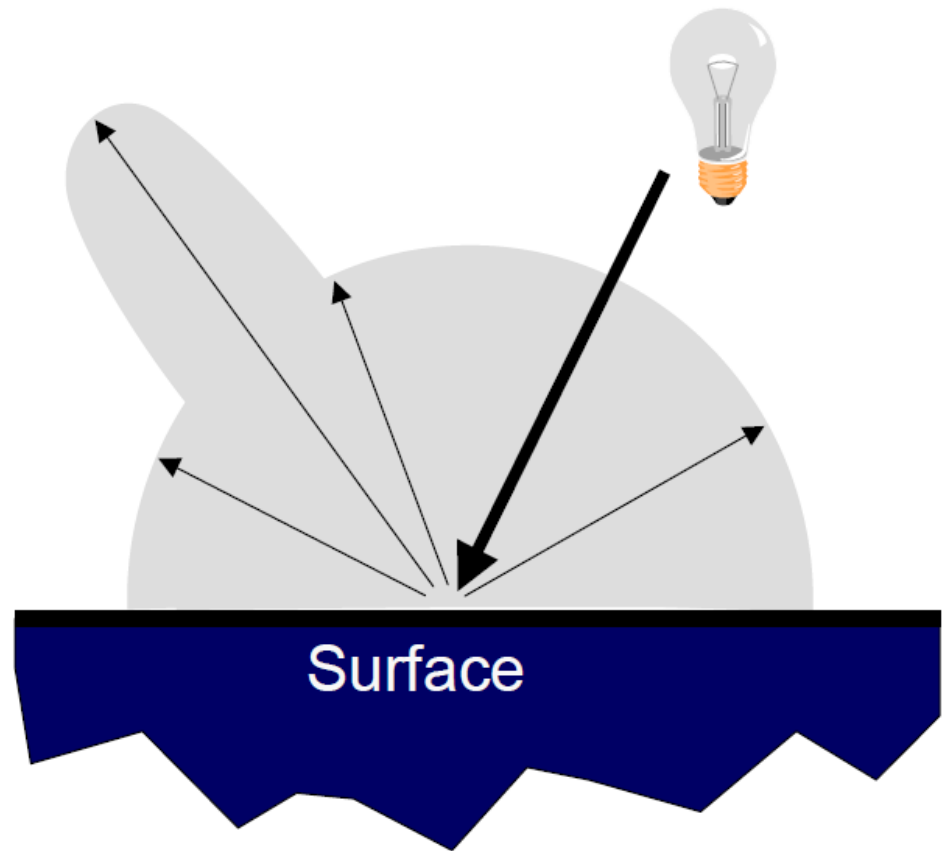
- ▶  $R_s(\theta, \phi, \gamma, \psi, \lambda)$  ...
  - ▶ describes the amount of incident energy, ...
  - ▶ arriving from direction  $(\theta, \phi)$ , ...
  - ▶ leaving in direction  $(\gamma, \psi)$ , ...
  - ▶ with wavelength  $\lambda$



# OpenGL Reflectance Model

## ► Simple empirical model:

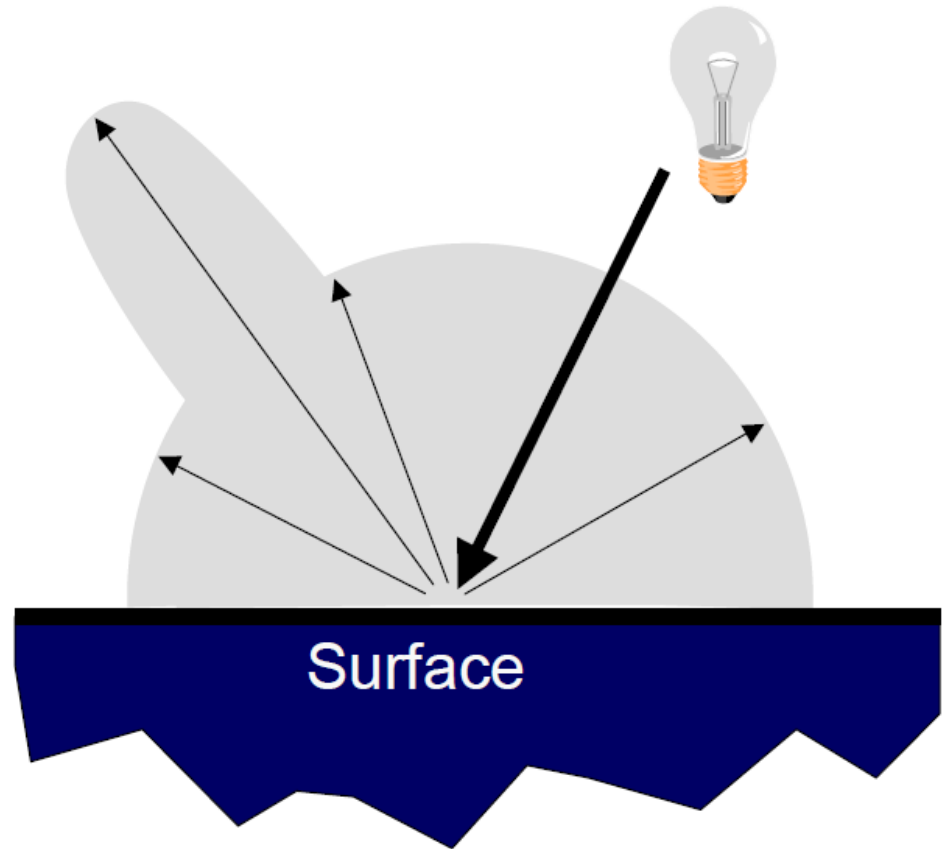
- diffuse reflection +
- specular reflection +
- emission +
- “ambient”
- Bui Tuong Phong, 1973



# OpenGL Reflectance Model

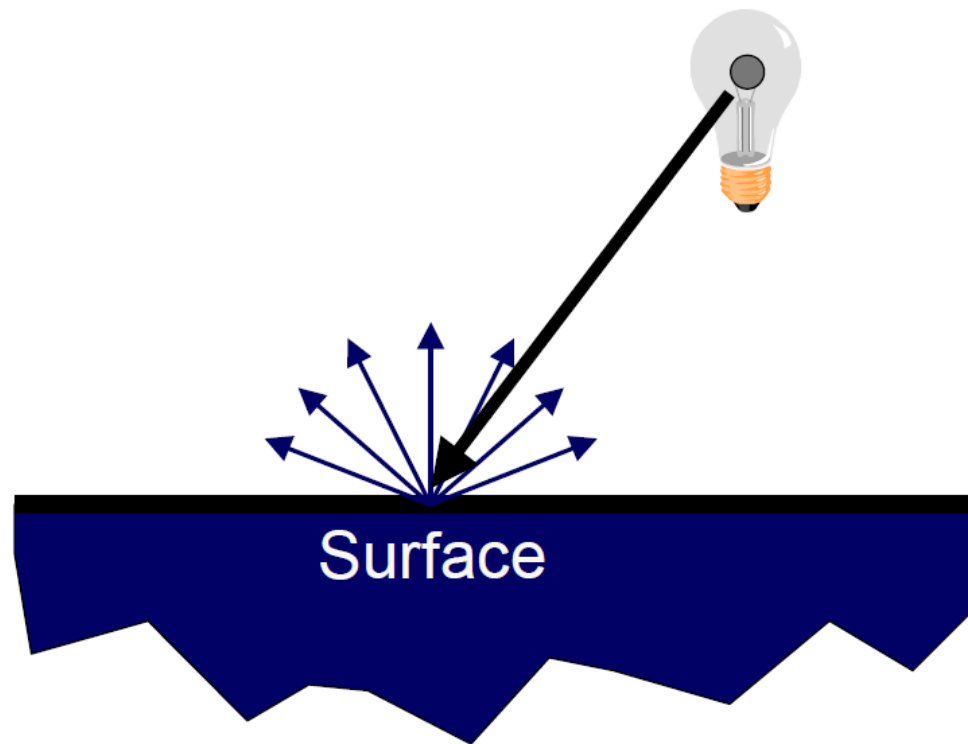
- ▶ Simple empirical model:

- ▶ **diffuse reflection** +
- ▶ specular reflection +
- ▶ emission +
- ▶ “ambient”



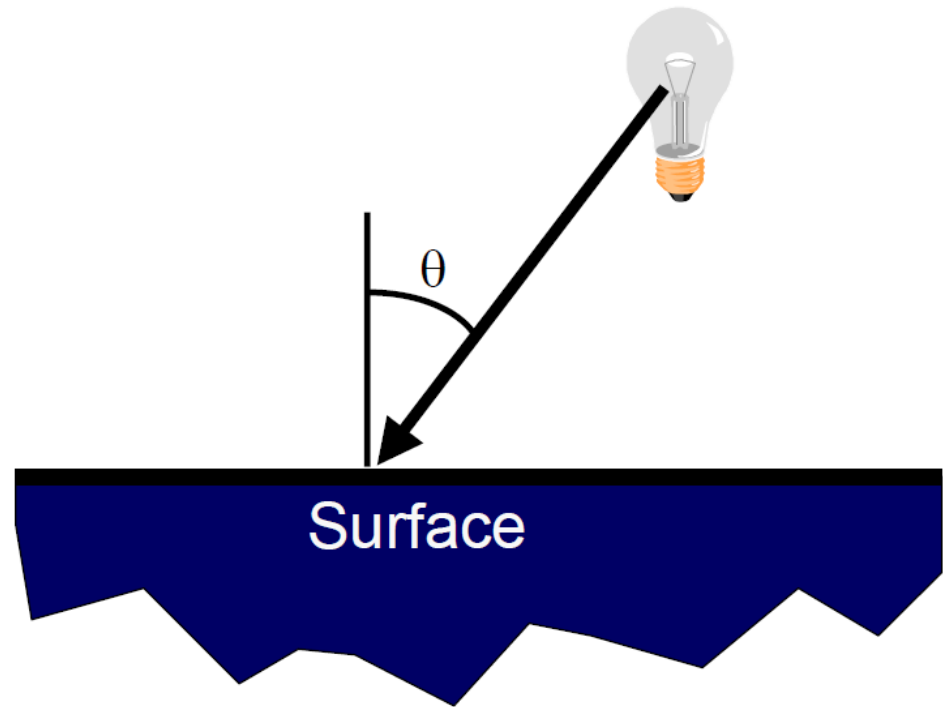
# Diffuse Reflection

- ▶ Assume surface reflects equally in all directions
  - ▶ Examples: chalk, clay



# Diffuse Reflection

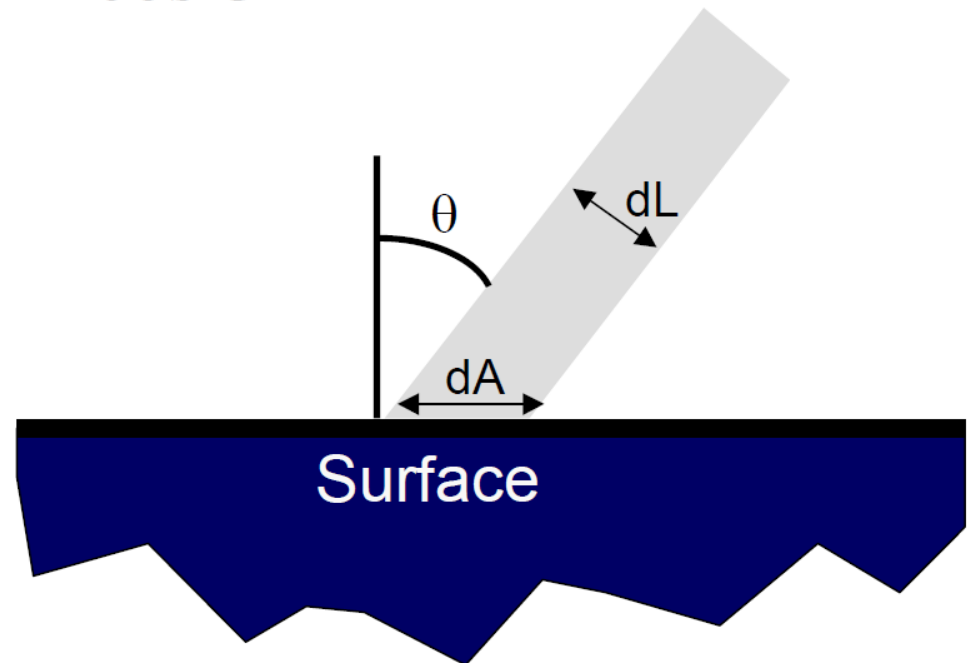
- ▶ How is light reflected ?
  - ▶ Depends on an angle of incident light



# Diffuse Reflection

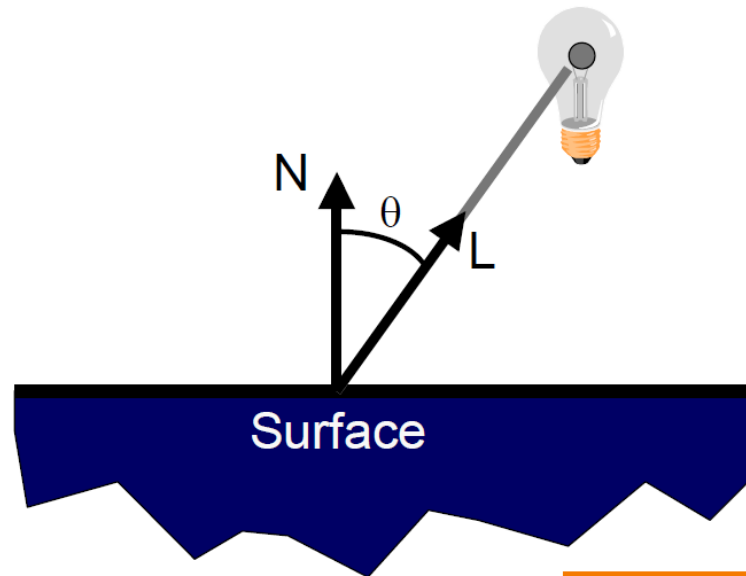
- ▶ How is light reflected ?
  - ▶ Depends on an angle of incident light

$$dL = dA \cos \Theta$$



# Diffuse Reflection

- Lambertian model
  - cosine law (dot product)



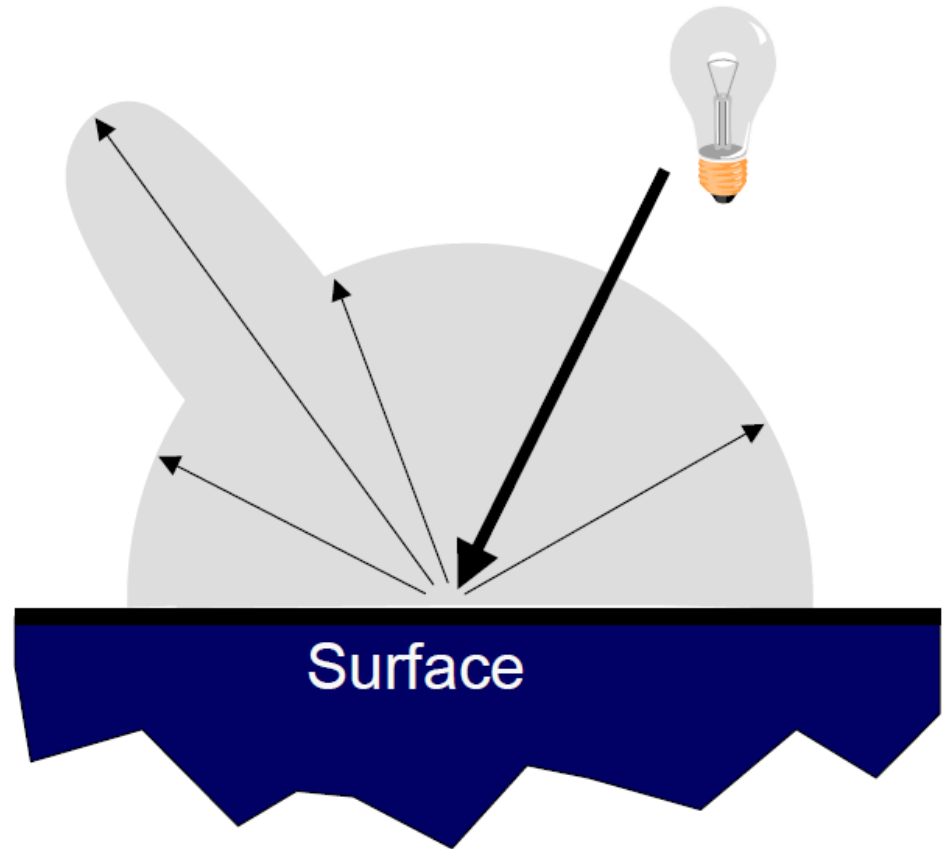
$$I_D = K_D (N \bullet L) I_L$$



# OpenGL Reflectance Model

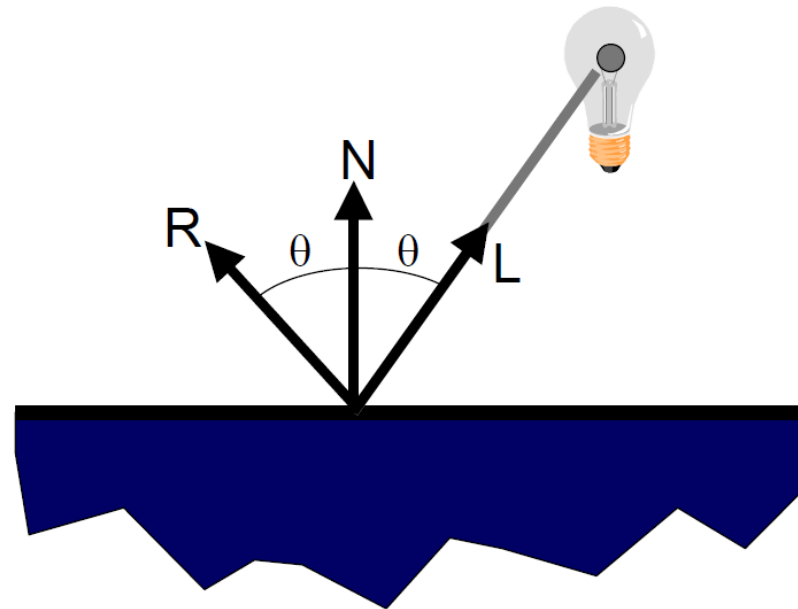
- ▶ Simple empirical model:

- ▶ diffuse reflection +
- ▶ **specular reflection** +
- ▶ emission +
- ▶ “ambient”



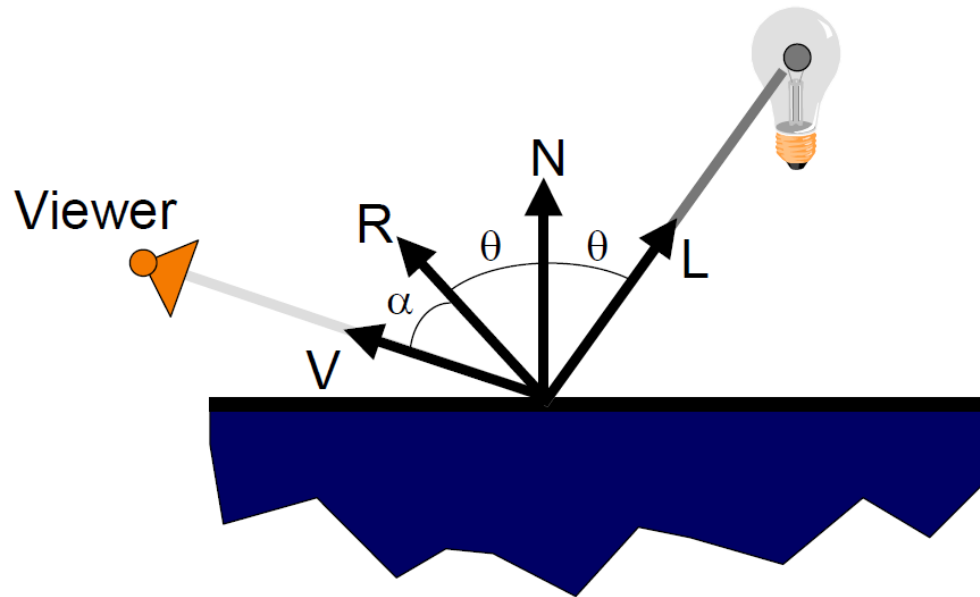
# Specular Reflection

- ▶ Reflection is strongest near mirror angle
  - ▶ Examples: Mirrors, Metals



# Specular Reflection

- ▶ How much light is seen ?
- ▶ Depends on:
  - ▶ angle of incident light
  - ▶ angle of viewer

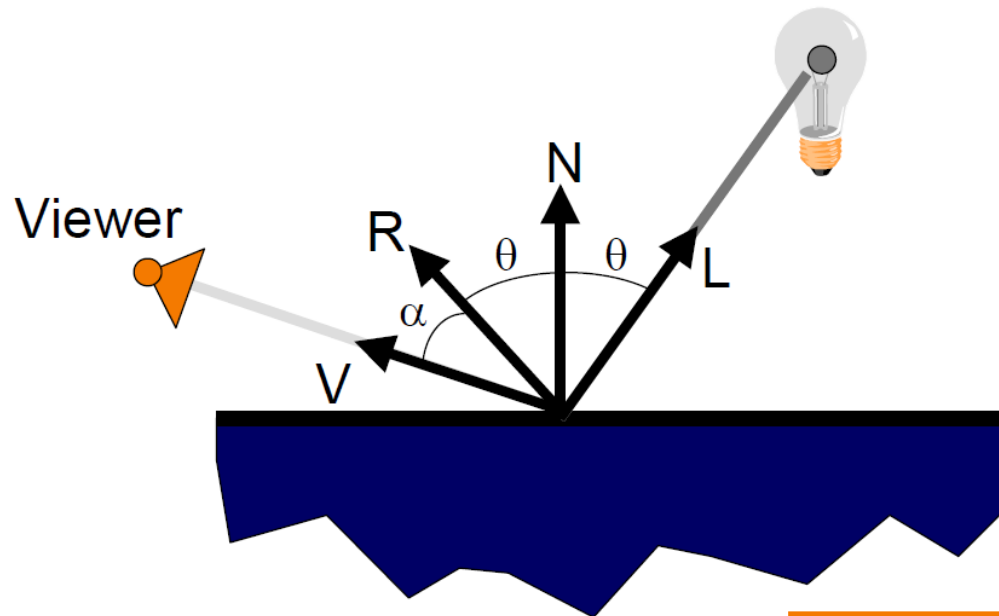


# Specular Reflection

## ► Phong Model

►  $\cos(\alpha)^n$

*This is a physically motivated hack!*

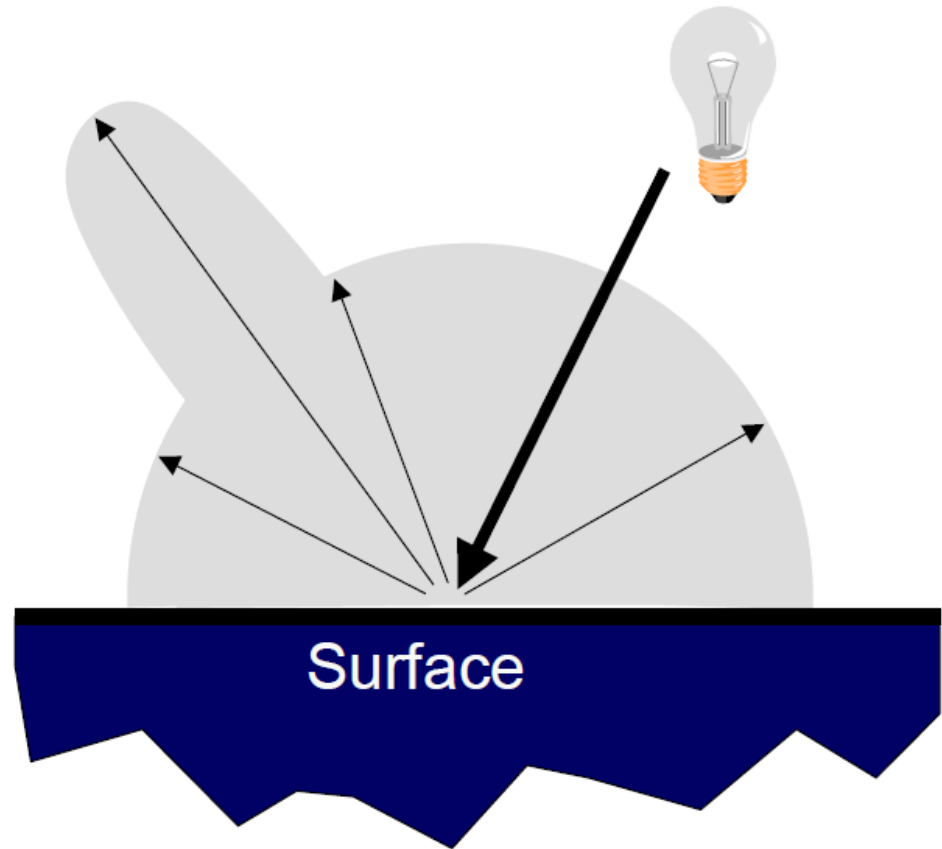


$$I_S = K_S (V \bullet R)^n I_L$$

# OpenGL Reflectance Model

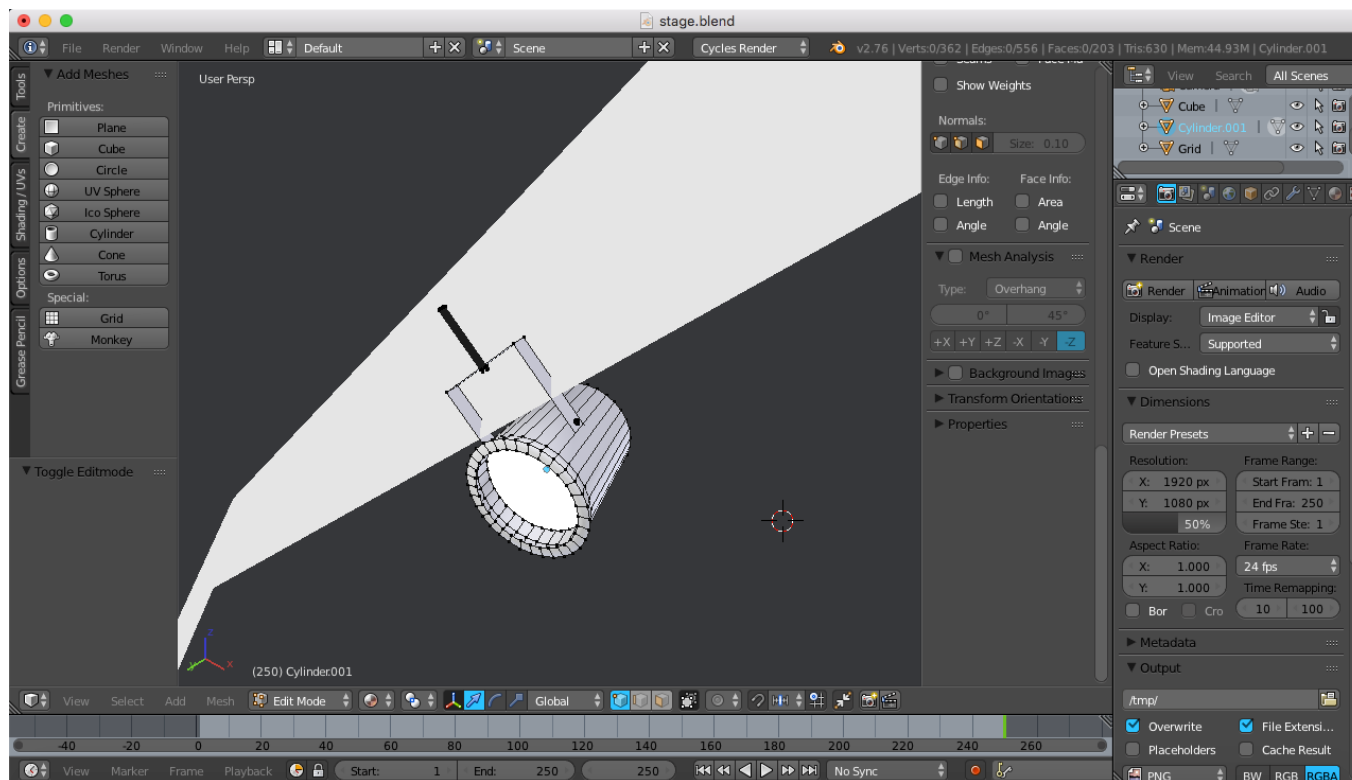
- ▶ Simple empirical model:

- ▶ diffuse reflection +
- ▶ specular reflection +
- ▶ **emission** +
- ▶ “ambient”



# Emission

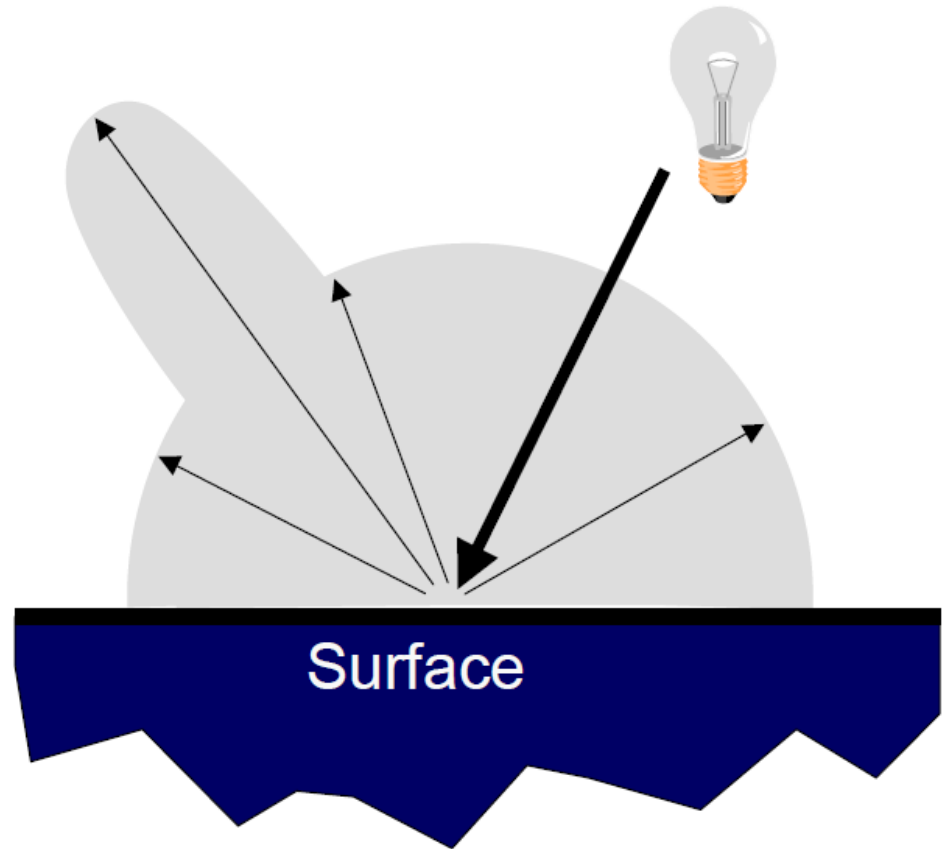
- Represents light emitted directly from surface



# OpenGL Reflectance Model

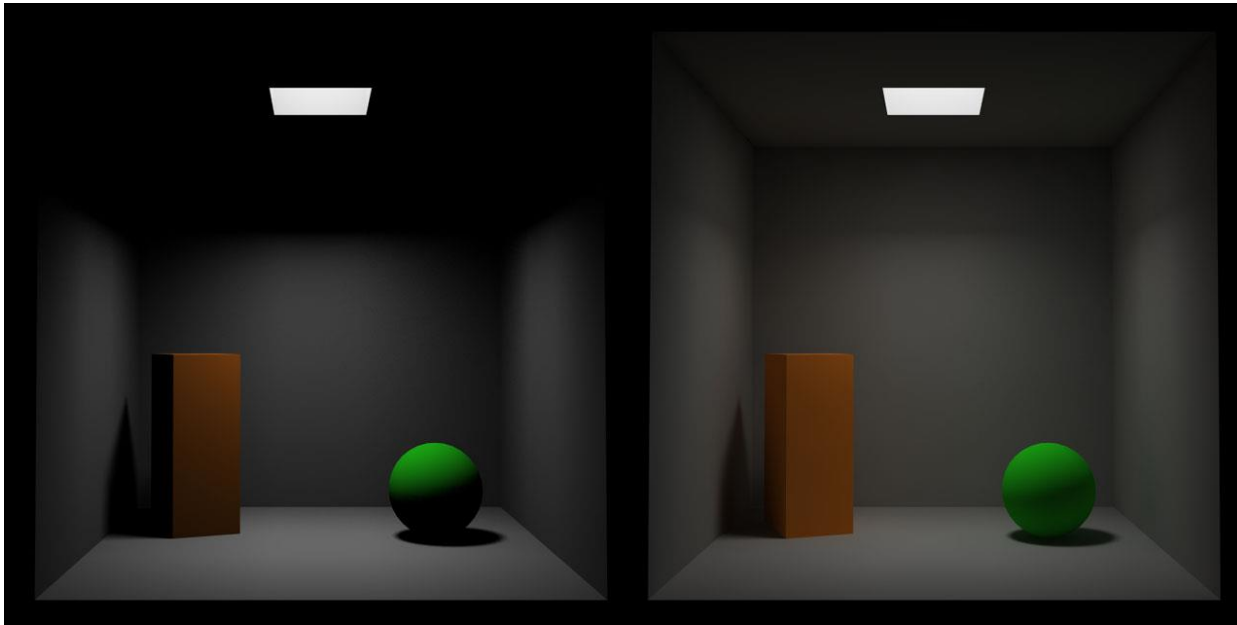
- ▶ Simple empirical model:

- ▶ diffuse reflection +
- ▶ specular reflection +
- ▶ emission +
- ▶ “ambient”



# Ambient term

- ▶ Represents reflection of all indirect illumination
- ▶ This is a total hack
  - ▶ (avoids complexity of global illumination)!

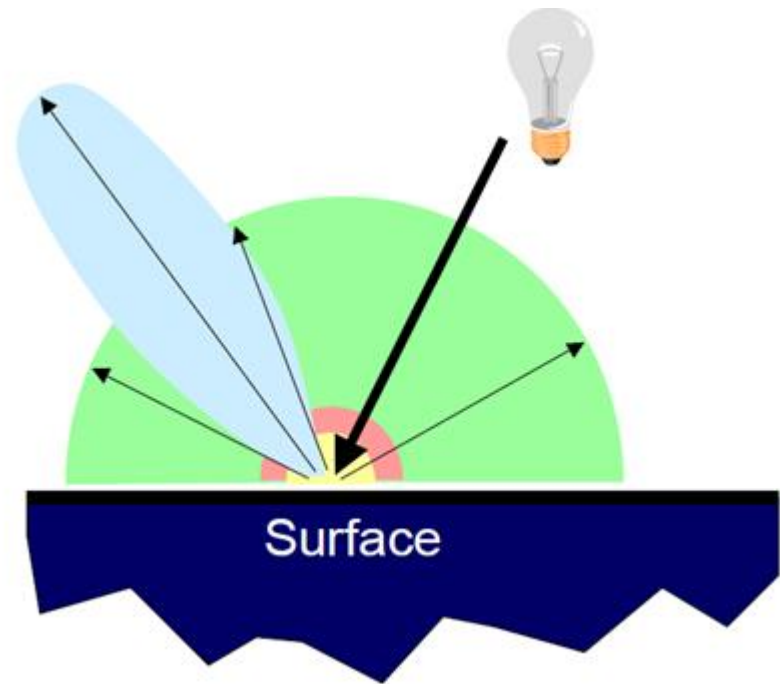




# OpenGL Reflectance Model

- ▶ Simple empirical model:

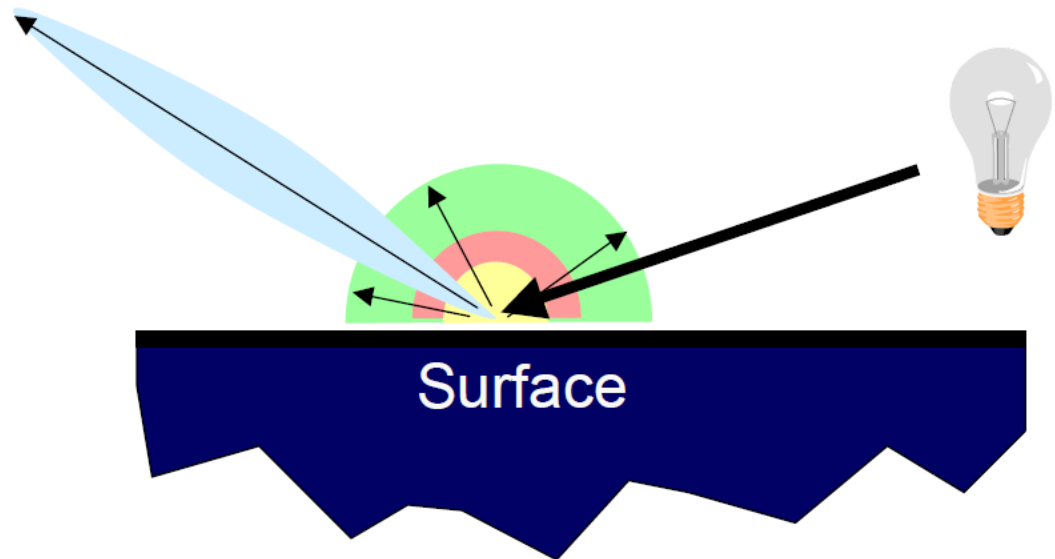
- ▶ diffuse reflection +
- ▶ specular reflection +
- ▶ emission +
- ▶ “ambient”



# OpenGL Reflectance Model

- ▶ Simple empirical model:

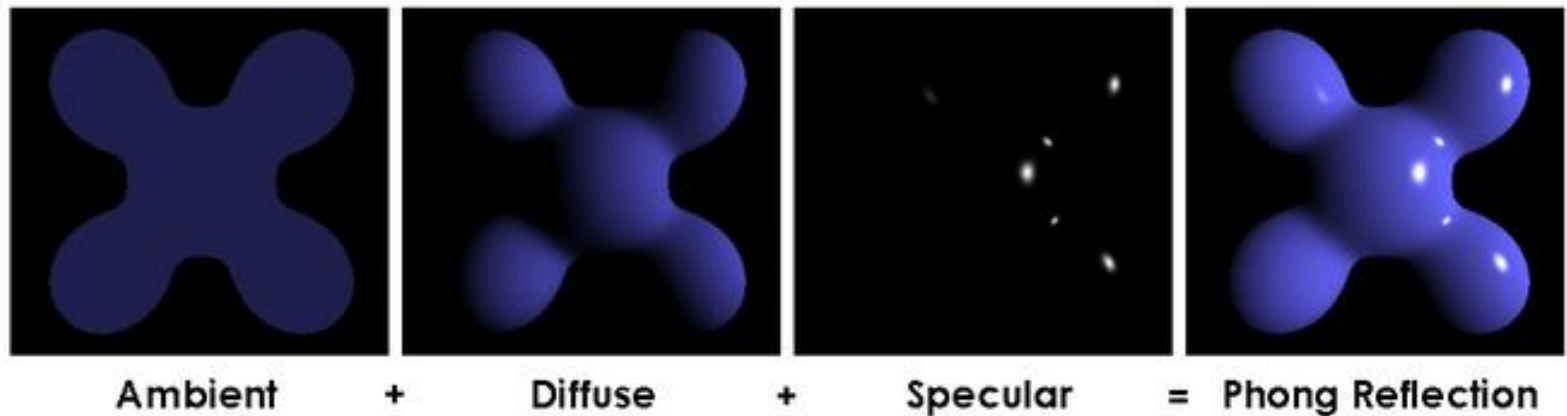
- ▶ diffuse reflection +
- ▶ specular reflection +
- ▶ emission +
- ▶ “ambient”



# OpenGL Reflectance Model

- ▶ Simple empirical model:

- ▶ diffuse reflection +
- ▶ specular reflection +
- ▶ emission +
- ▶ “ambient”



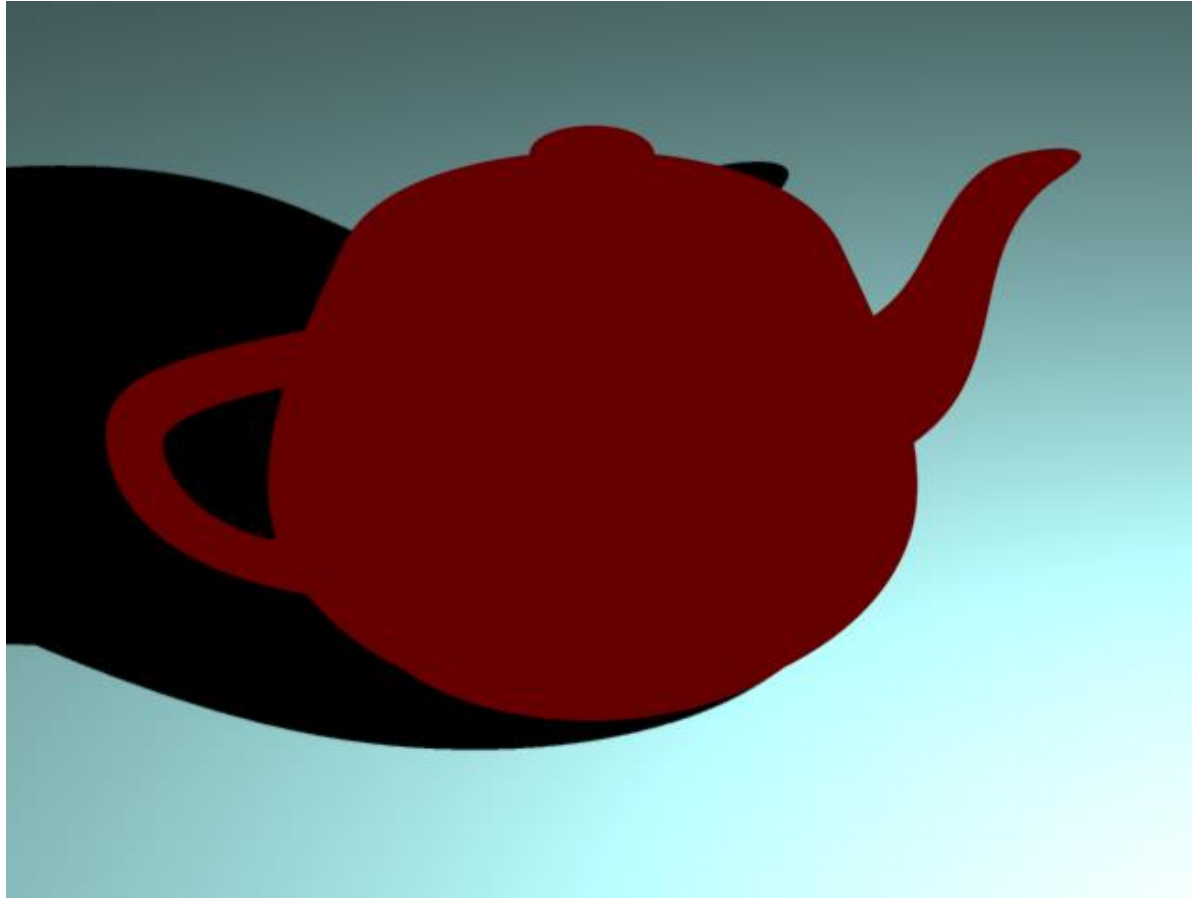
# Diffuse light

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# Ambient light

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# Diffuse + Ambient light

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# Specular + Diffuse + Ambient light

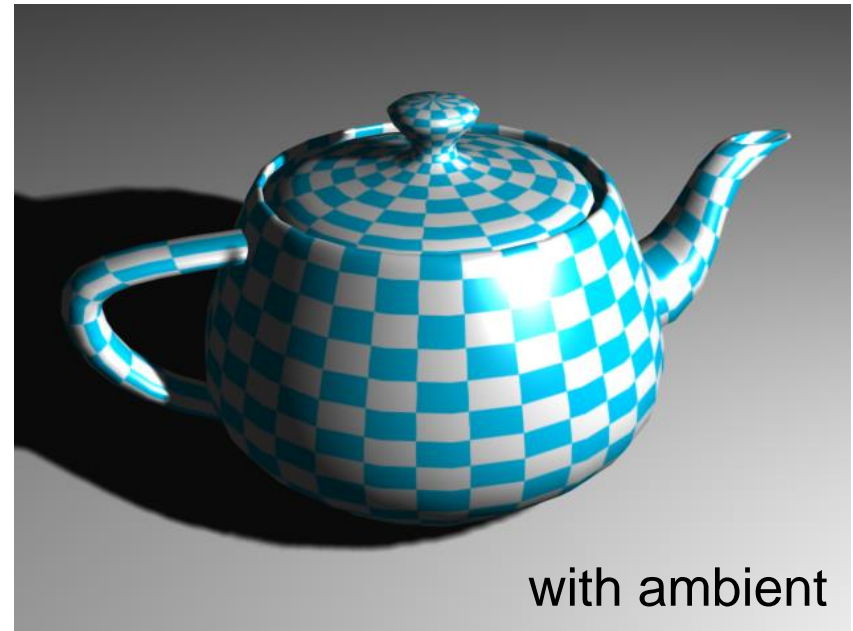
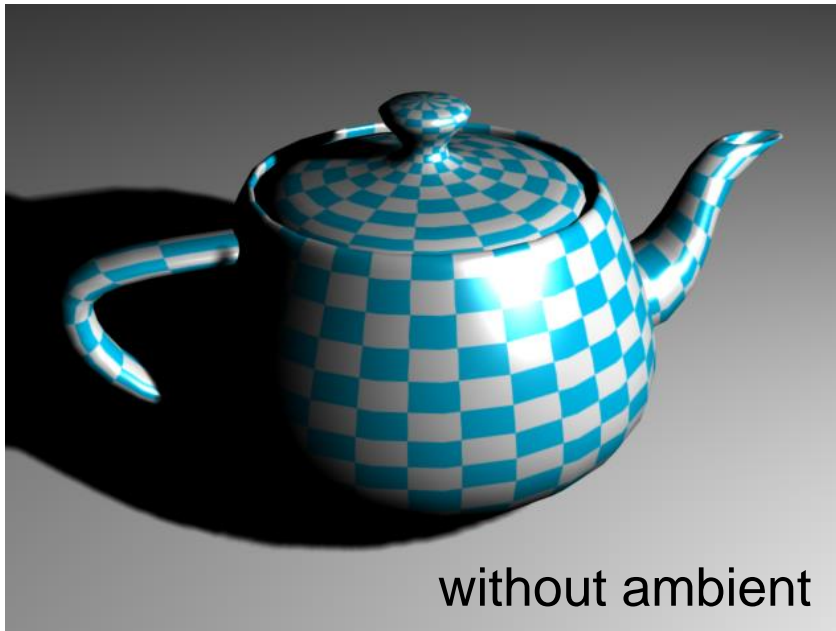
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# Phong lighting model

- **Ambient** + Diffuse + Specular components



- Simulates global light scattered in the scene and reflected from other objects



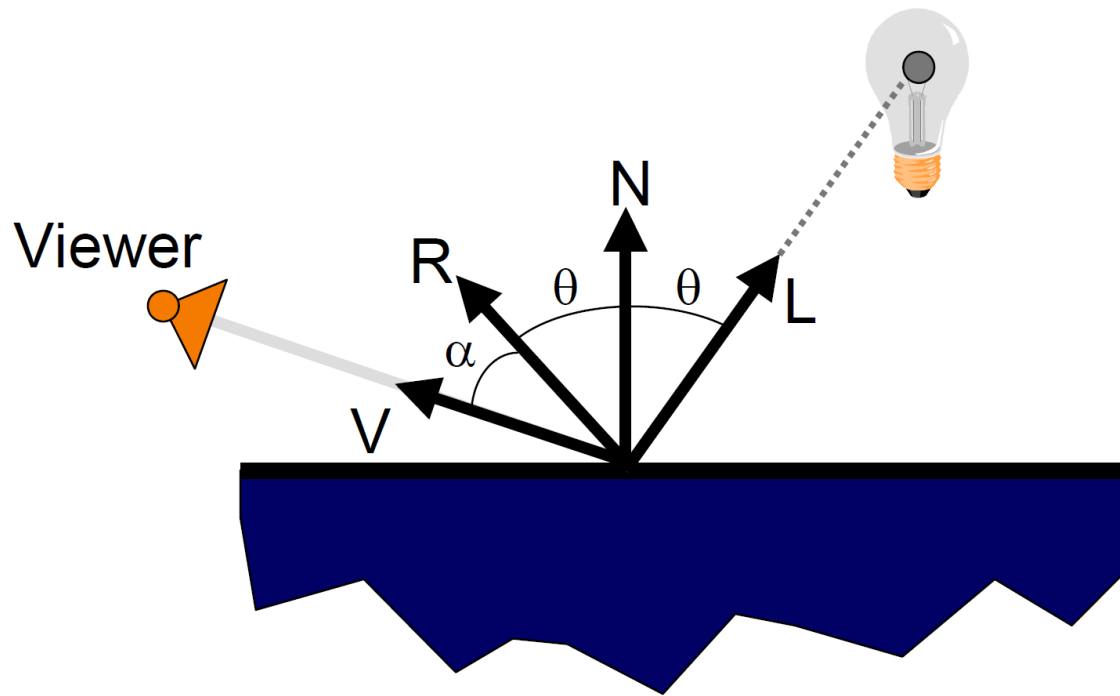
# Other lighting models

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- ▶ **Blinn-Phong**
  - ▶ generalization of Phong's model
- ▶ **Cook-Torrance**
  - ▶ microfacets
- ▶ **Oren-Nayar**
  - ▶ rough surfaces
- ▶ **Anisotropic microfacet distribution**

# Direct Illumination

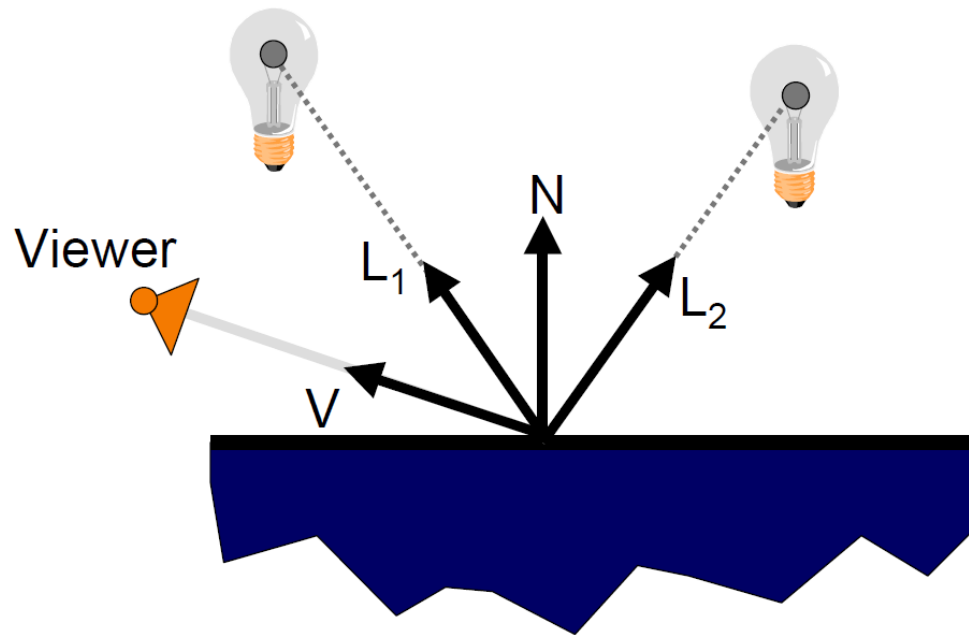
## ► Single light source example



$$I = I_E + K_A I_{AL} + K_D (N \cdot L) I_L + K_S (V \cdot R)^n I_L$$

# Direct Illumination

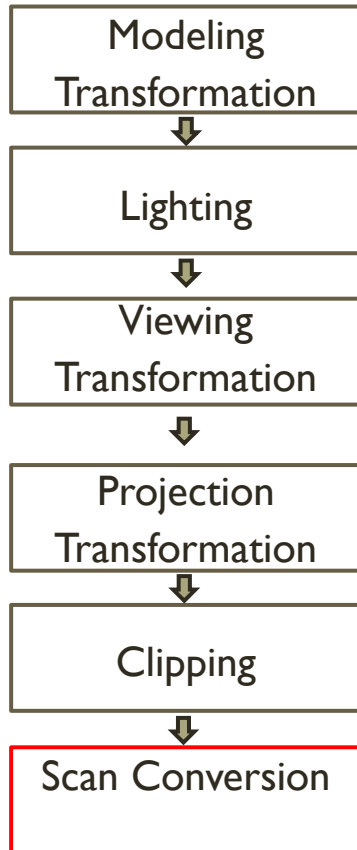
## ► Multiple light source example



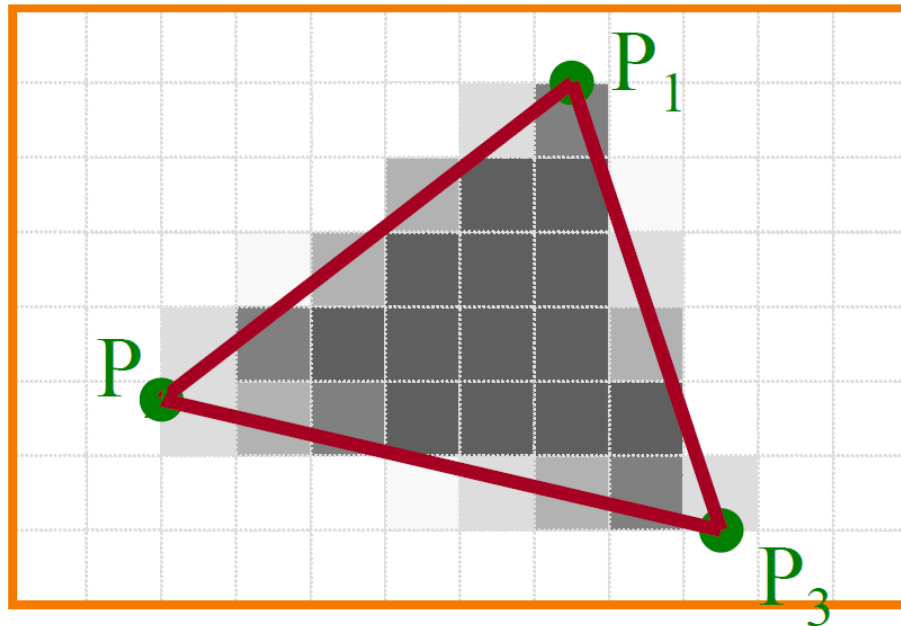
$$I = I_E + K_A I_{AL} + \sum_i (K_D (N \cdot L_i) I_i + K_S (V \cdot R_i)^n I_i)$$

# 3D rendering pipeline

3D polygons



2D Image



Draw pixels

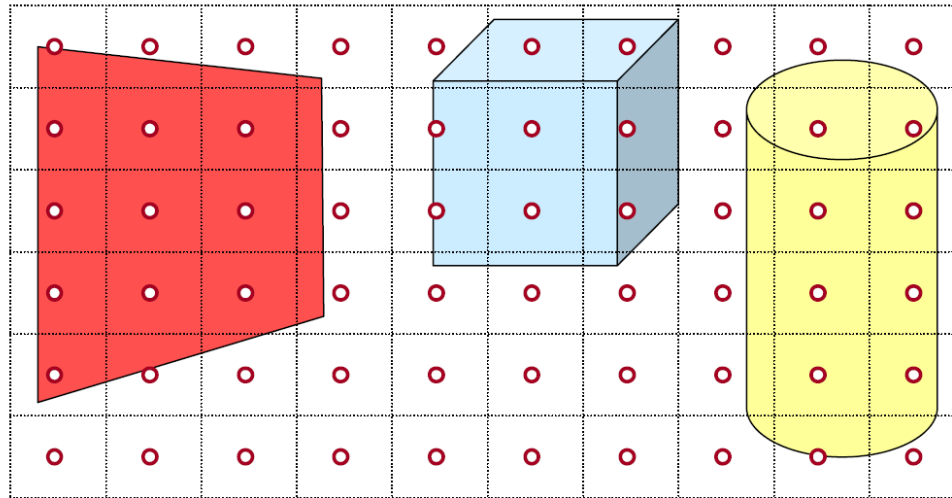
# Pixel Shading

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How to effectively get the value  
of the illumination model  
for each pixel ?

# Ray Casting

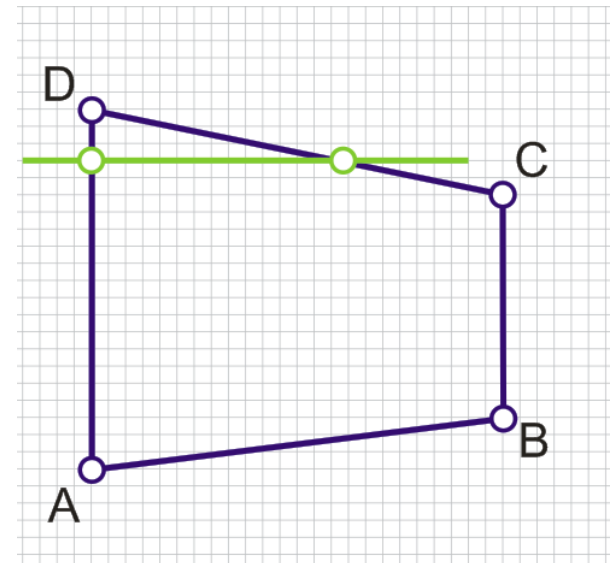
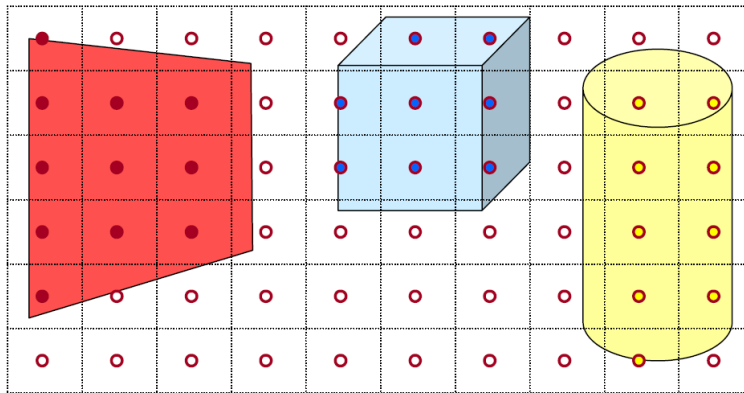
- Independent lighting calculation for each pixel
  - Computationally expensive



$$I = I_E + K_A I_{AL} + \sum_i (K_D (N \bullet L_i) I_i + K_S (V \bullet R_i)^n I_i)$$

# Polygon Shading

- Can take advantage of spatial coherence
  - Illumination calculations of pixels of a triangle are related
  - Scanline rasterization



$$I = I_E + K_A I_{AL} + \sum_i (K_D (N \bullet L_i) I_i + K_S (V \bullet R_i)^n I_i)$$

# Overview

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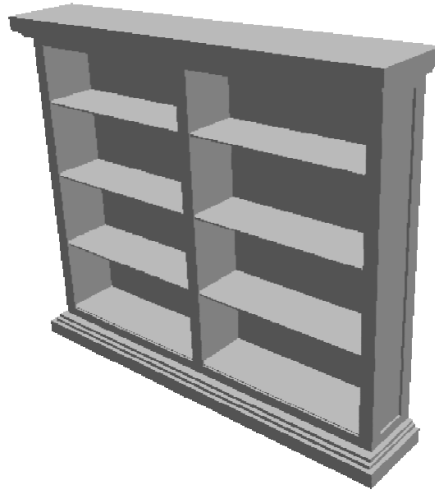
- ▶ Global Illumination
  - ▶ Shadows
  - ▶ Refractions
  - ▶ Inter-object reflections
- ▶ **Shading**
  - ▶ Flat
  - ▶ Gouraud
  - ▶ Phong





# Flat Shading

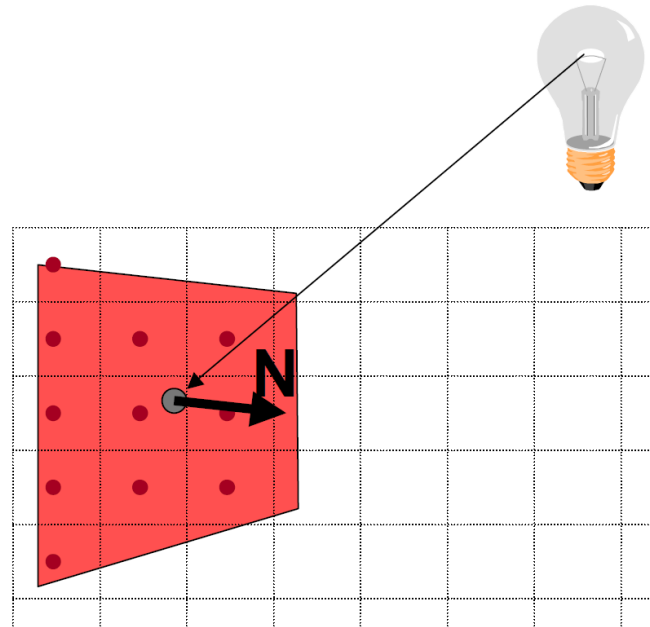
- Fill triangles using single calculated color



$$I = I_E + K_A I_{AL} + \sum_i (K_D (N \bullet L_i) I_i + K_S (V \bullet R_i)^n I_i)$$

# Flat Shading

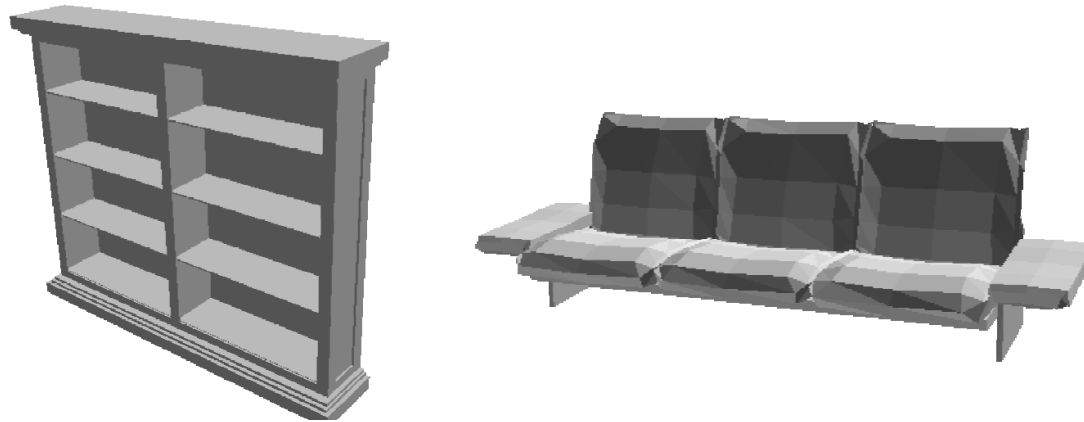
- ▶ One Illumination calculation per polygon
- ▶ Assign all pixels of each polygon the same color



# Flat Shading

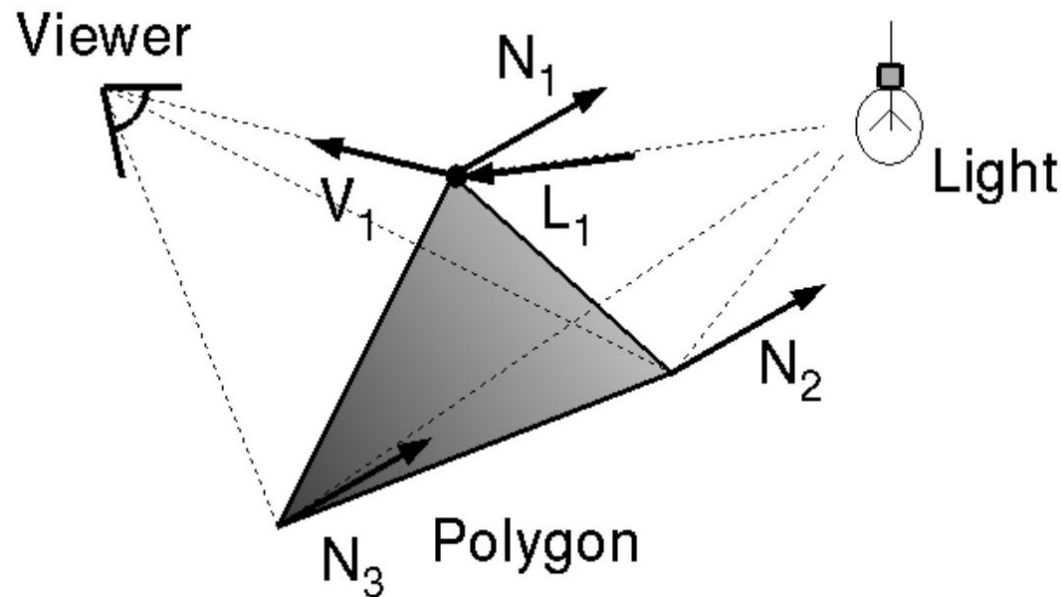
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- ▶ Objects look like they are composed of polygons
- ▶ Ok for polyhedral objects
- ▶ Not so good for smooth surfaces



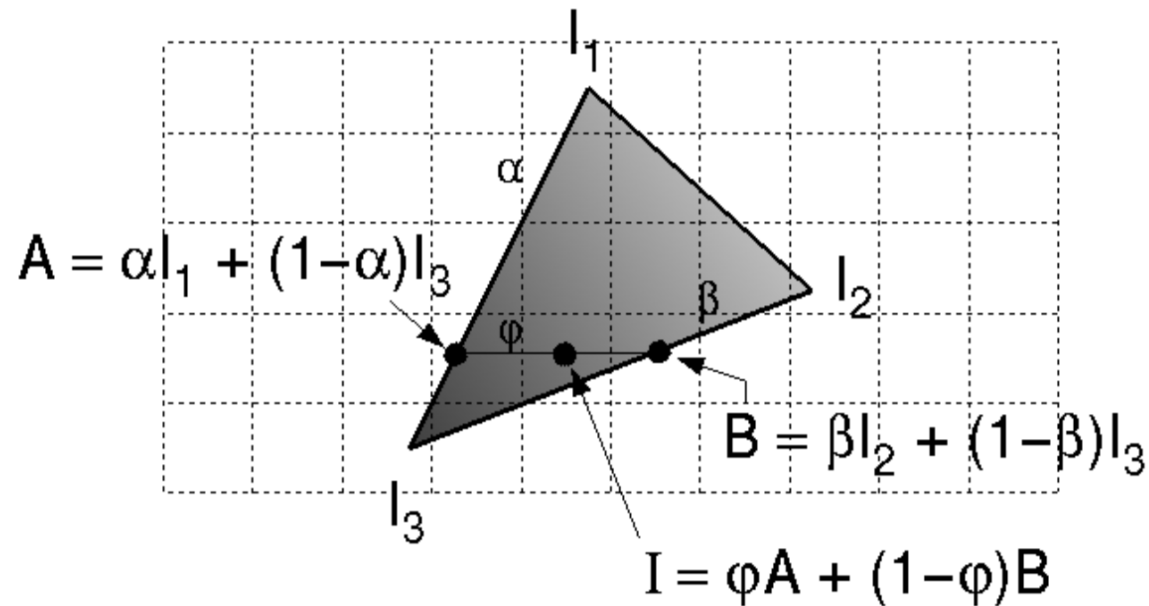
# Gouraud Shading

- ▶ One lighting calculation per vertex
- ▶ Assign pixels inside polygon by interpolating colors computed at vertices



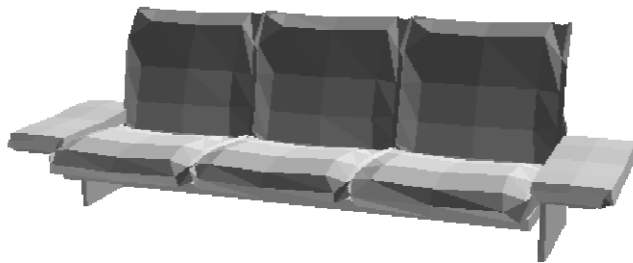
# Gouraud Shading

- Bilinearly interpolate colors of triangle across scan line

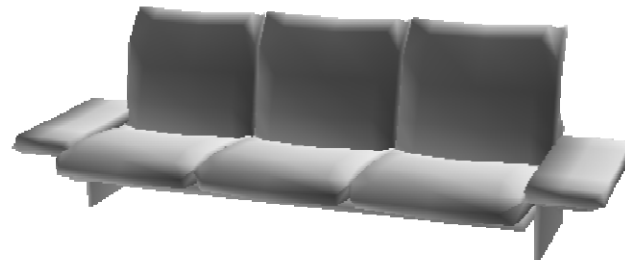


# Gouraud Shading

- ▶ Smooth shading over adjacent polygons
  - ▶ Curved surfaces
  - ▶ Illumination highlights
- ▶ Produces smoothly shaded polygonal mesh
  - ▶ Fast linear approximation
  - ▶ Needs fine mesh to capture subtle lighting effects



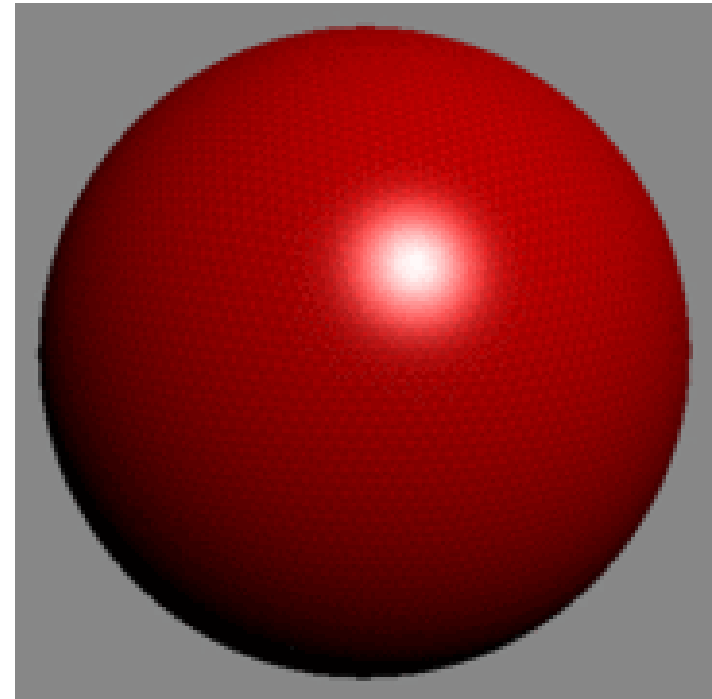
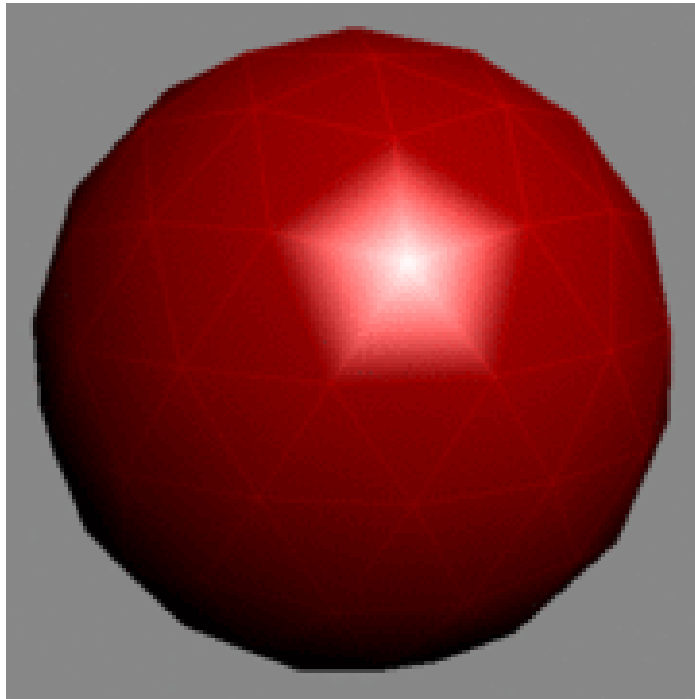
Flat Shading



Gouraud Shading

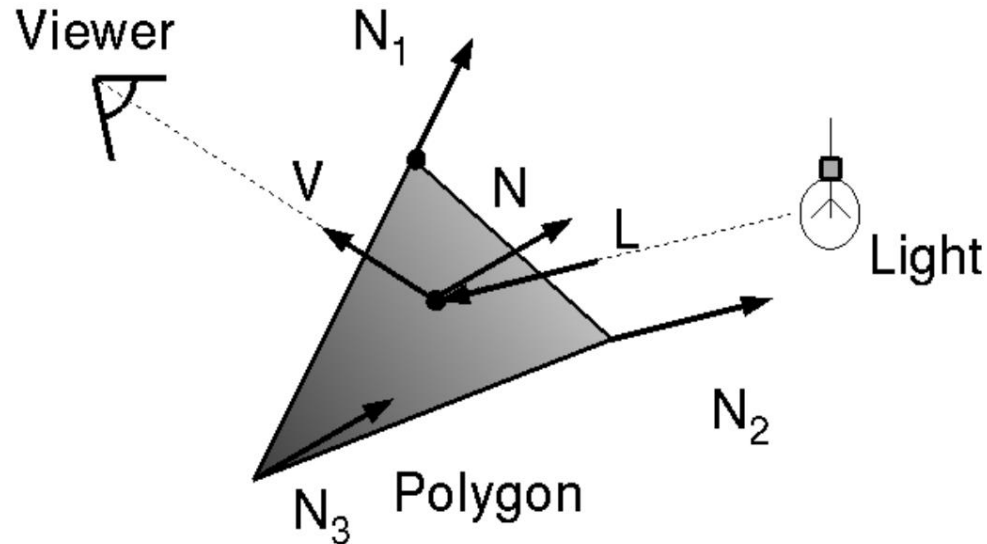
# Gouraud Shading

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# Phong Shading

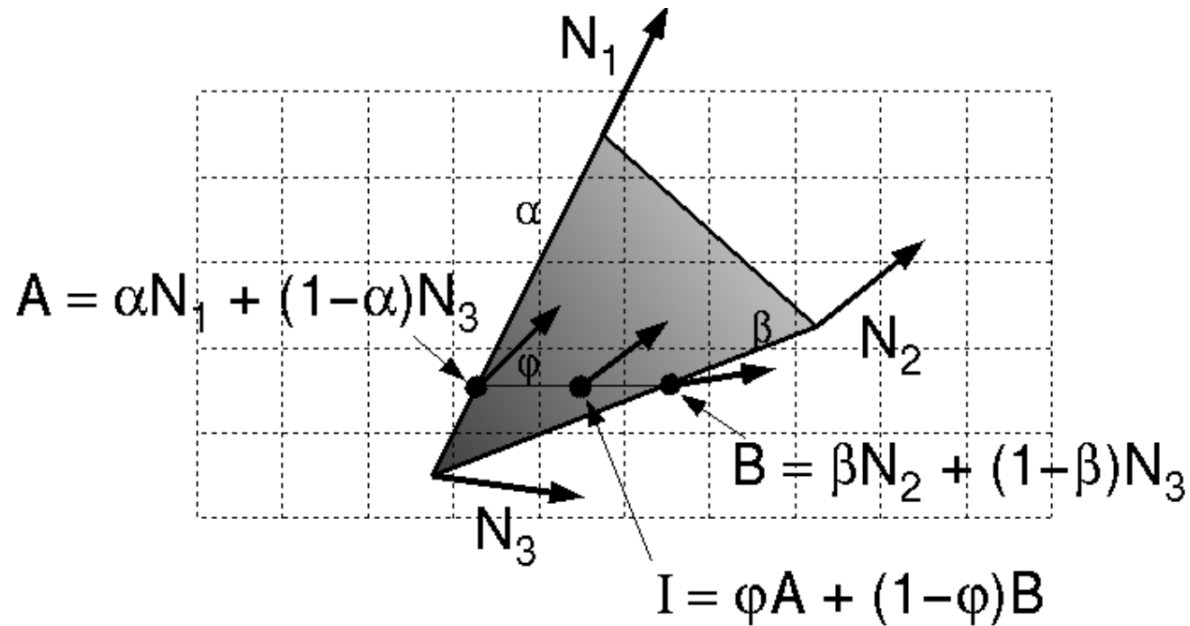
- ▶ NOT Phong lighting model
- ▶ One lighting calculation per pixel
  - ▶ Approximate surface normals inside polygon using bilinear interpolation of normals from vertices



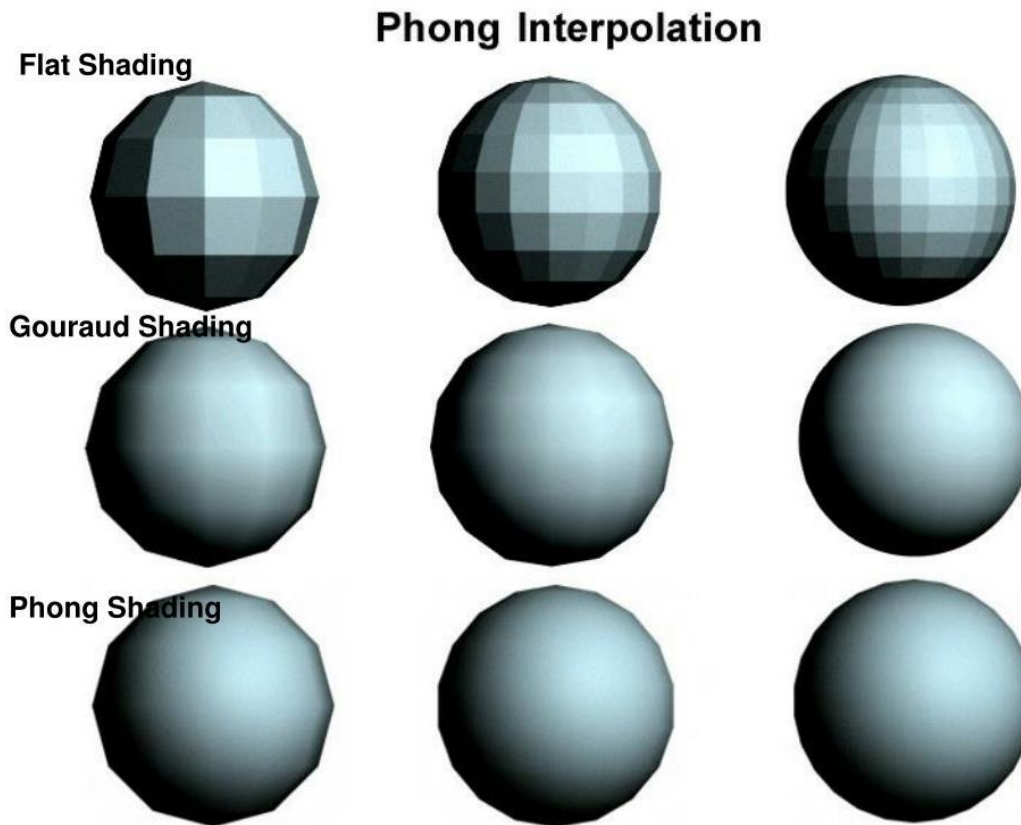


# Phong Shading

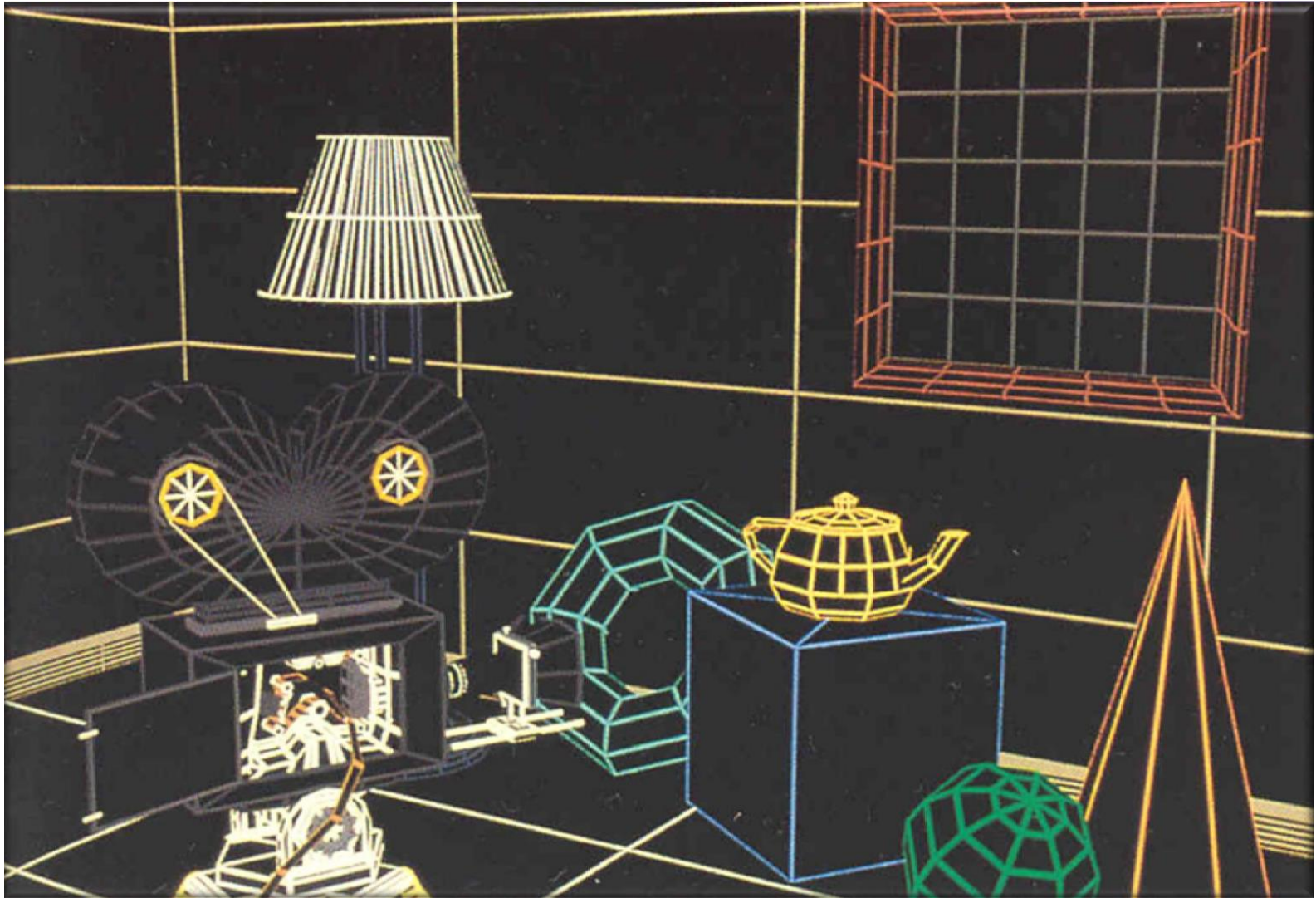
- Bilinearly interpolate surface normals at vertices down and across scan lines



# Polygon Shading Algorithms

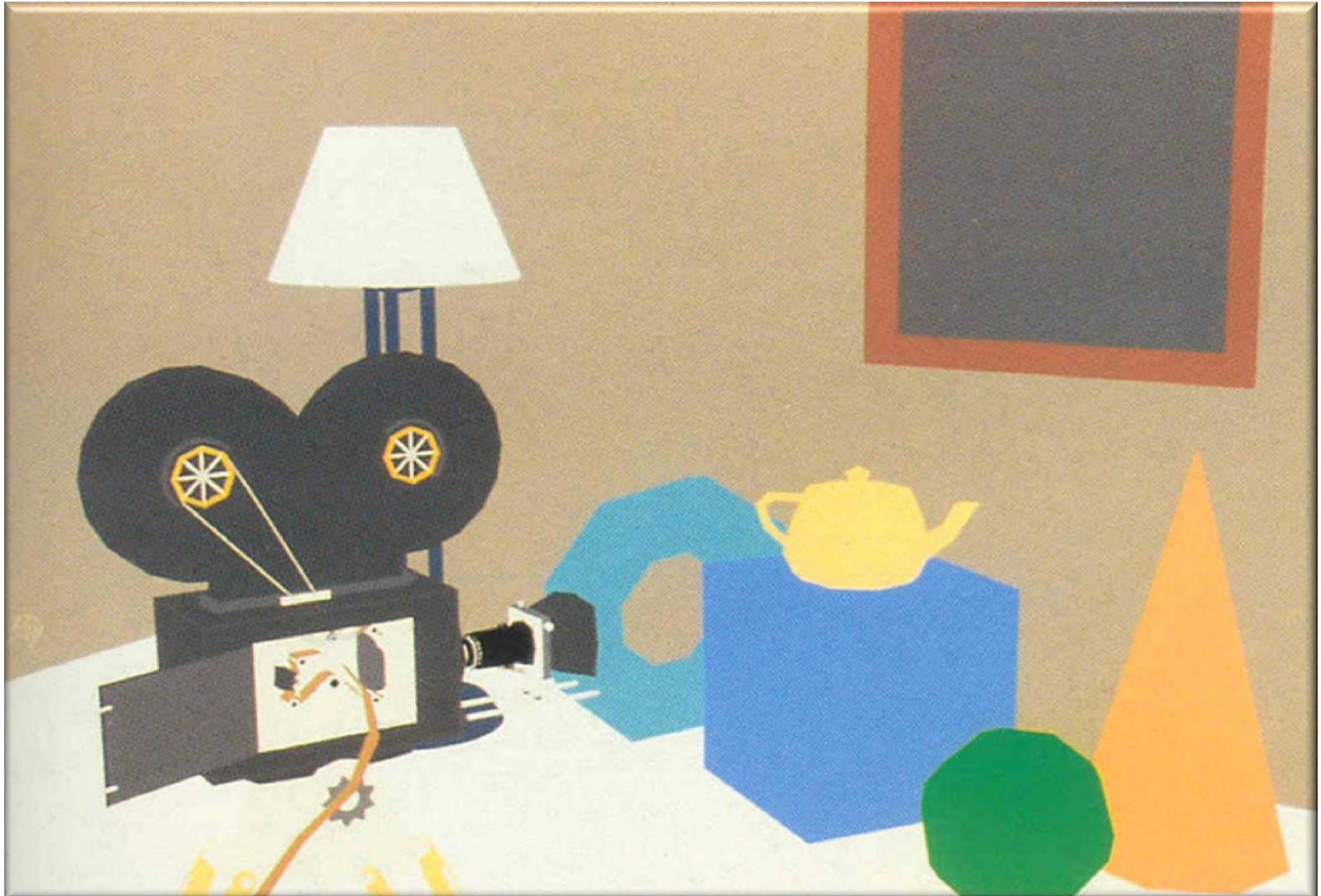


# Example: Wireframe scene



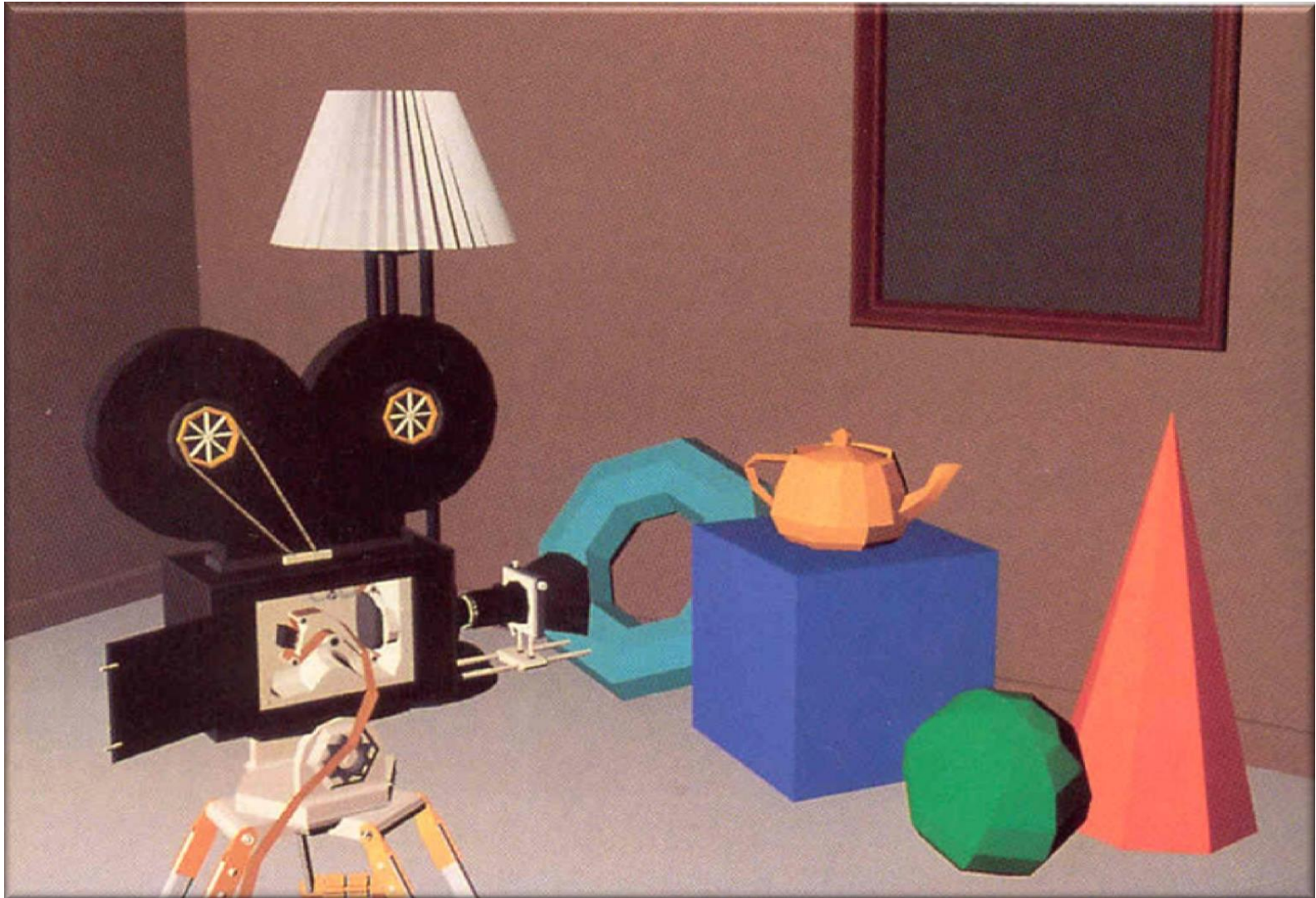


# Example: Ambient only



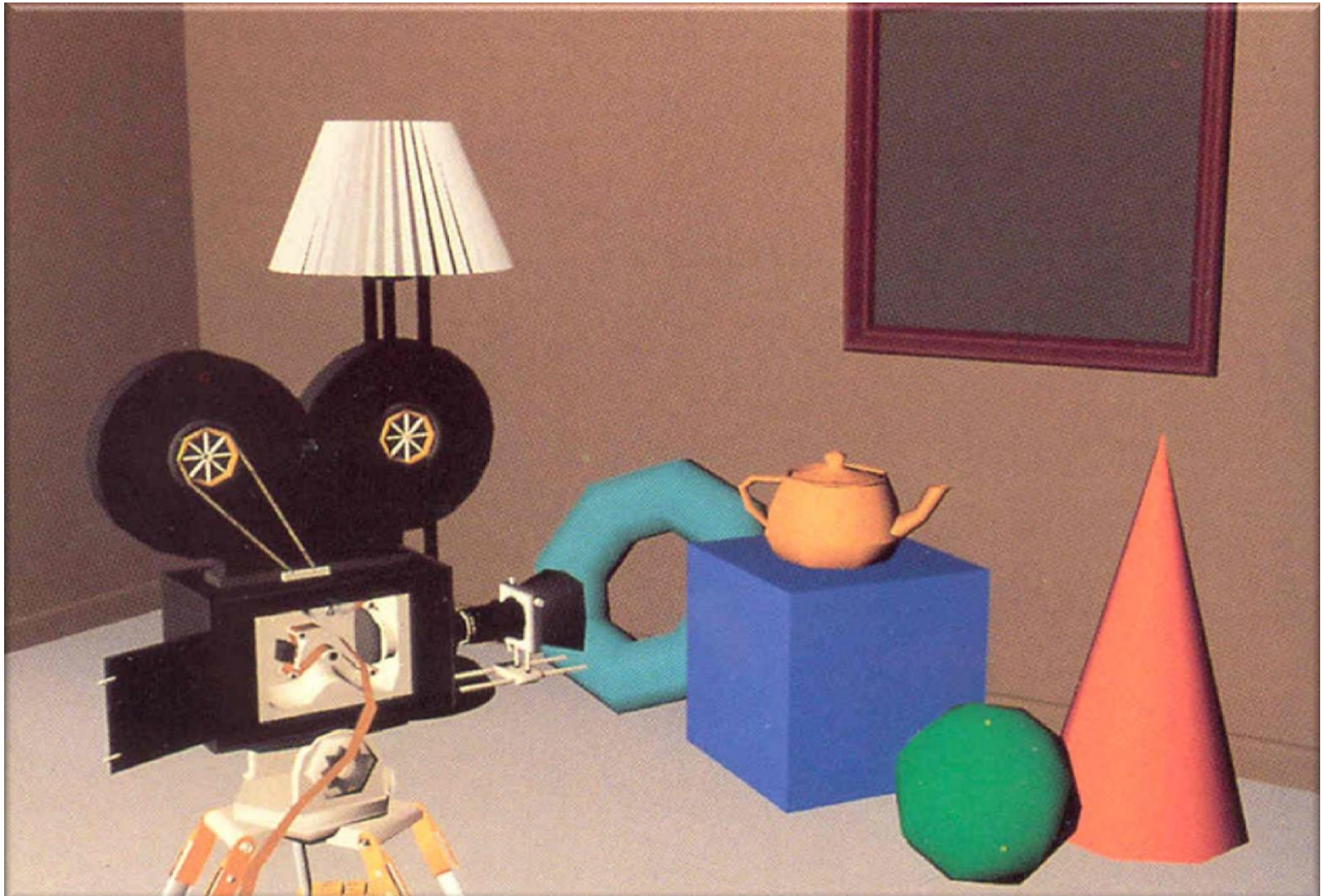


# Example: Flat shading with Diffuse



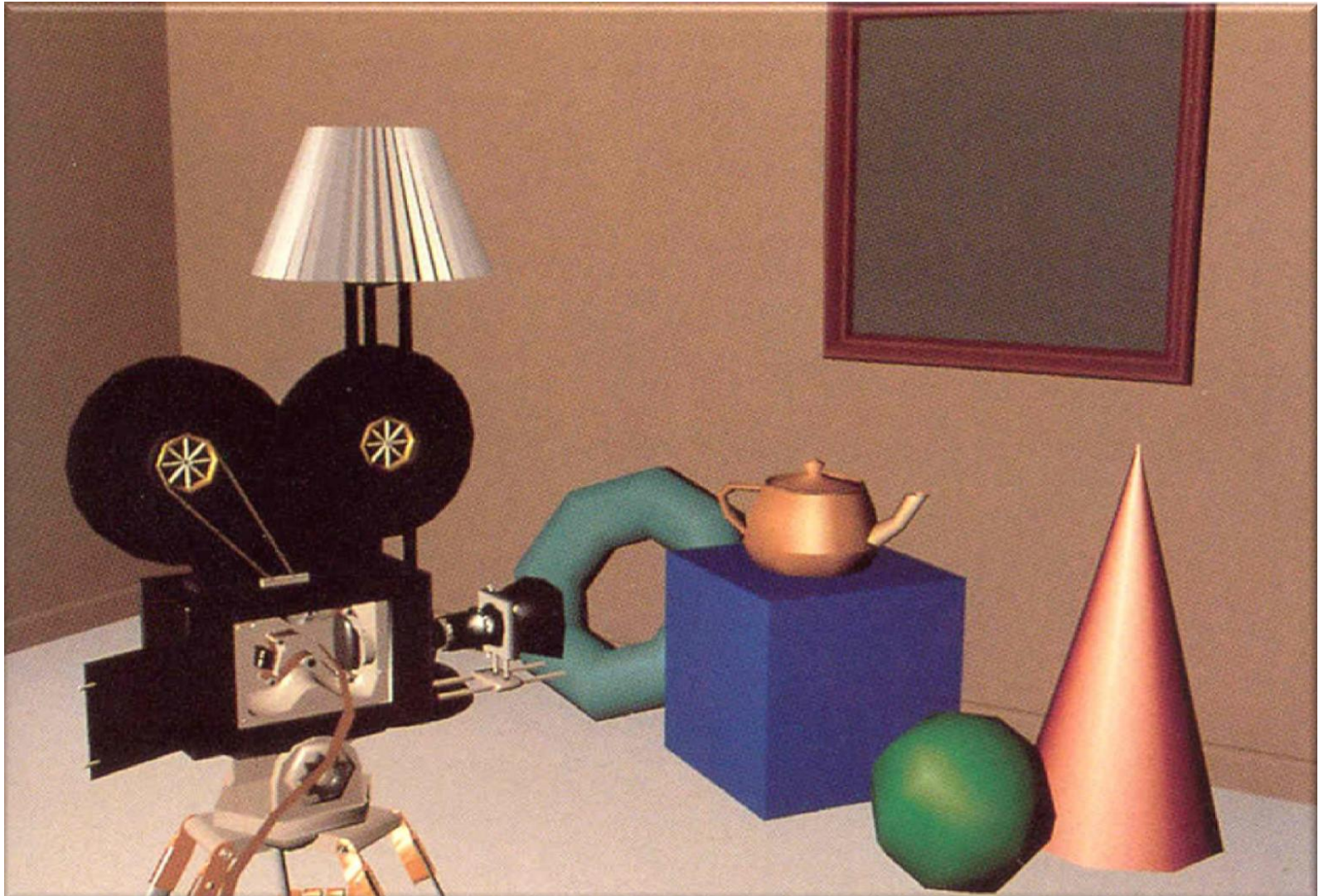


# Example: Gouraud shading with Diffuse



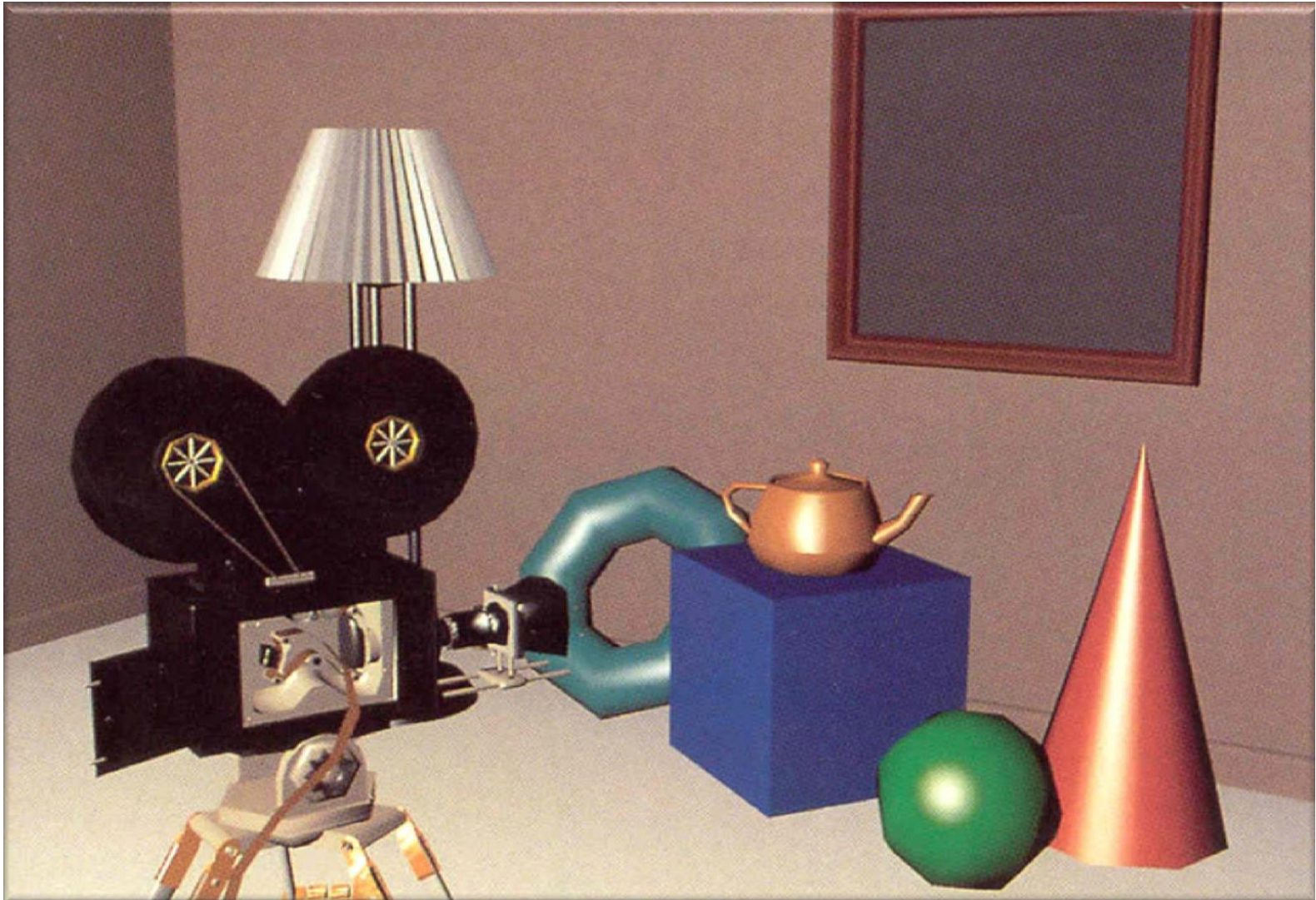


# Example: Gouraud shading with Specular





# Example: Phong shading with Specular





# Shading Issues

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- ▶ Problems with interpolated shading
  - ▶ Problems computing shared vertex normals
  - ▶ Perspective distortion
  - ▶ Problems at T-vertices



# Shading Benefits

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- ▶ **Good performance and quality of output**
  - ▶ Excellent for hardware
  - ▶ Works well with subdivision surfaces

# How the lectures should look like #2

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- Ask questions, please!!!
- Be communicative
- More active you are, the better for you!

# Overview

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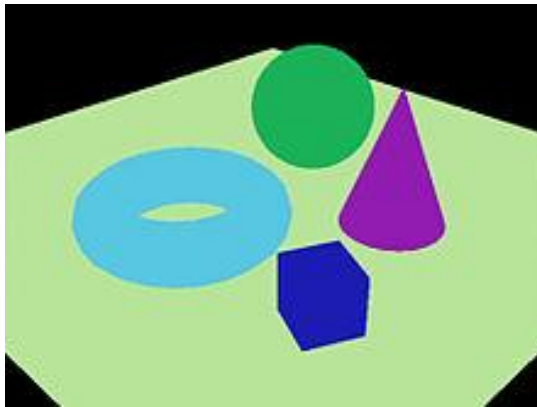
- ▶ Advanced Shading and Mapping
  - ▶ Deferred Shading

# Deferred Shading

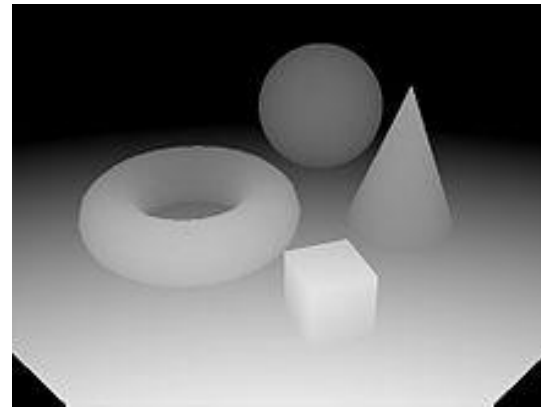
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- ▶ Compute Lighting in Screen-Space
- ▶ Two pass approach
- ▶ Decoupling of geometry and lighting
- ▶ G-Buffer stores positions, normals, materials ...
- ▶ Lighting is a per-pixel operation
- ▶ Problems with transparency and G-buffer size
- ▶  $O(\text{objects} + \text{lights})$

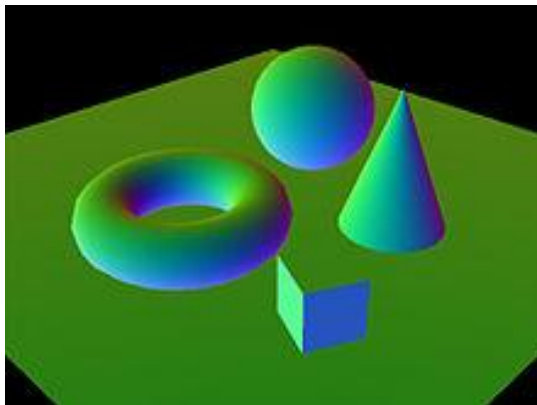
# Deferred Shading



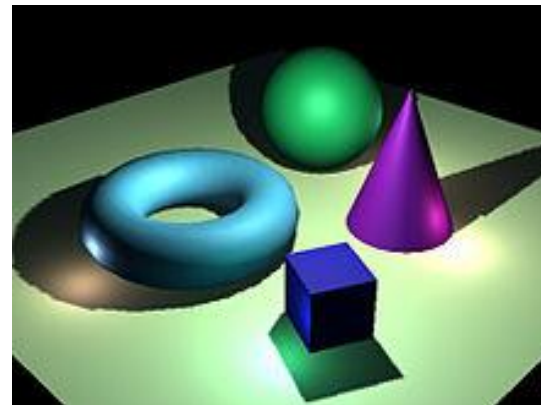
Diffuse Color



Z Buffer



Surface Normals

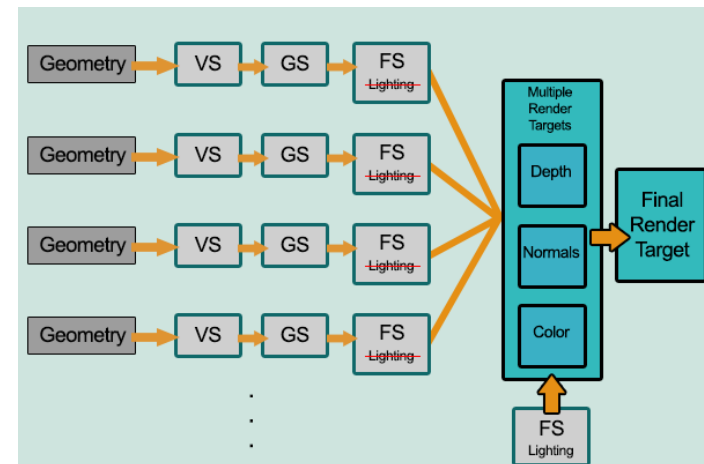
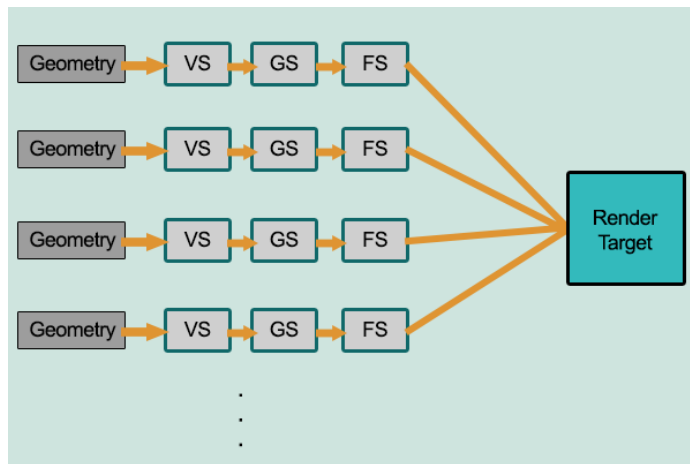


Final Composition

# Deferred Shading

## Forward rendering

$$O(\text{num\_geometry\_fragments} * \text{num\_lights})$$



<https://gamedevelopment.tutsplus.com/articles/forward-rendering-vs-deferred-rendering--gamedev-12342>

## Deferred shading

$$O(\text{screen\_resolution} * \text{num\_lights})$$

# Deferred Shading Pros/Cons

---

## ► Pros

- The primary advantage of deferred rendering is that the lighting is only computed for fragments that are visible
- In forward rendering, each fragment requires a loop over all light sources and for each, an evaluation of the lighting model
- Deferred rendering provides better scalability as the number of light sources increases.

## ► Cons

- The primary disadvantage of deferred rendering is the additional storage for the g-buffer
- This becomes a difficulty when different materials are required for different objects in the scene



# Next Lecture

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## Visibility, Culling



# Acknowledgements

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Output of all the publications and great team work



Very best data from 3D cameras



# Questions ?!

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