



**Fundamentals of
Computer Graphics and Image Processing
Visibility, Culling, Clipping (05)**

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Overview

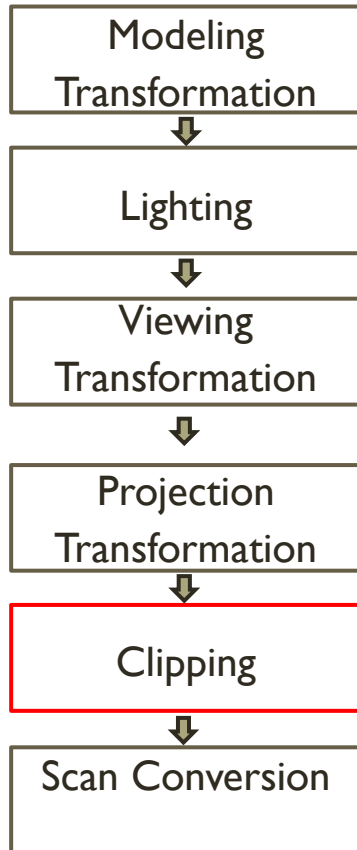
- ▶ **Clipping**

- ▶ Point Clipping
- ▶ Line Clipping
- ▶ Polygon Clipping

- ▶ **Hidden Surface Removal**

3D rendering pipeline

3D polygons



2D Image

Rasterization (05)

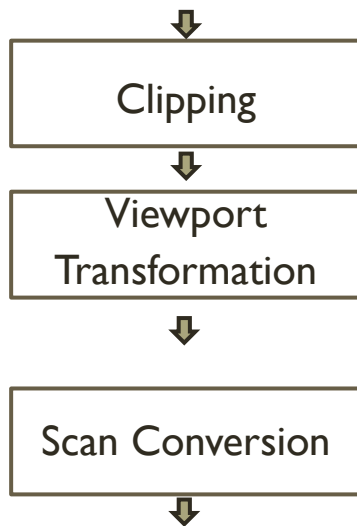
Clip polygons outside of camera's view

How the lectures should look like #1

- Ask questions, please!!!
- Be communicative
- More active you are, the better for you!

2D rendering pipeline

2D geometry

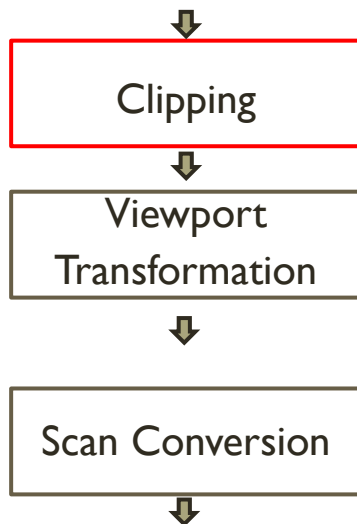


- ▶ Clip and remove geometry outside of the window
- ▶ Transform from screen coordinates to image coordinates
- ▶ Fill pixels on the screen

2D Image

2D rendering pipeline

2D geometry



- ▶ Clip and remove geometry outside of the window
- ▶ Transform from screen coordinates to image coordinates
- ▶ Fill pixels on the screen

2D Image

Clipping

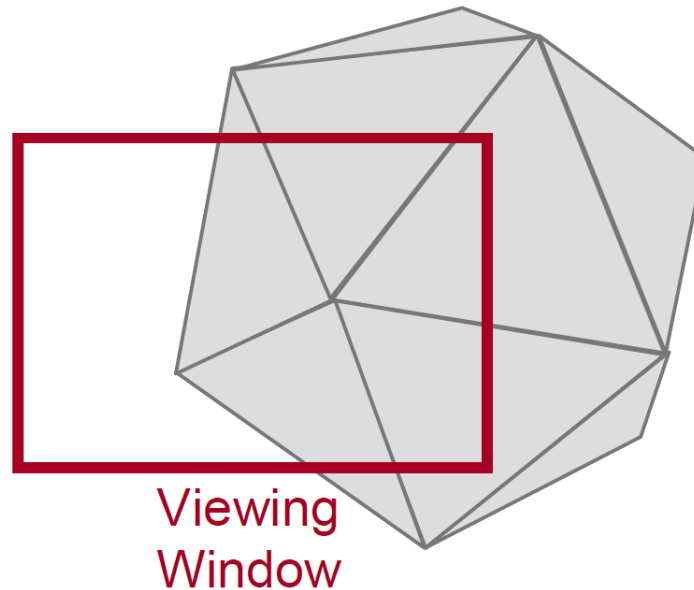
- ▶ Avoid drawing parts of primitives outside window
 - ▶ Window defines part of scene being viewed
 - ▶ Must draw geometric primitives only inside window



Screen Coordinates

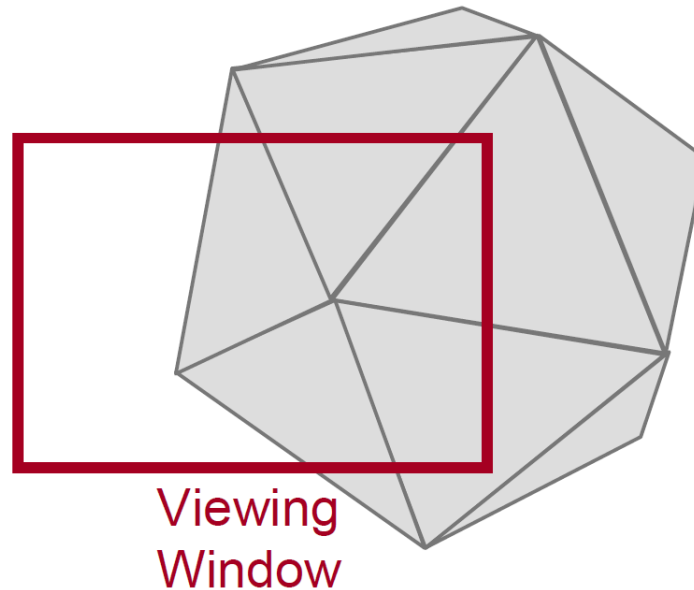
Clipping

- ▶ Avoid drawing parts of primitives outside window
 - ▶ Window defines part of scene being viewed
 - ▶ Must draw geometric primitives only inside window



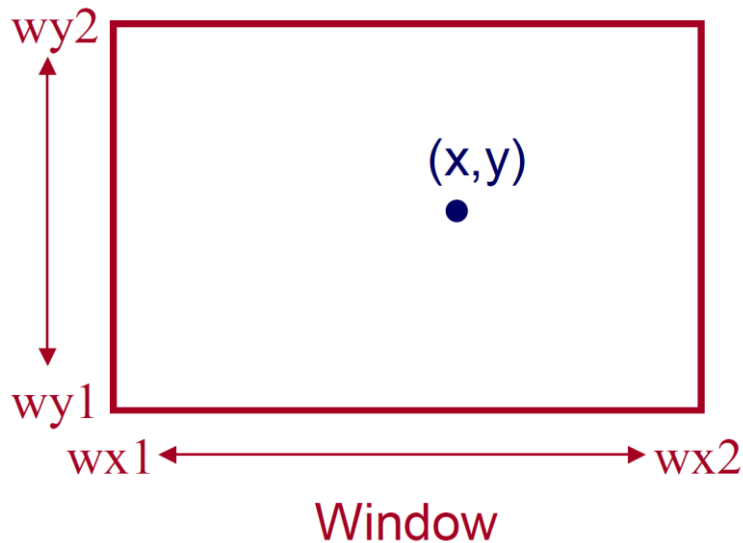
Clipping

- ▶ Avoid drawing parts of primitives outside window
 - ▶ Points, Lines, Polygons, Circles etc.



Point Clipping

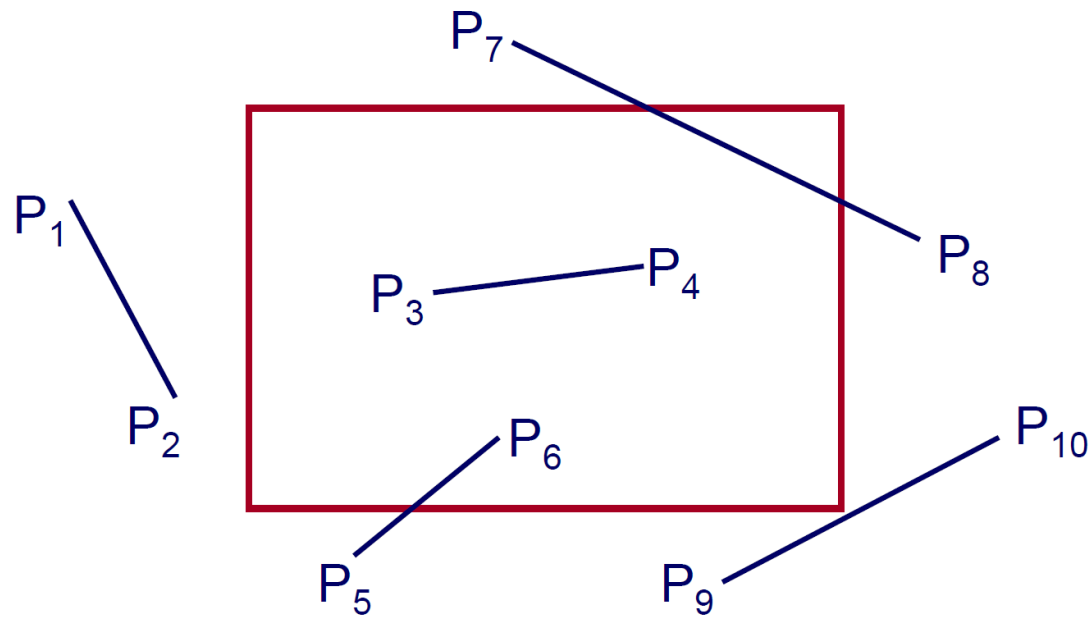
- Is point (x,y) inside clip window ?



```
inside =  
    (x >= wx1) &&  
    (x <= wx2) &&  
    (y >= wy1) &&  
    (y <= wy2) ;
```

Line Clipping

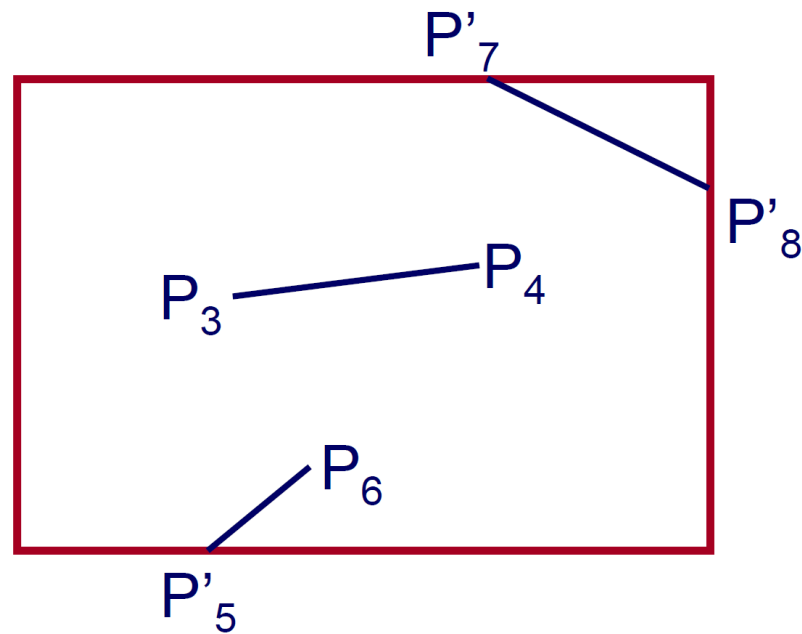
- Find the part of a line inside the clip window



Before Clipping

Line Clipping

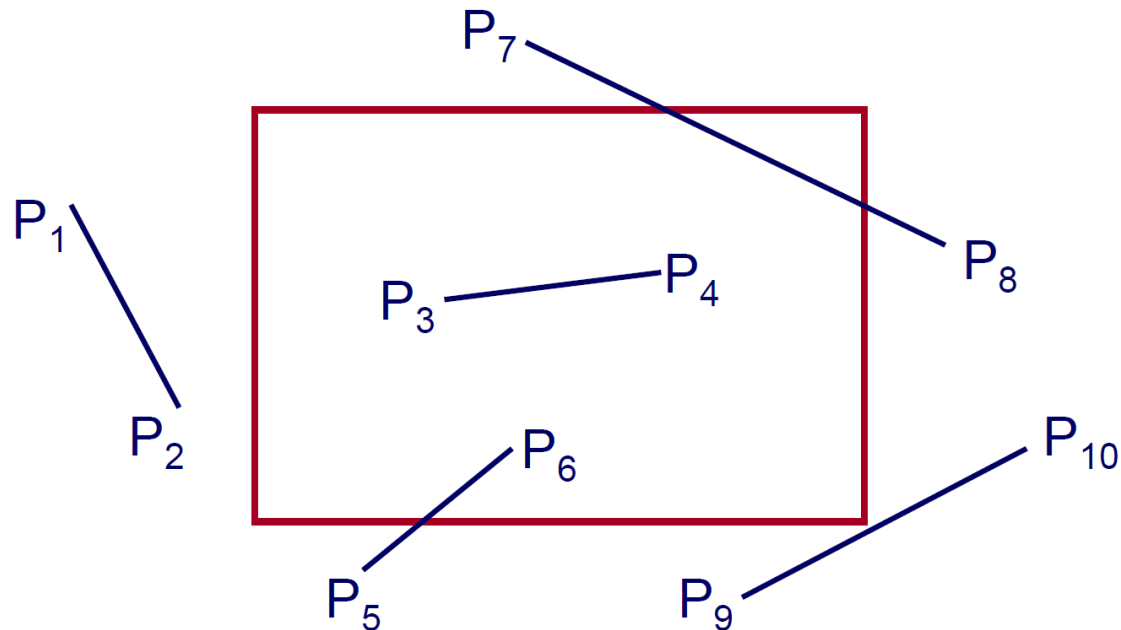
- Find the part of a line inside the clip window



After Clipping

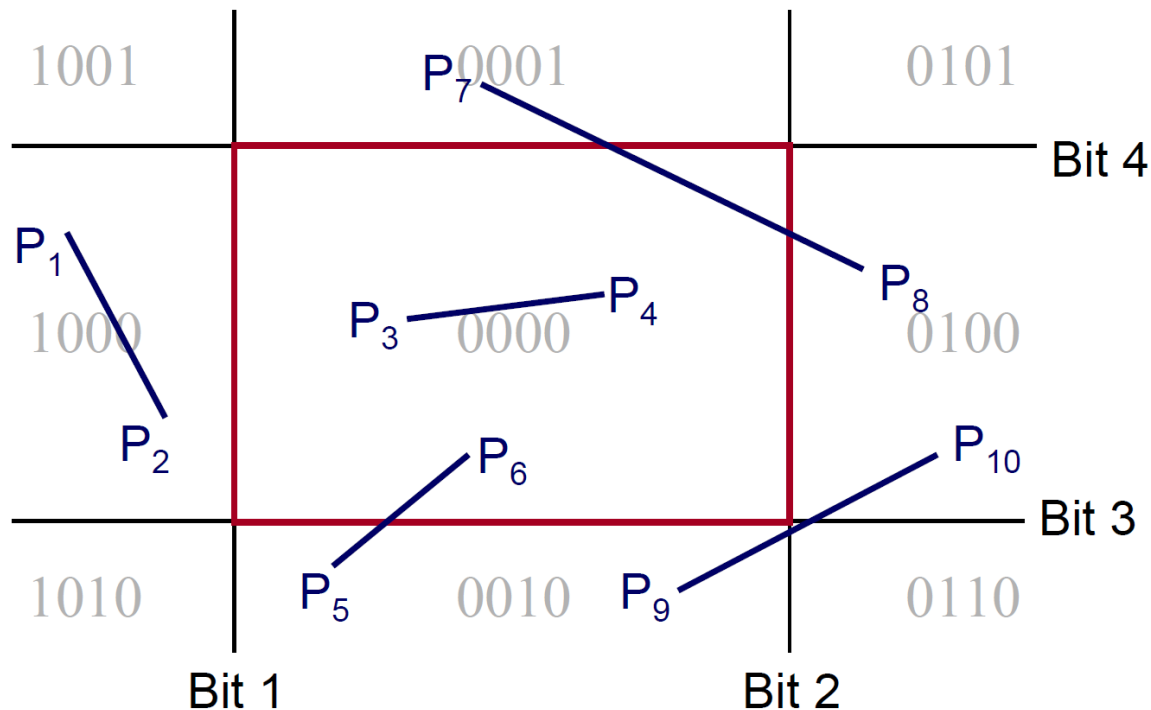
Cohen-Sutherland Line Clipping

- ▶ Use simple test to classify easy cases first
- ▶ Danny Cohen, Ivan Sutherland 1967



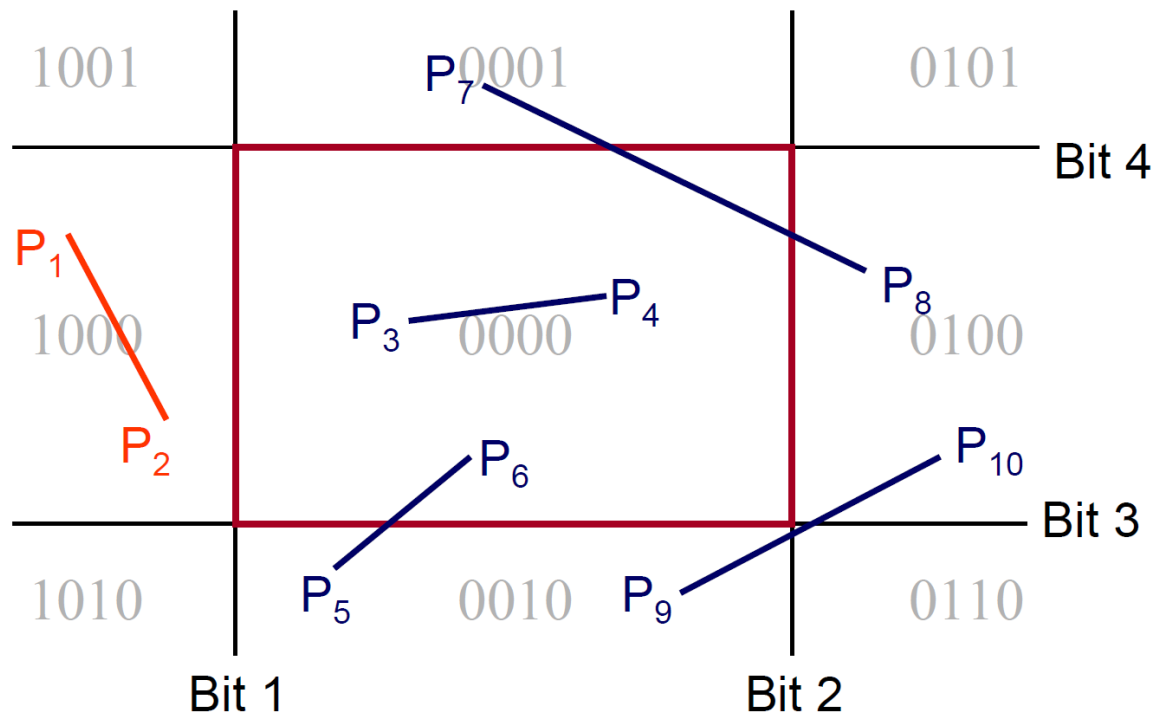
Cohen-Shutherland Line Clipping

- Classify lines quickly by AND of bit codes representing regions of two endpoints (test for 0: inside or clipping, 1: outside)



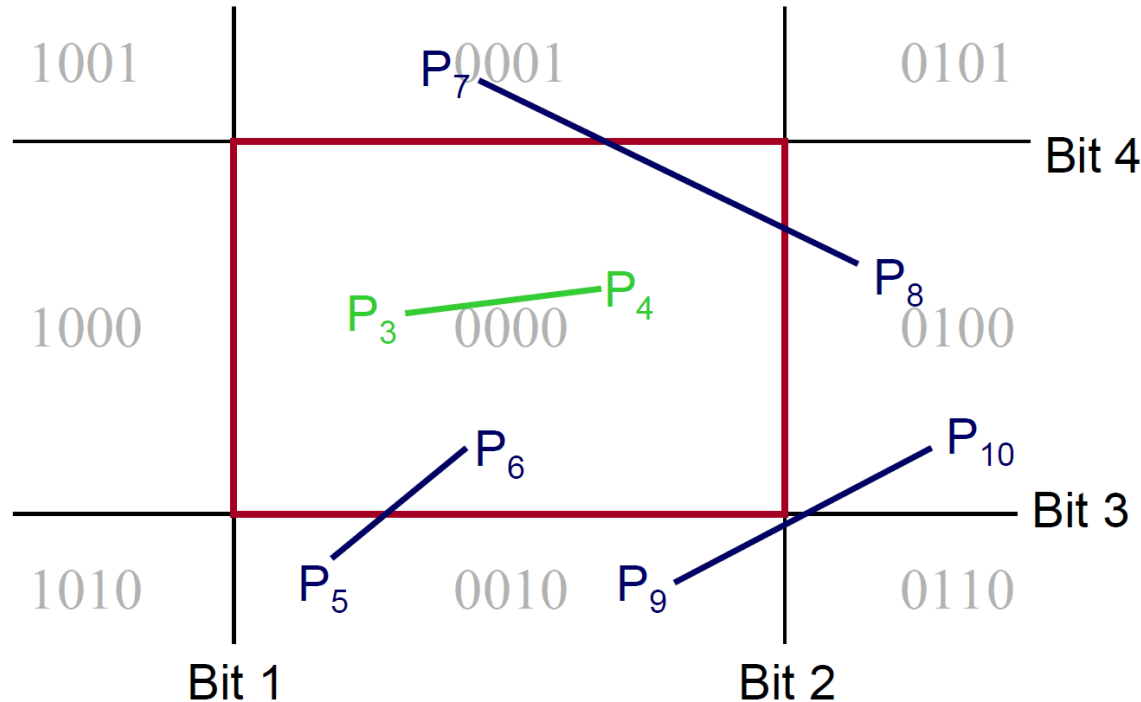
Cohen-Shutherland Line Clipping

- Classify lines quickly by AND of bit codes representing regions of two endpoints (test for 0: inside or clipping, 1: outside)



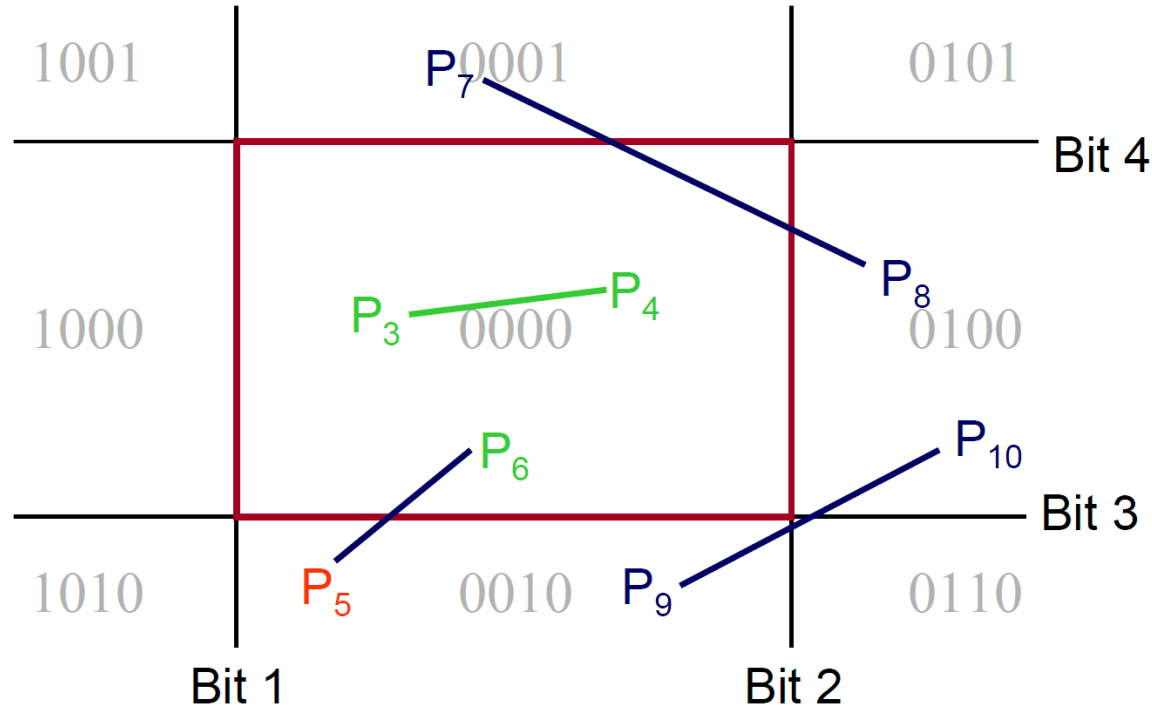
Cohen-Shutherland Line Clipping

- Classify possible clipping lines by OR of bit codes representing regions of two endpoints (test for 0: inside)



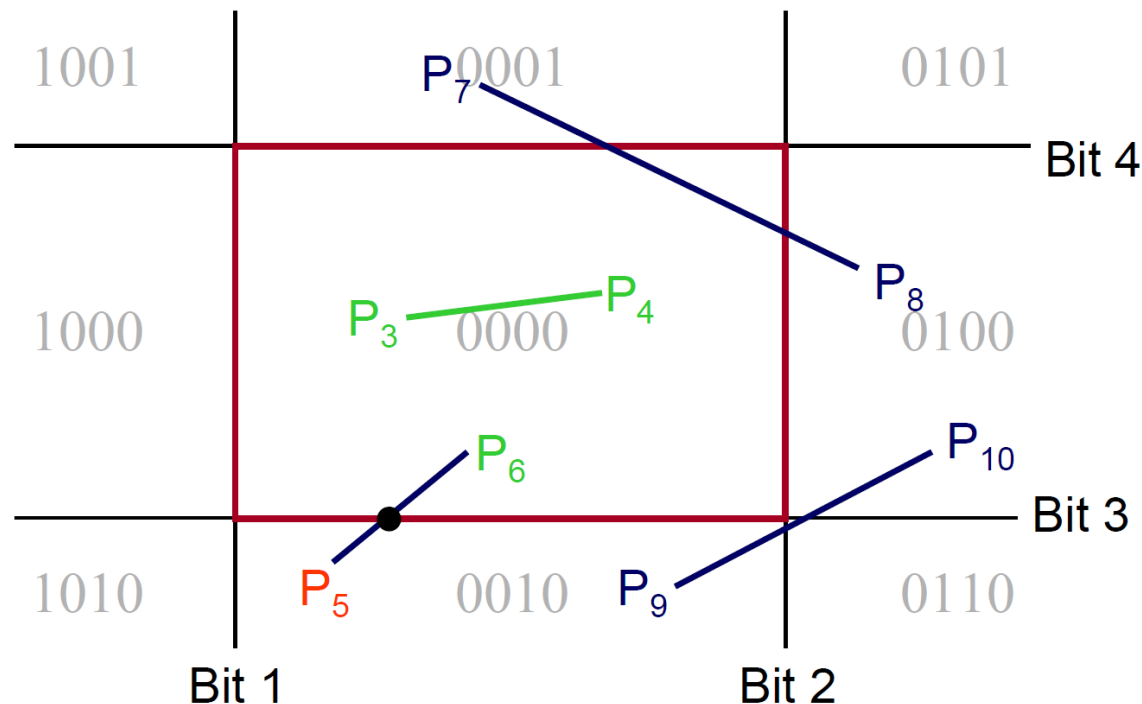
Cohen-Shutherland Line Clipping

- Compute intersections with window boundary for remaining lines, OR of bit codes representing the boundary



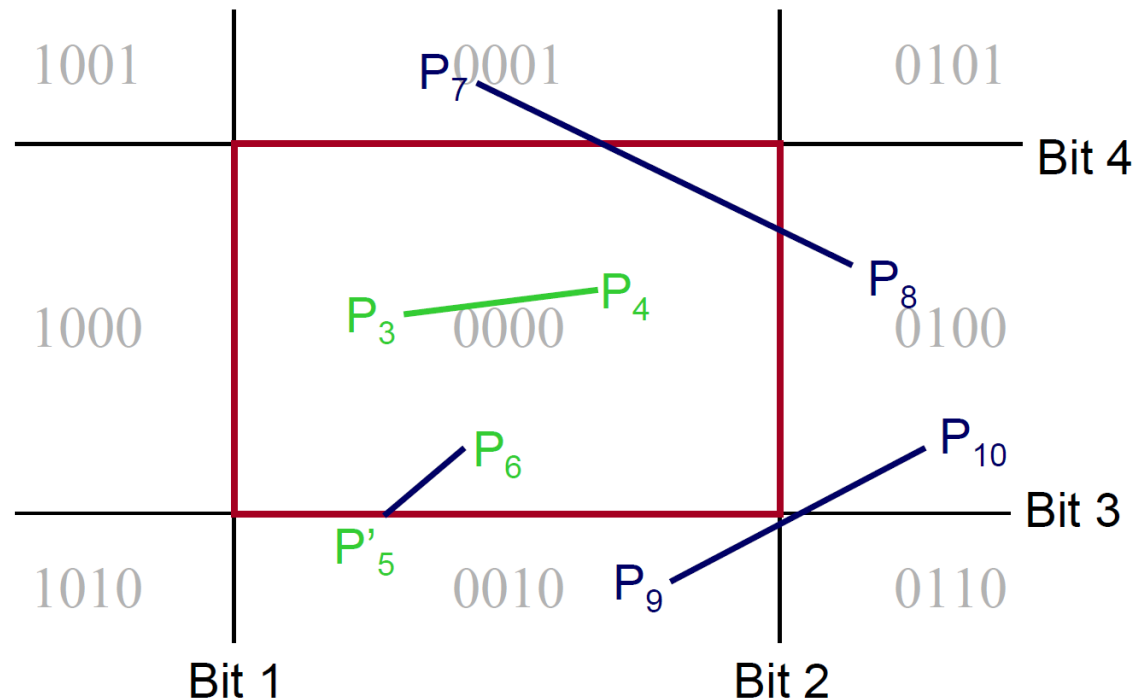
Cohen-Shutherland Line Clipping

- Intersect with boundary determined by the bits of the non zero point and set 0000 for the new point



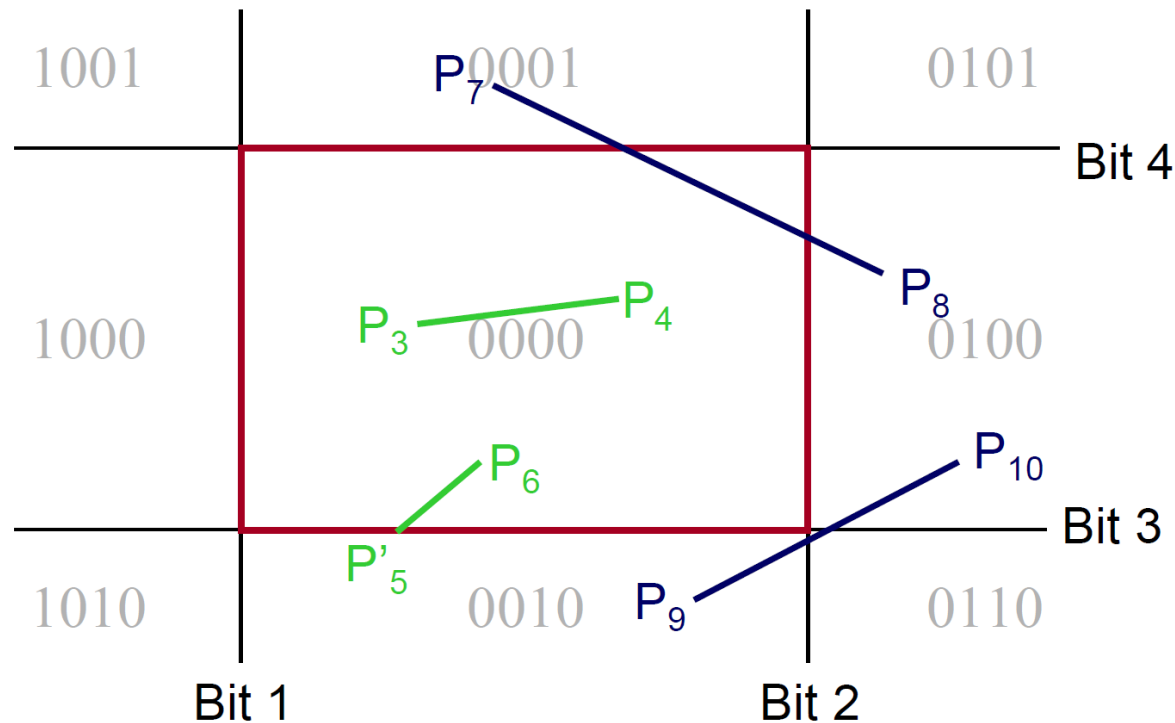
Cohen-Shutherland Line Clipping

- Create new point on the boundary



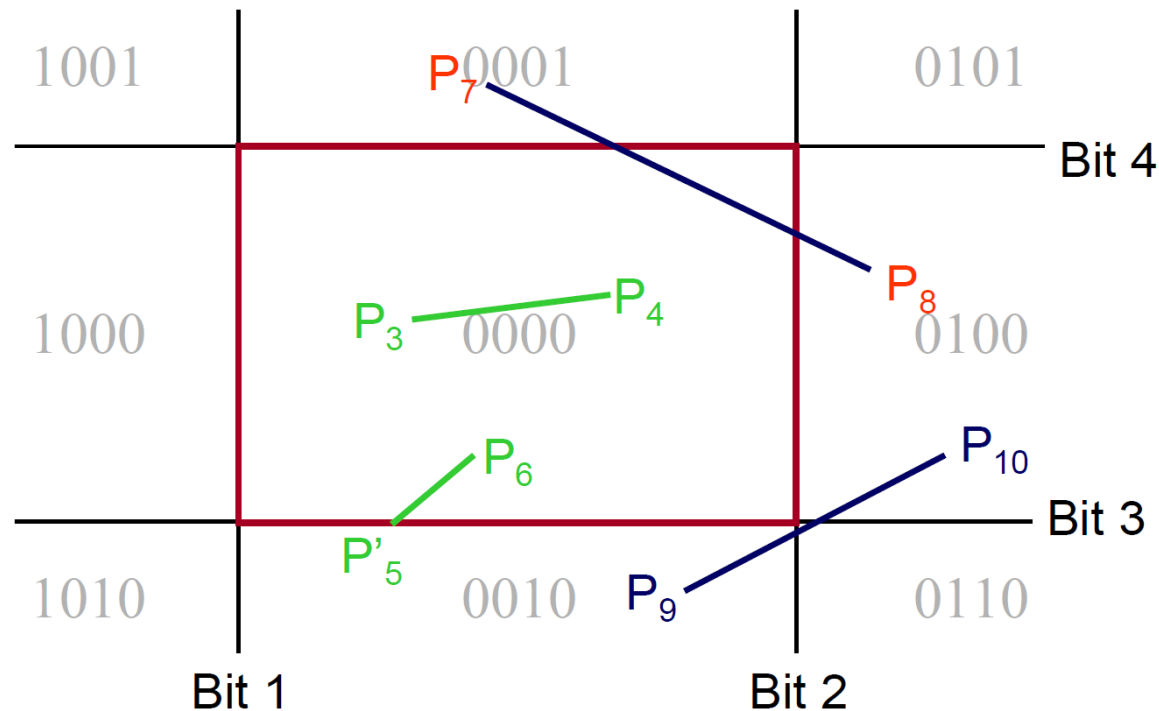
Cohen-Shutherland Line Clipping

- Check using the AND operation again



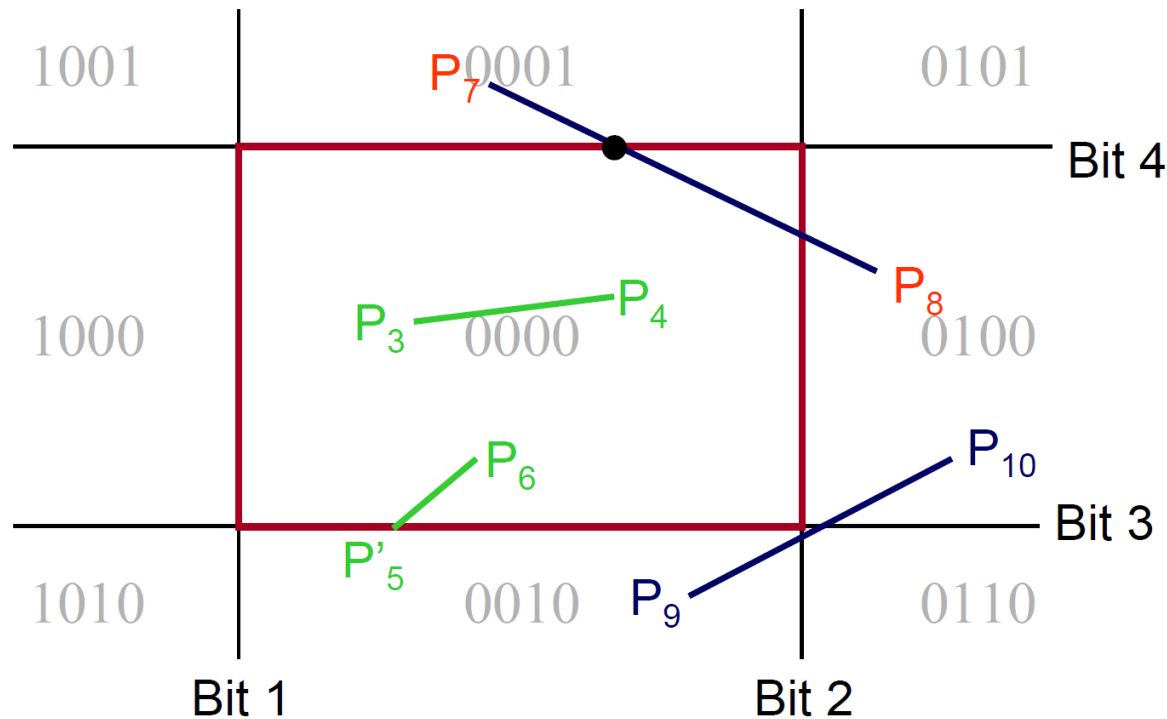
Cohen-Shutherland Line Clipping

- Do the same for the next line



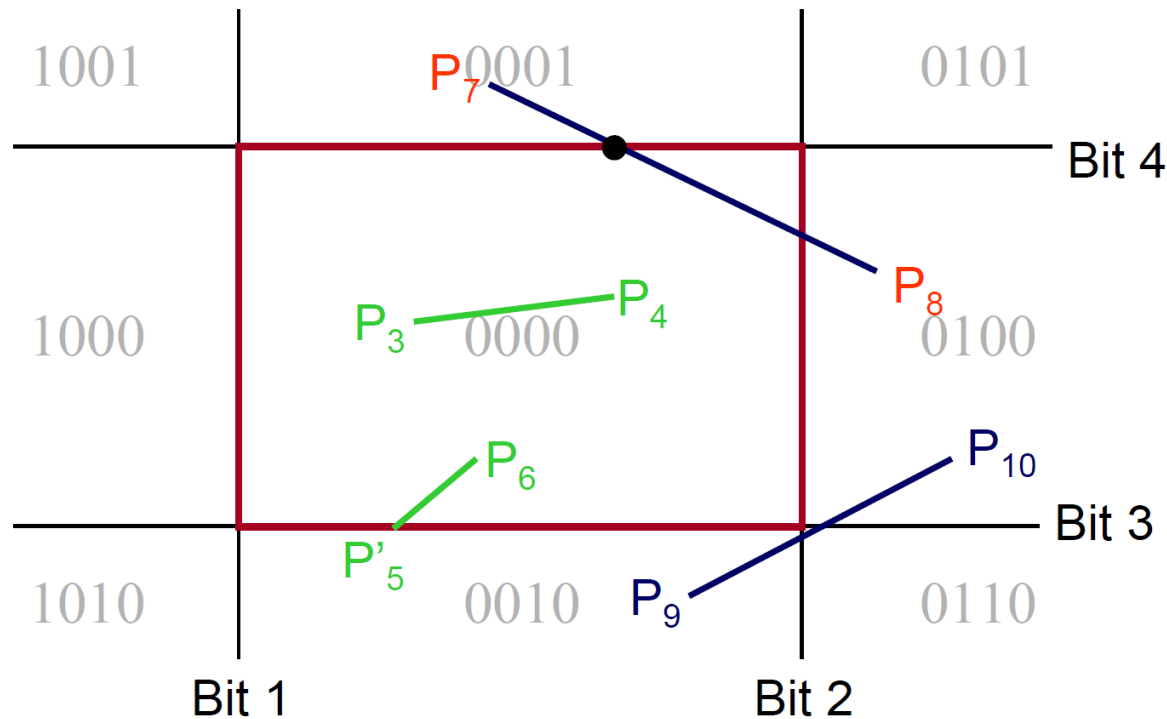
Cohen-Shutherland Line Clipping

- Clip using the boundary determined by P7



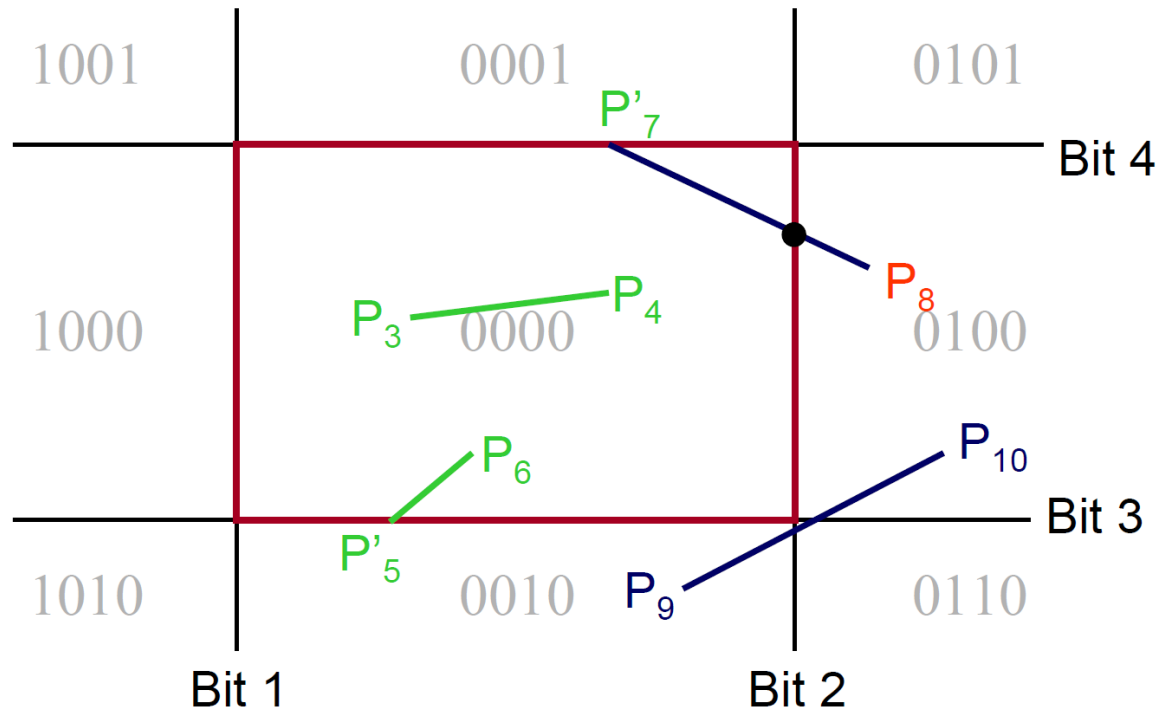
Cohen-Shutherland Line Clipping

- Clip using the boundary determined by P7



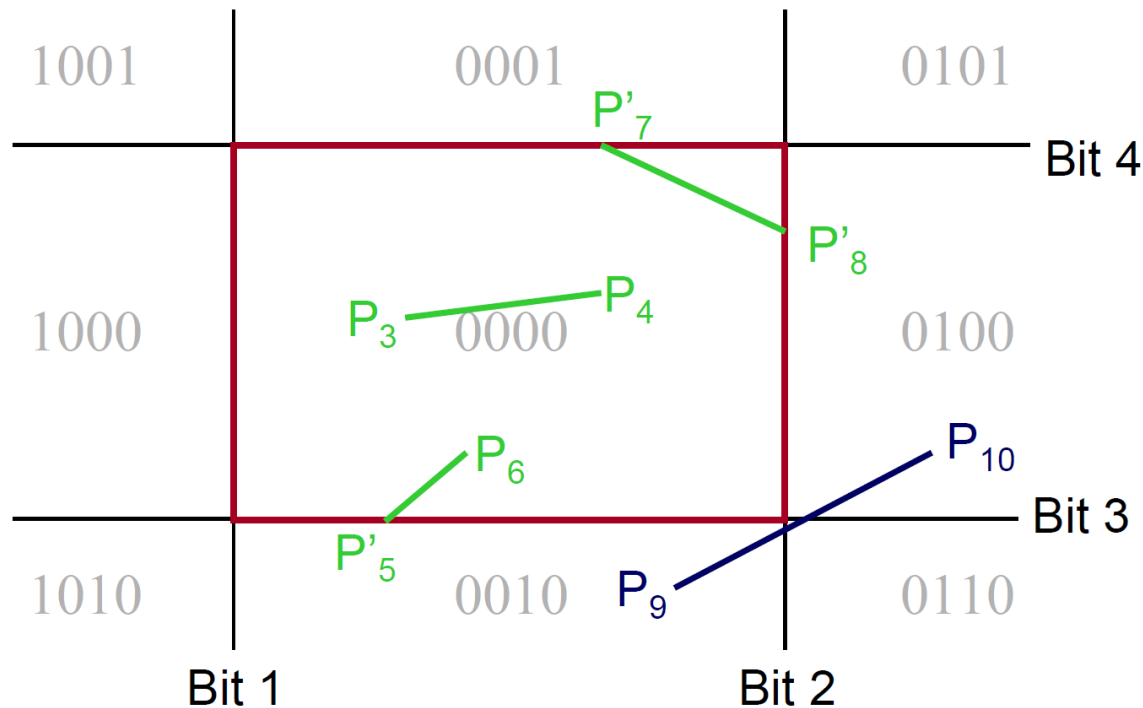
Cohen-Shutherland Line Clipping

- Clip using the boundary determined by P8



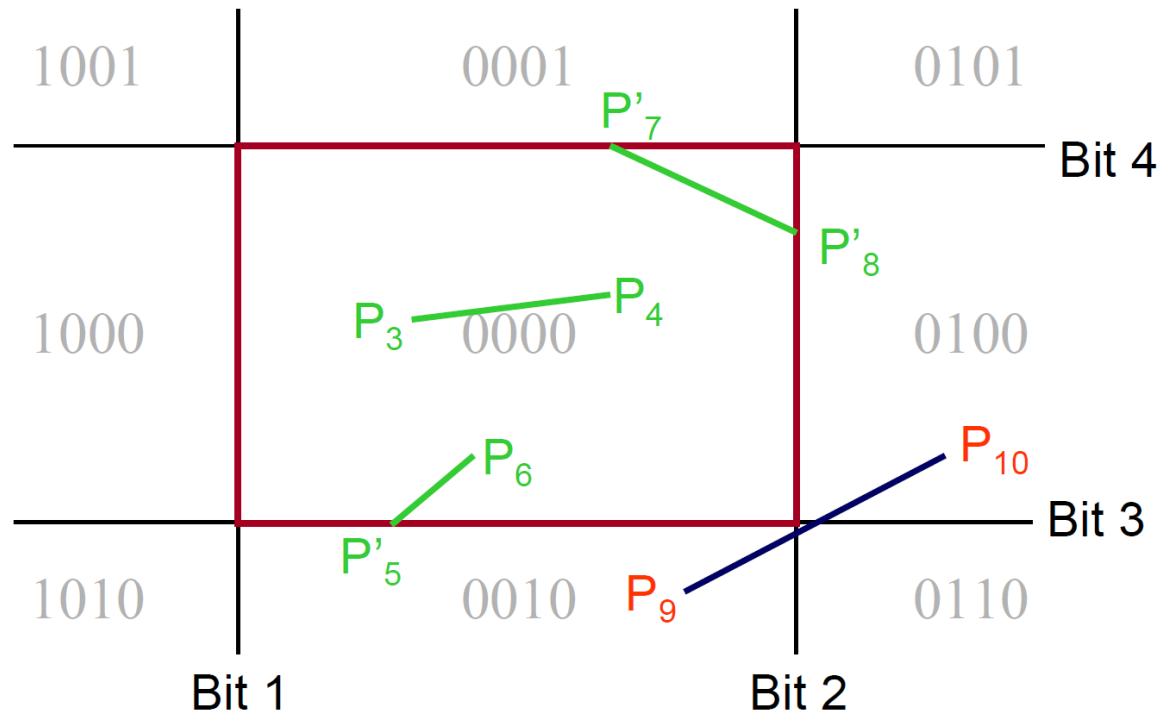
Cohen-Shutherland Line Clipping

- Test the line again using AND



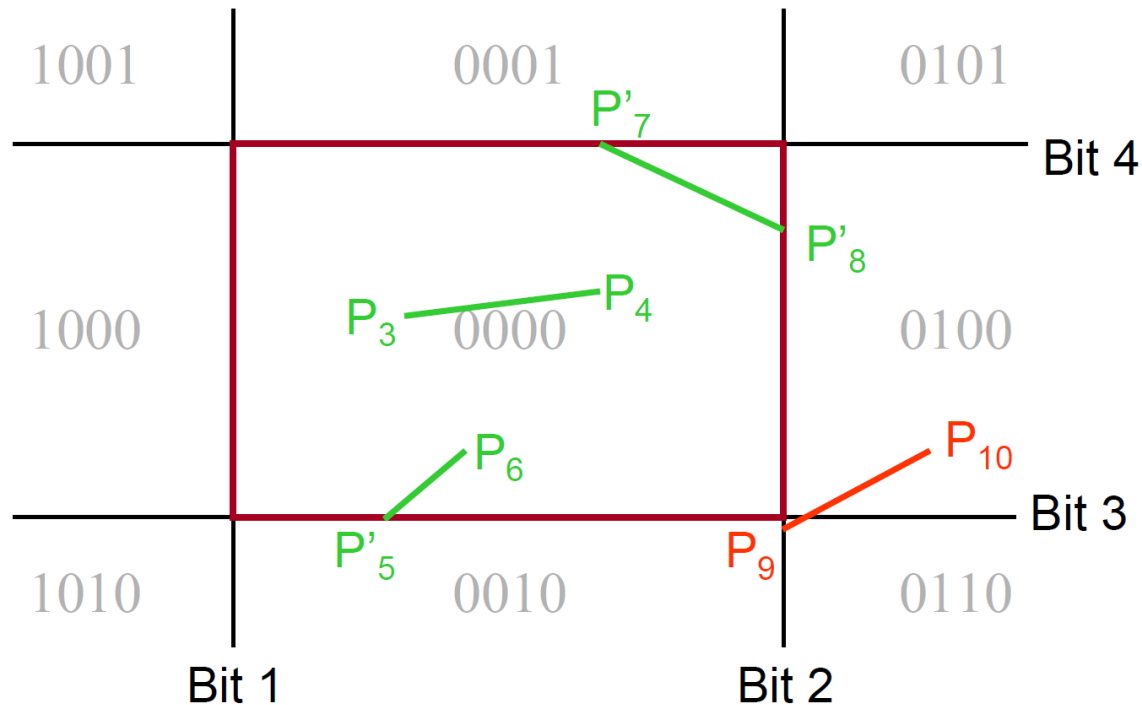
Cohen-Shutherland Line Clipping

- Again for the last line



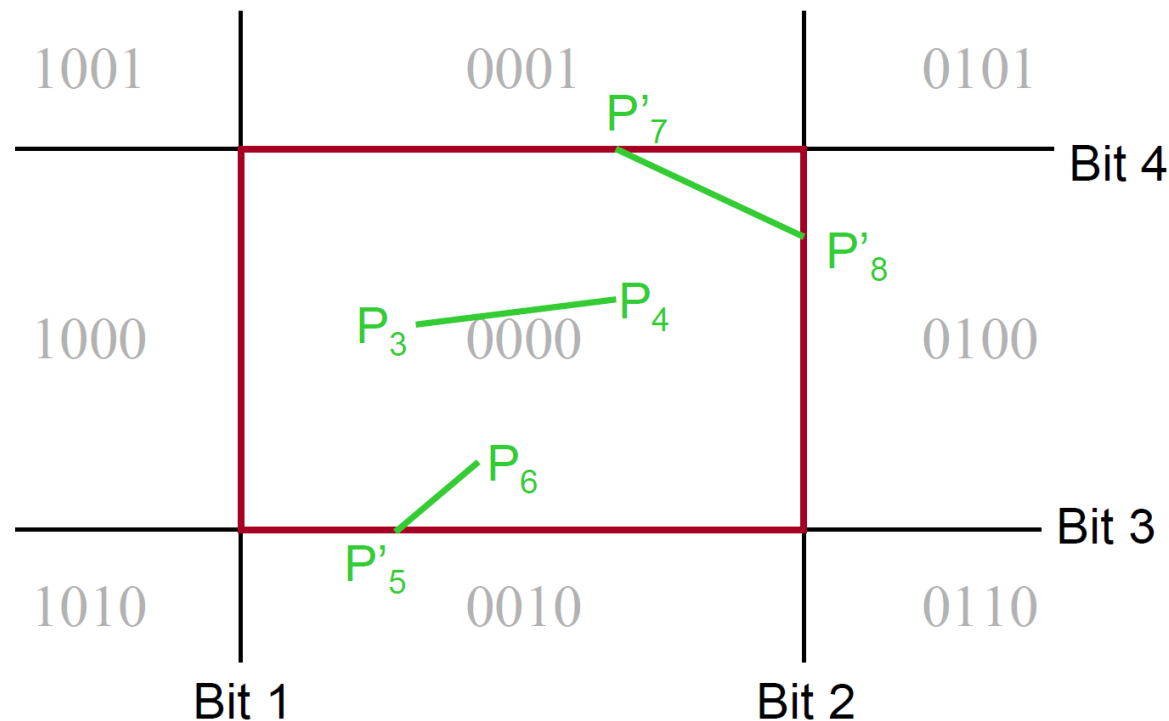
Cohen-Shutherland Line Clipping

- P9 AND P10 no longer zero



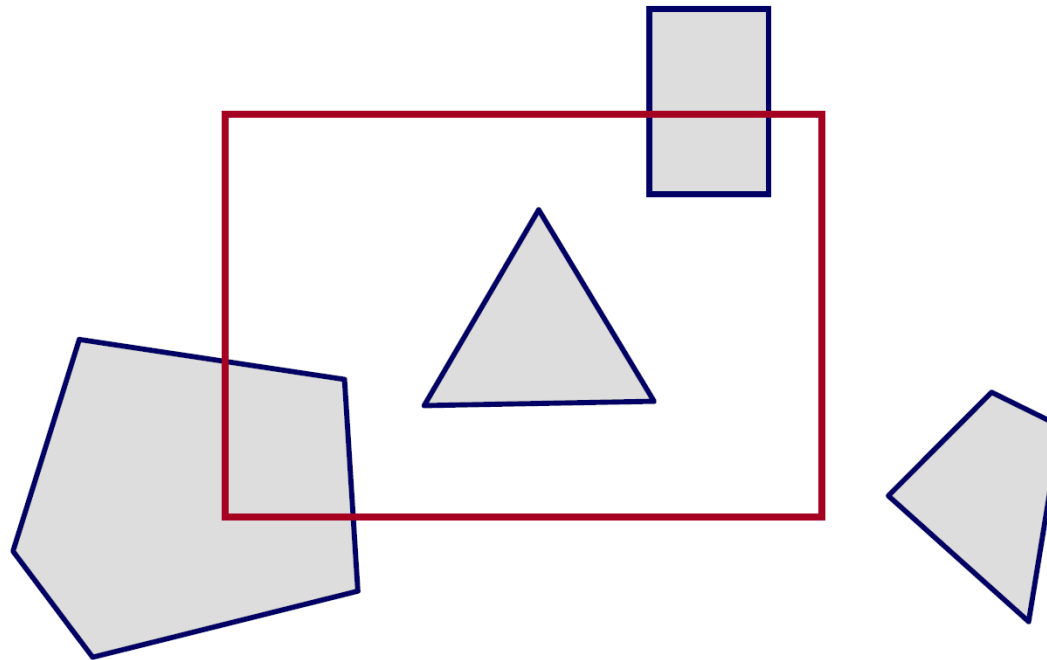
Cohen-Shutherland Line Clipping

► Final result



Polygon Clipping

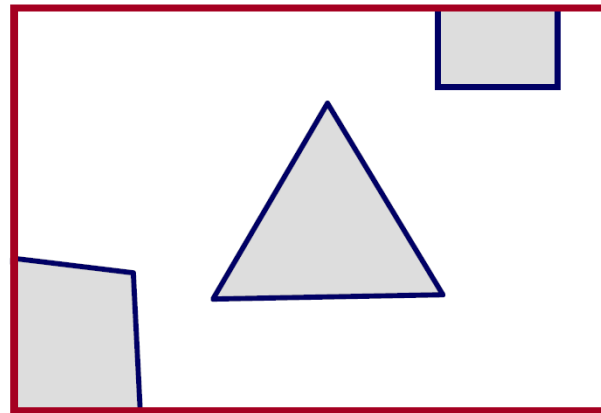
- Find the part of a polygon inside the clip window?



Before Clipping

Polygon Clipping

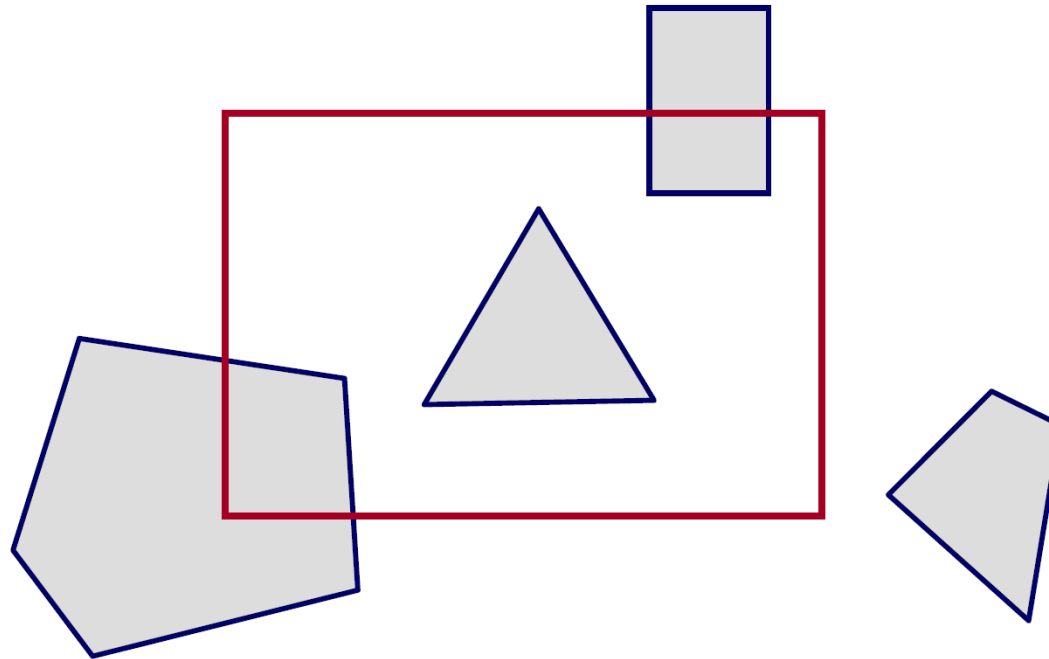
- Find the part of a polygon inside the clip window?



After Clipping

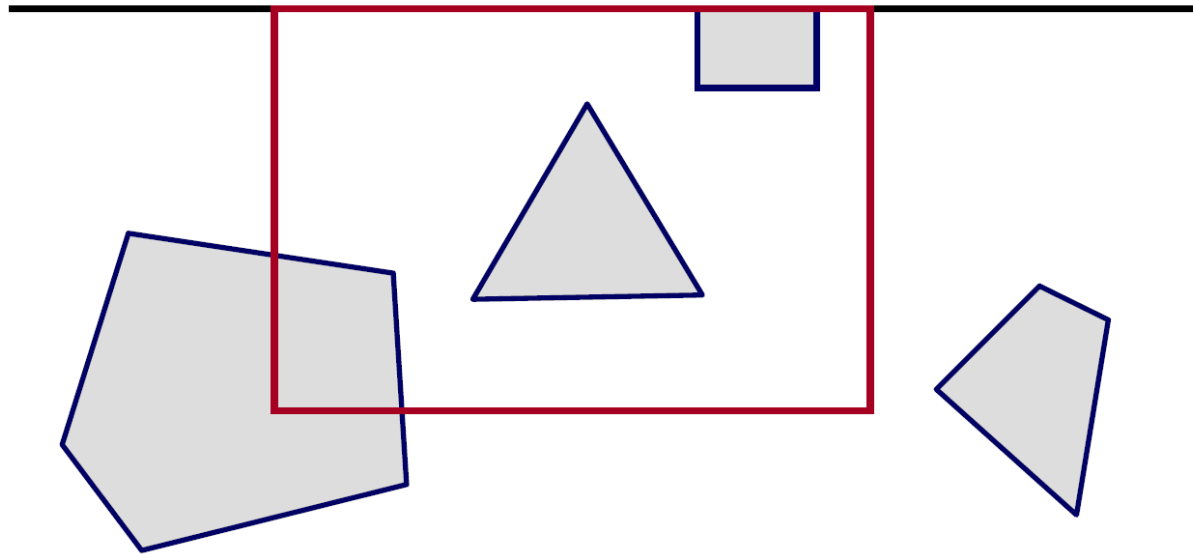
Sutherland–Hodgman Clipping

- Clip to each window boundary one at a time



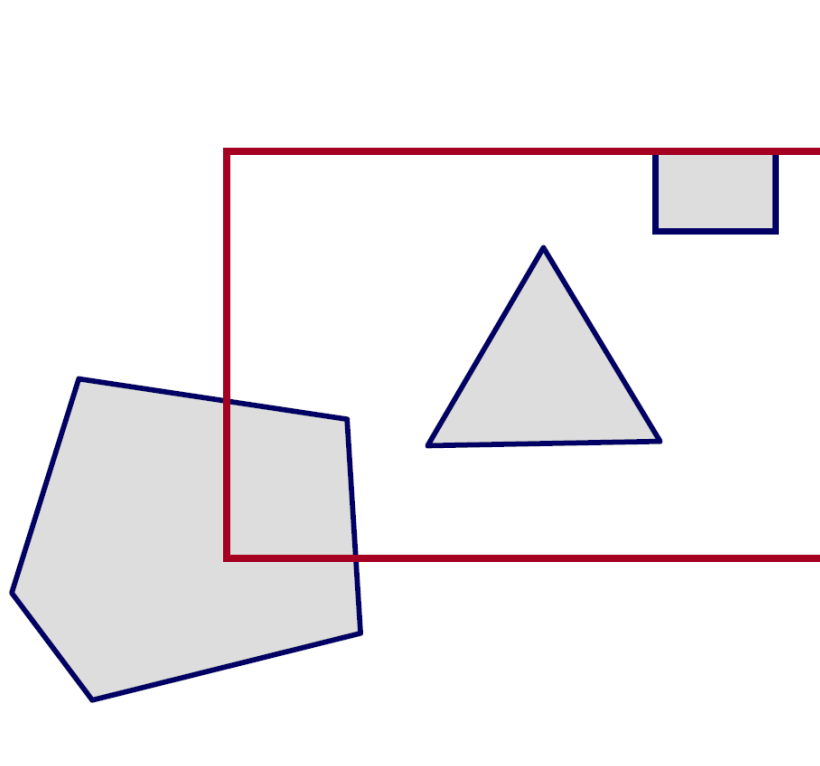
Sutherland–Hodgman Clipping

- Clip to each window boundary one at a time



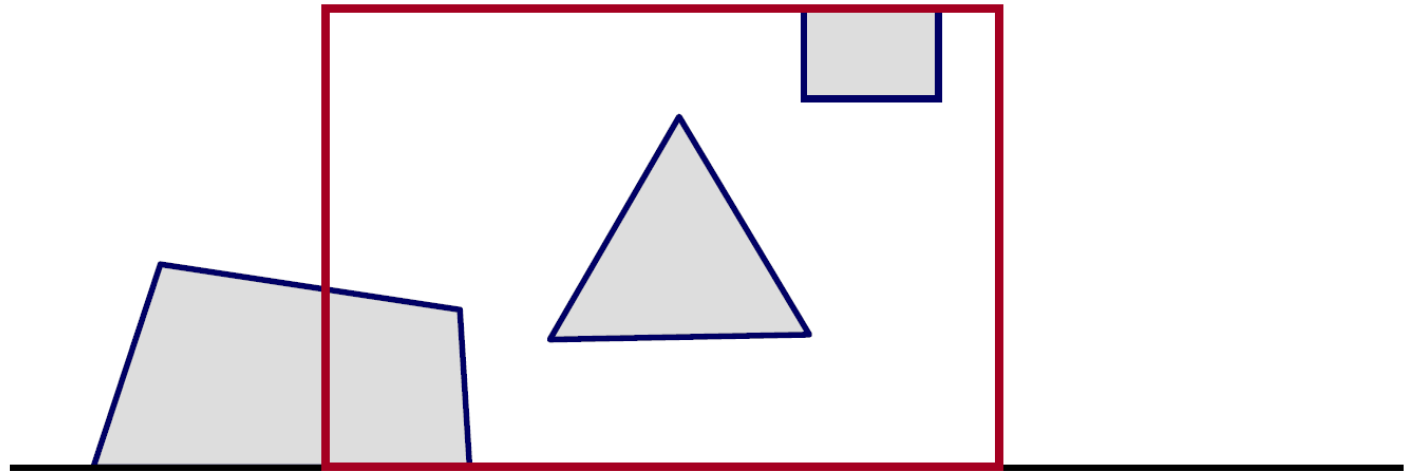
Sutherland–Hodgman Clipping

- Clip to each window boundary one at a time



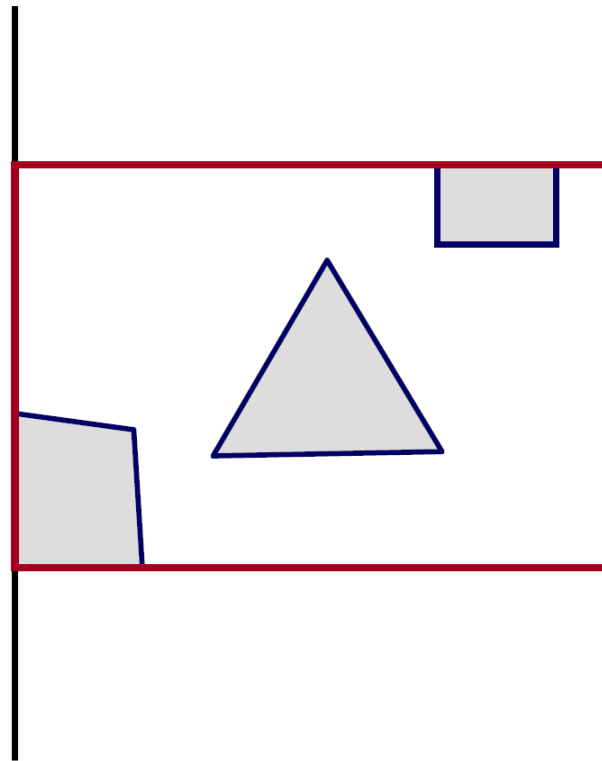
Sutherland–Hodgman Clipping

- Clip to each window boundary one at a time



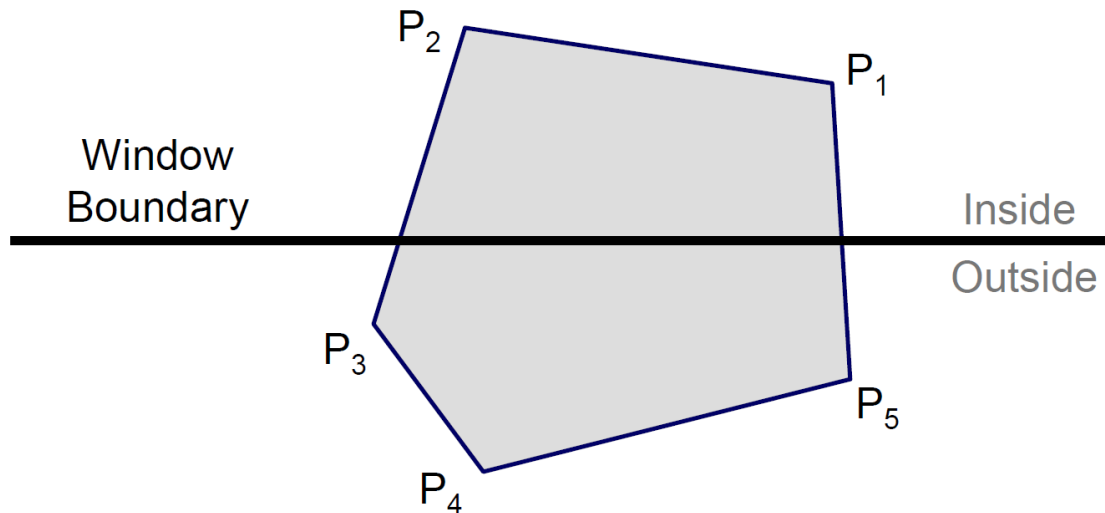
Sutherland–Hodgman Clipping

- Clip to each window boundary one at a time



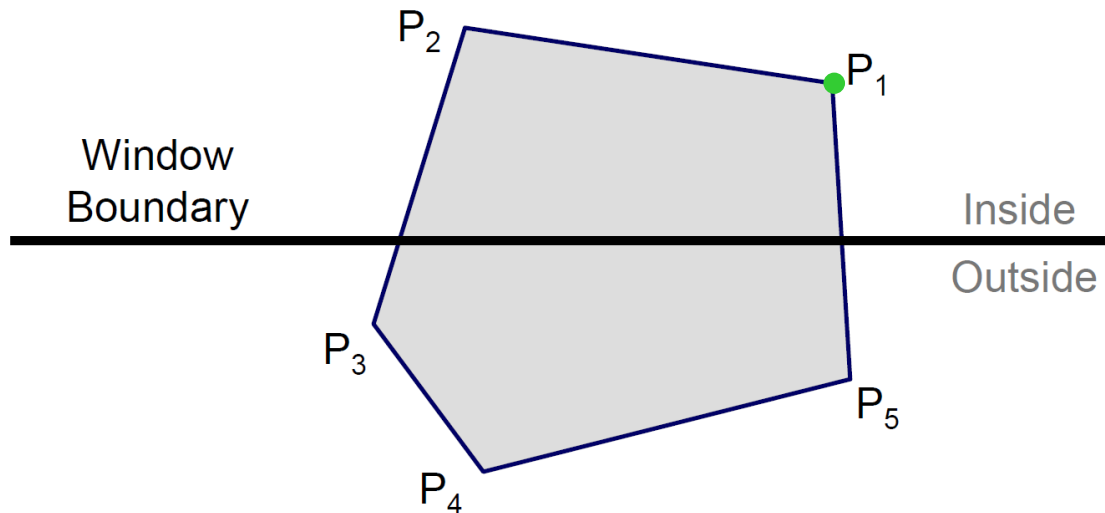
Clipping to a Boundary

- ▶ Do inside test for each point in sequence
- ▶ Insert new points when crossing the boundary
- ▶ Remove points outside of boundary



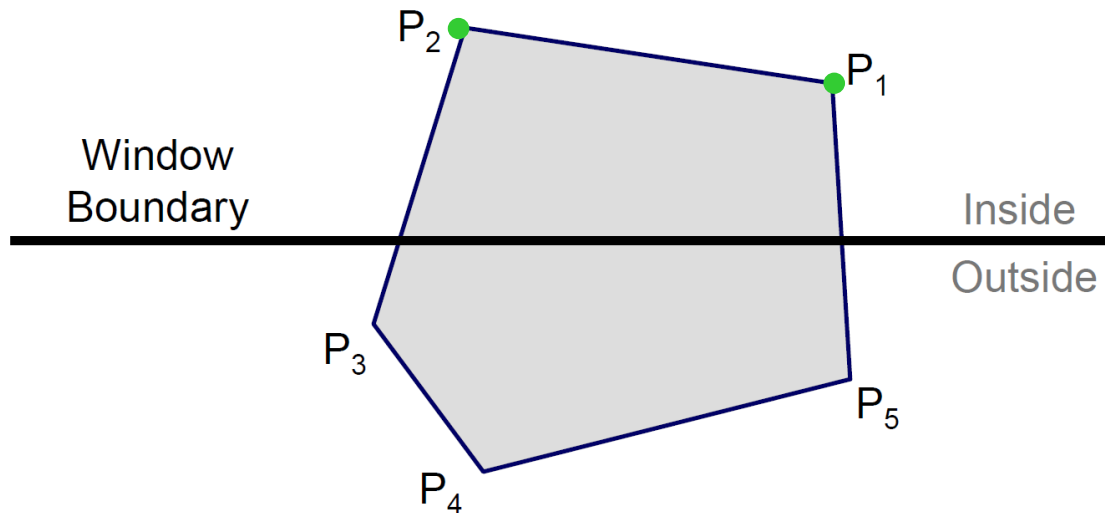
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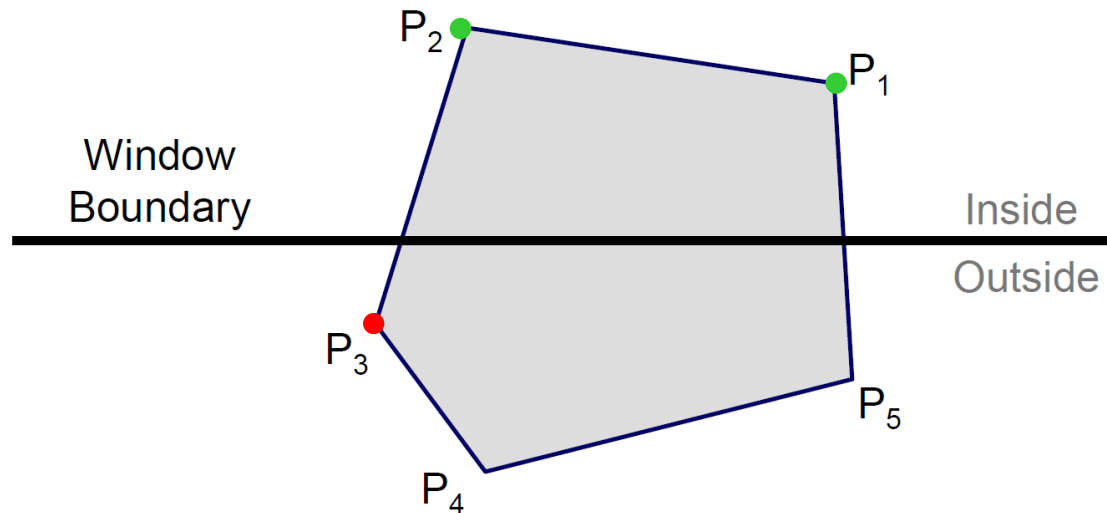
Clipping to a Boundary

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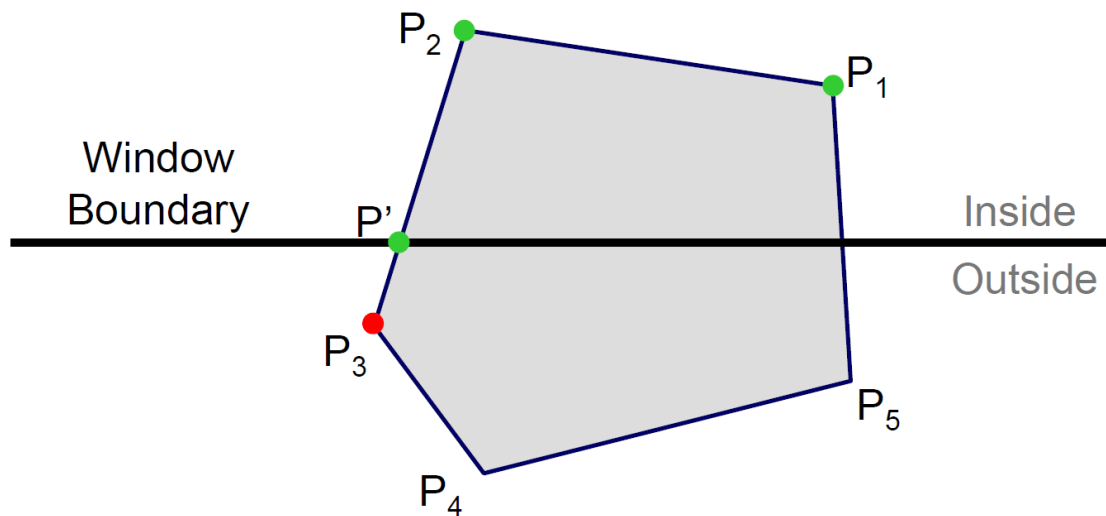
Clipping to a Boundary

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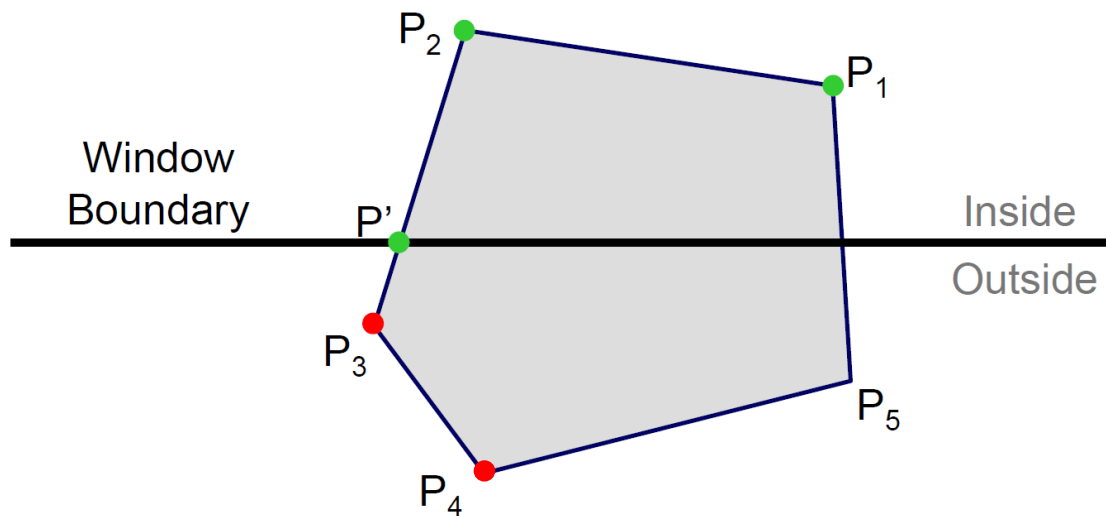
Clipping to a Boundary

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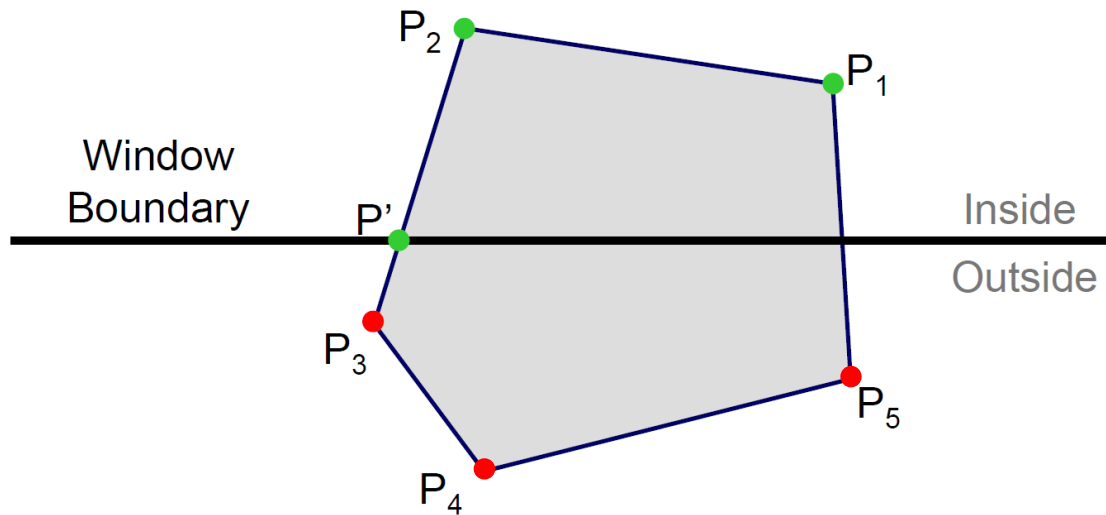
Clipping to a Boundary

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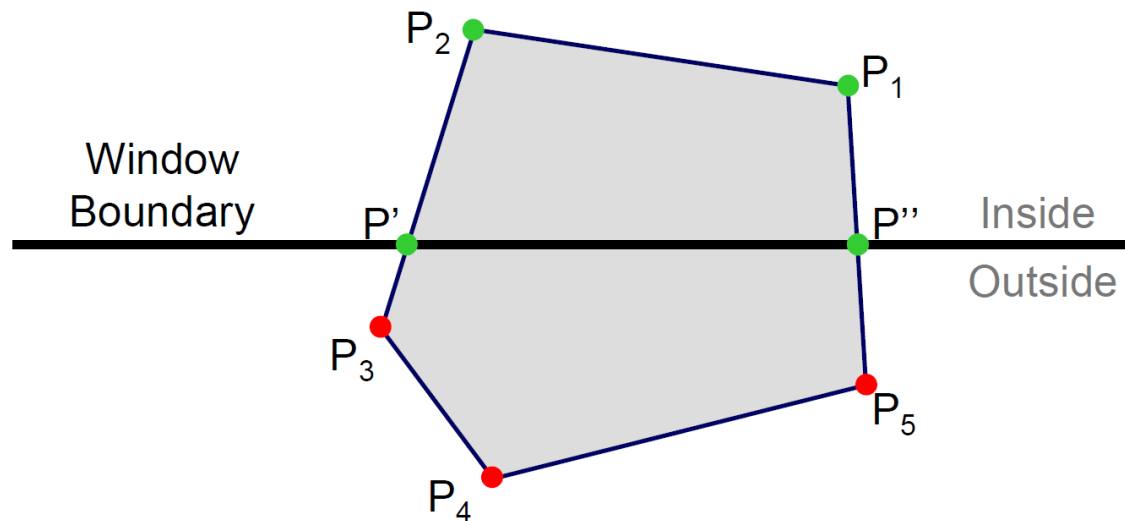
Clipping to a Boundary

- ▶ Do inside test for each point in sequence
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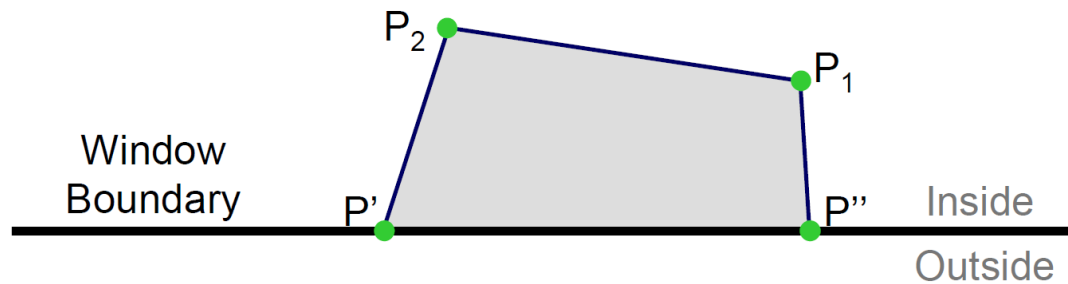
Clipping to a Boundary

- ▶ Do inside test for each point in sequence
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- ▶ Remove points outside of boundary



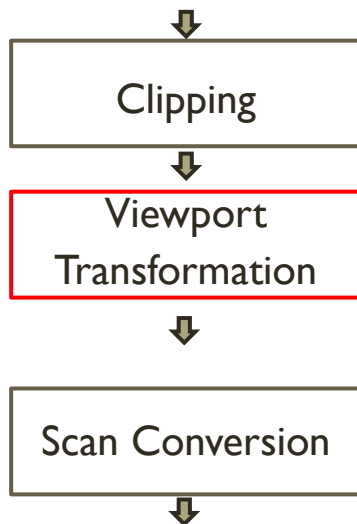
Clipping to a Boundary

- ▶ Do inside test for each point in sequence
- ▶ Insert new points when crossing the boundary
- ▶ Remove points outside of boundary



2D rendering pipeline

2D geometry

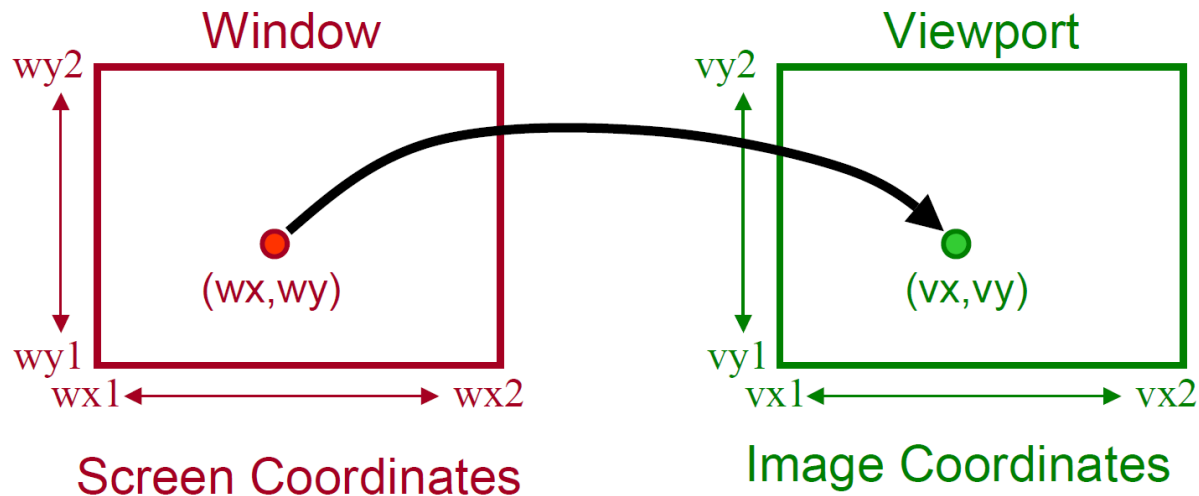


- ▶ Clip and remove geometry outside of the window
- ▶ Transform from screen coordinates to image coordinates
- ▶ Fill pixels on the screen

2D Image

Viewport Transformation

- ▶ Window to viewport mapping

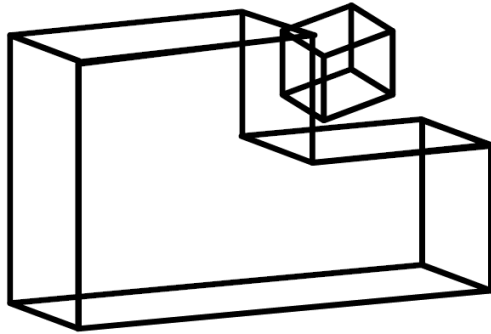


$$\begin{aligned} vx &= vx1 + (wx - wx1) * (vx2 - vx1) / (wx2 - wx1); \\ vy &= vy1 + (wy - wy1) * (vy2 - vy1) / (wy2 - wy1); \end{aligned}$$

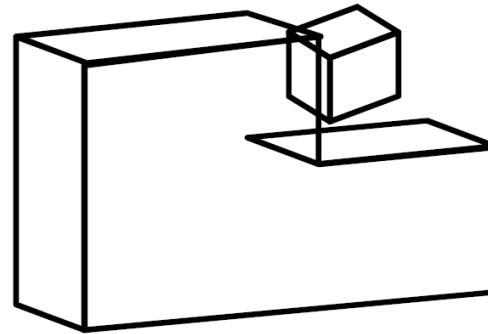
Overview

- ▶ Clipping
 - ▶ Point Clipping
 - ▶ Line Clipping
 - ▶ Polygon Clipping
- ▶ **Hidden Surface Removal**

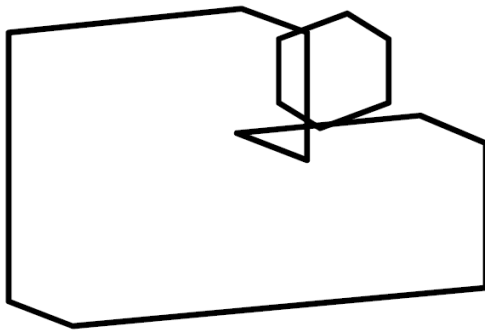
Visibility



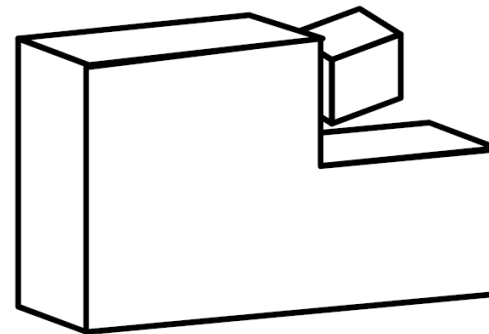
wireframe model



front faces



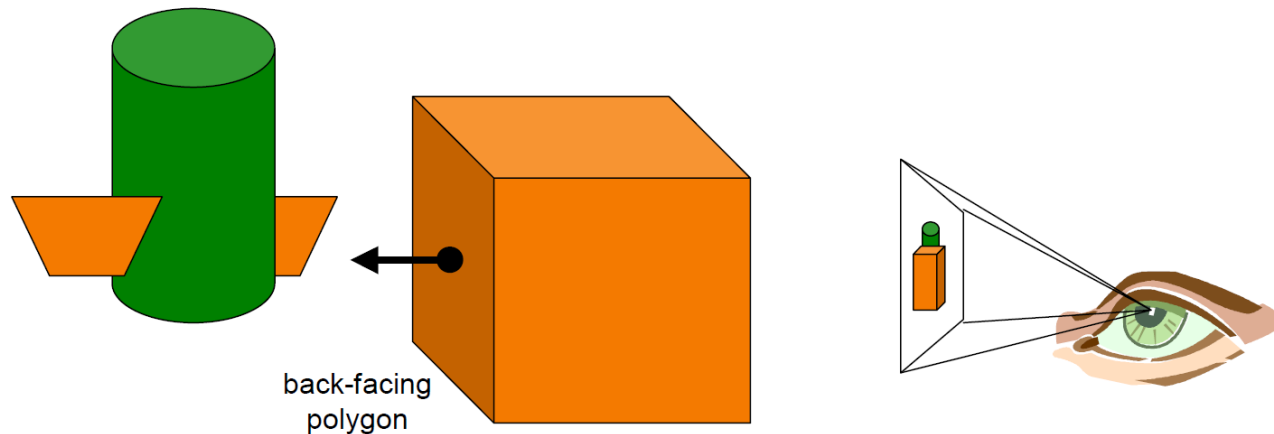
silhouette



visible faces, edges

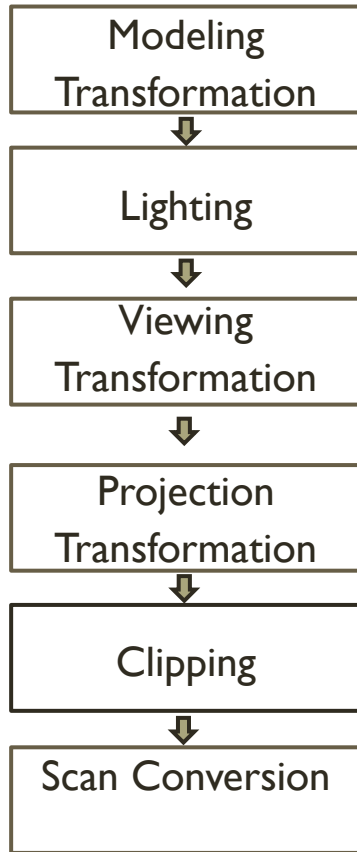
Motivation

- ▶ Surfaces may be back-facing
- ▶ Surfaces may be occluded
- ▶ Surfaces may overlap in the image plane
- ▶ Surfaces may intersect



3D rendering pipeline

3D polygons



2D Image

- Somewhere here we have to determine which objects are visible and which are hidden

Basic algorithms for HSR

- ▶ Clipping
 - ▶ Point Clipping
 - ▶ Line Clipping
 - ▶ Polygon Clipping
- ▶ **Hidden Surface Removal**

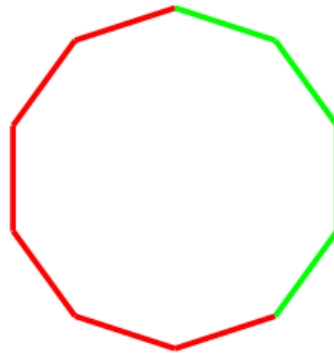
Optimizing visibility

- ▶ Get rid of objects that are surely not visible
- ▶ Frustum culling
- ▶ Occlusion culling
- ▶ Back-face culling



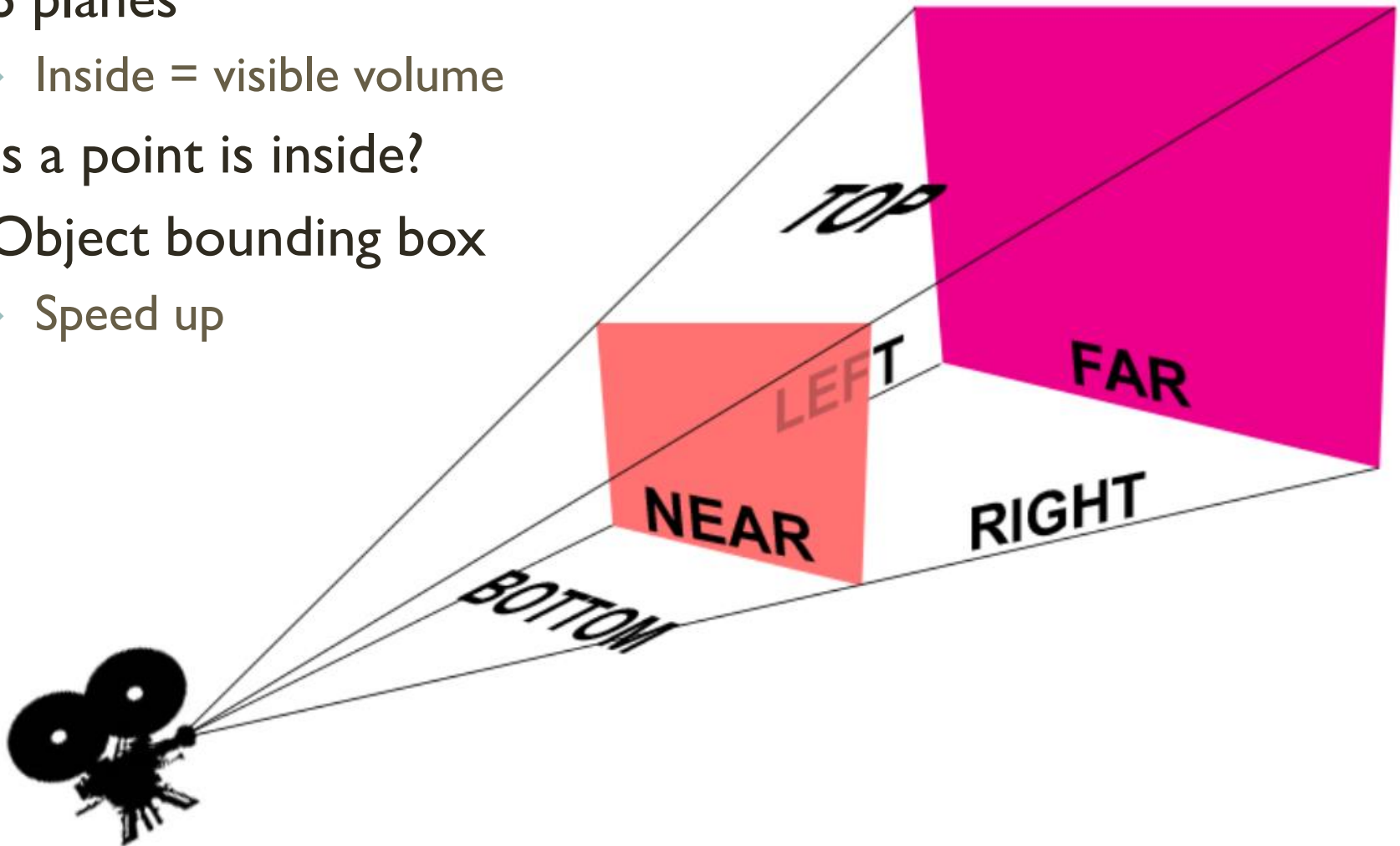
Back-face culling

- ▶ Which object faces are visible?
- ▶ Remember normal vector (face orientation)



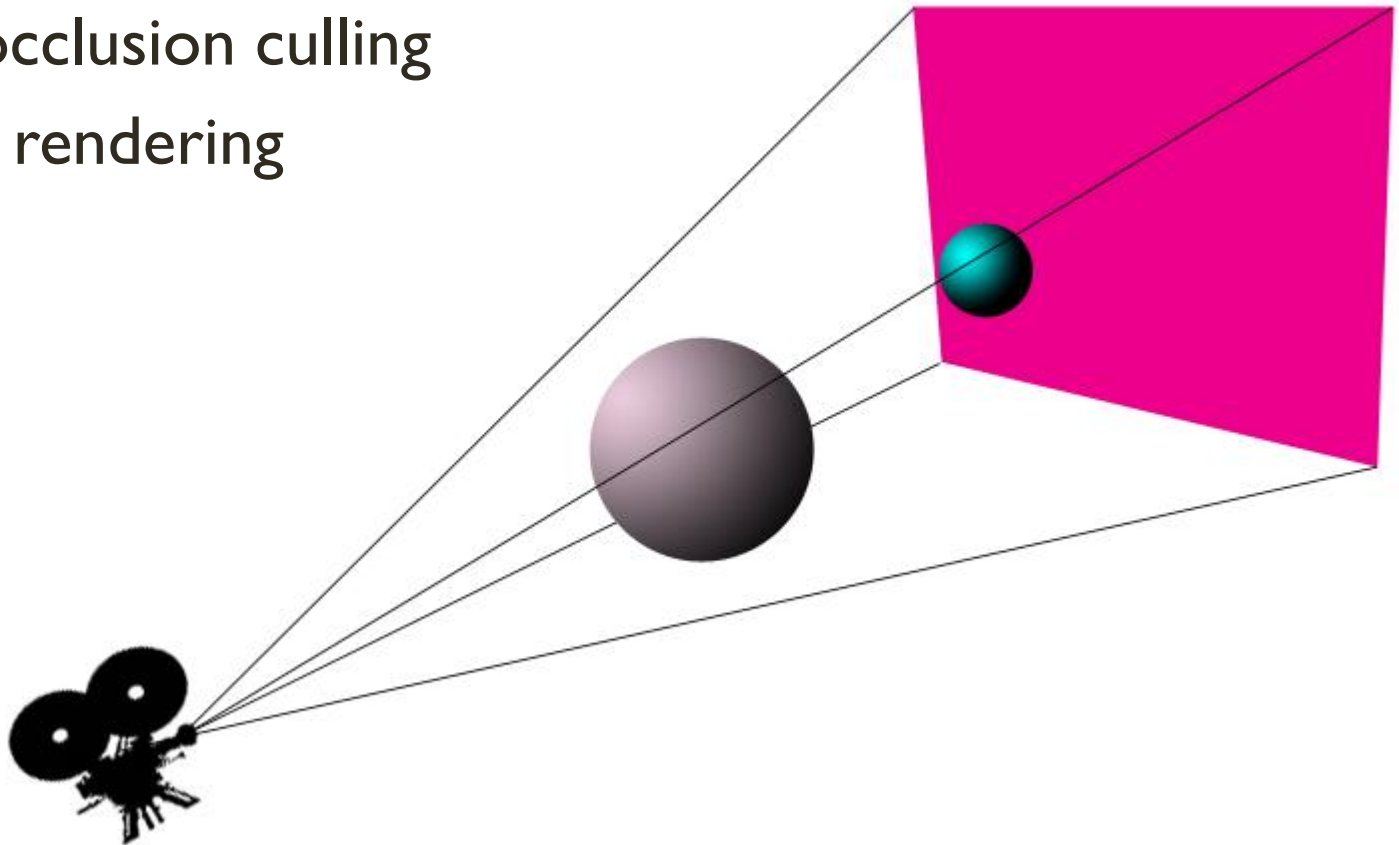
Frustum culling

- ▶ 6 planes
 - ▶ Inside = visible volume
- ▶ Is a point is inside?
- ▶ Object bounding box
 - ▶ Speed up



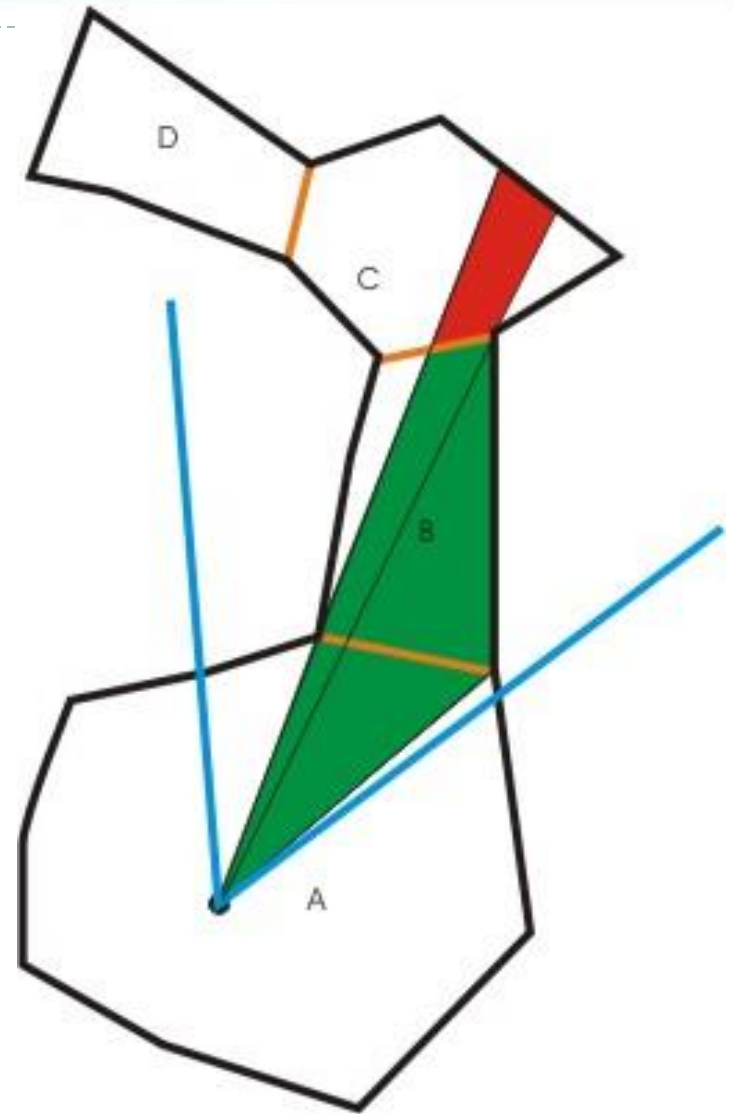
Occlusion culling

- ▶ Some objects are fully occluded by others
- ▶ Spatial relations between objects
- ▶ Portals, occlusion culling
- ▶ Realtime rendering

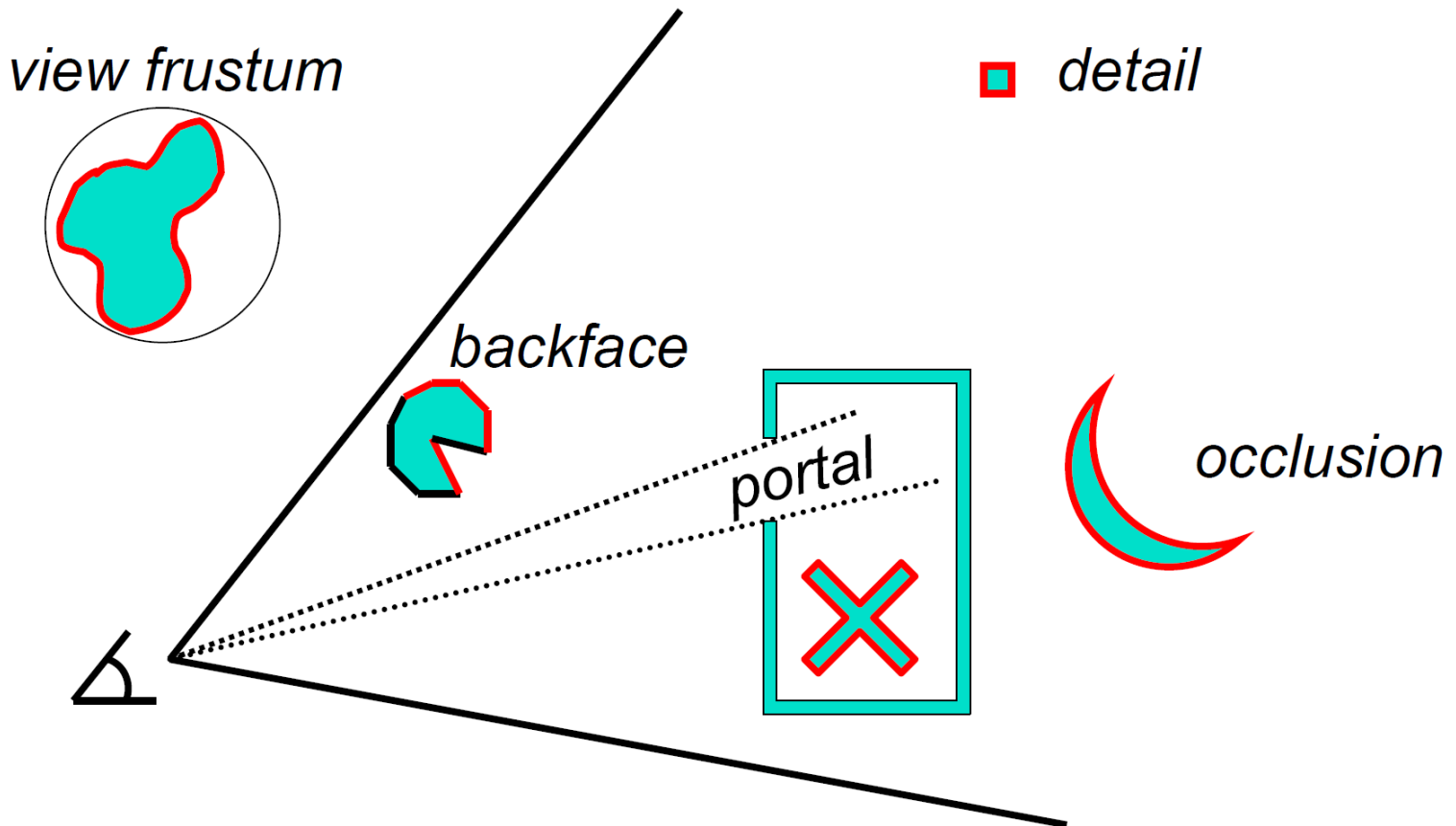


Portal culling

- Some parts of the scene are not visible from some other parts of the scene



Optimizing visibility

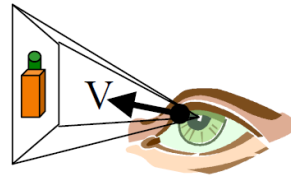
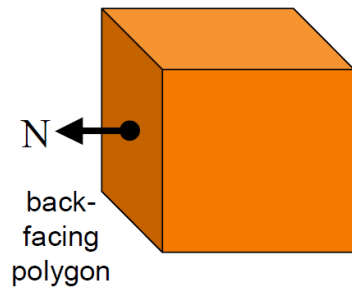


Basic algorithms for HSR

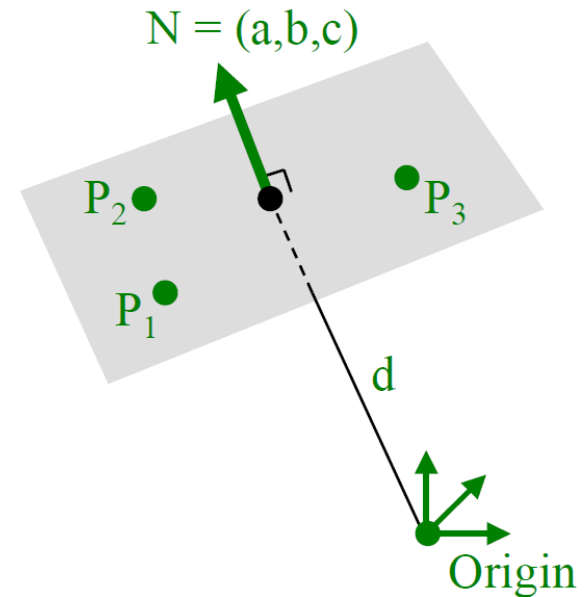
- ▶ Back-face culling
- ▶ Depth sort
- ▶ Z-Buffer

Back-face culling

- ▶ How do we test back-facing polygons ?
- ▶ Dot product the normal and view direction



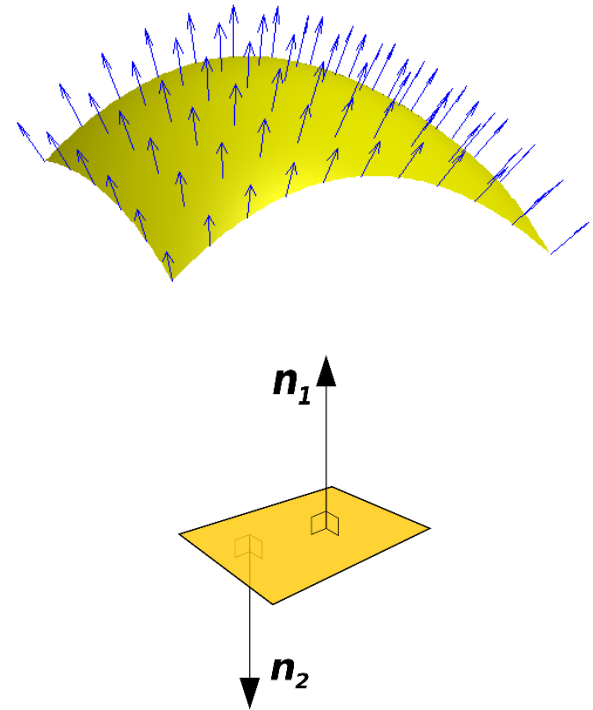
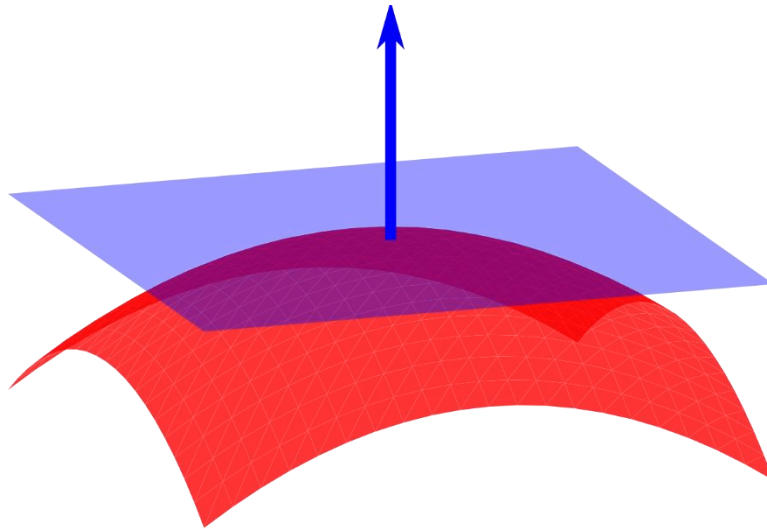
$$N \cdot V > 0$$



Surface Normals

► Normal

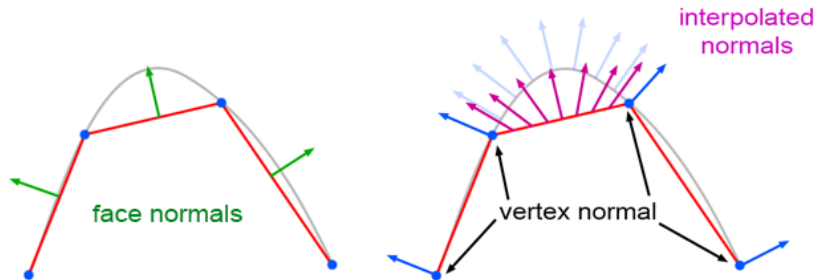
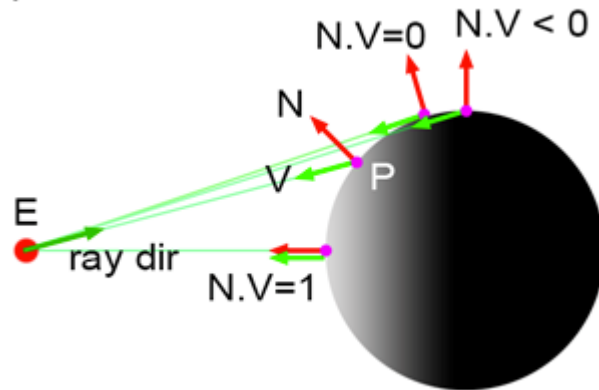
- Cross product of surface tangent vectors
- Length normalized to 1



Vertex / Fragment Normals

- ▶ Dot product the normal and view direction
- ▶ Fragment normals can be interpolated from vertex normals

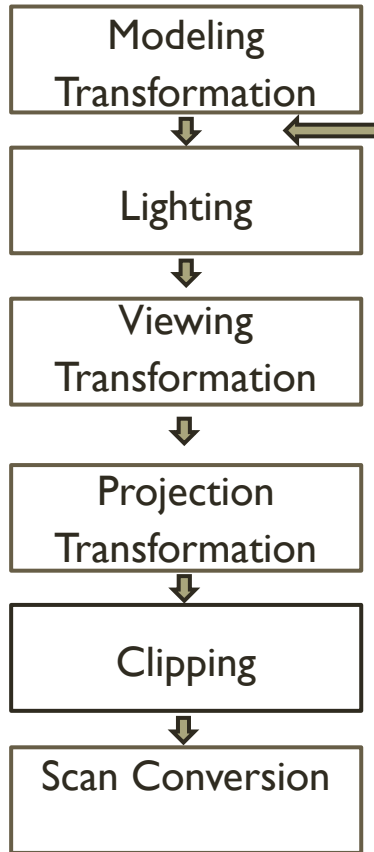
profile view



© www.scratchapixel.com

3D rendering pipeline

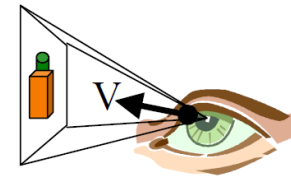
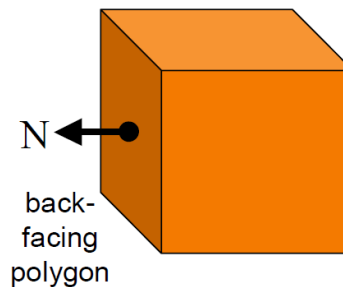
3D polygons



2D Image

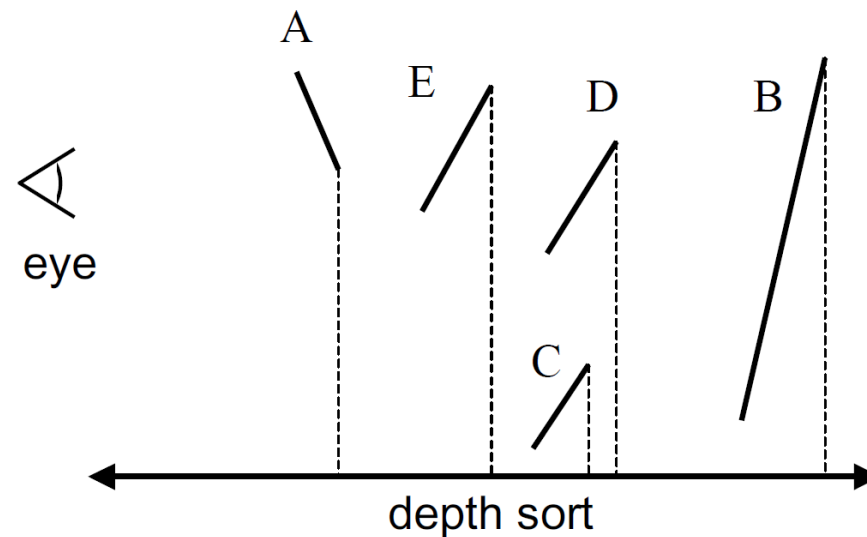
► Back-face culling

► Remove all polygons that are back-facing



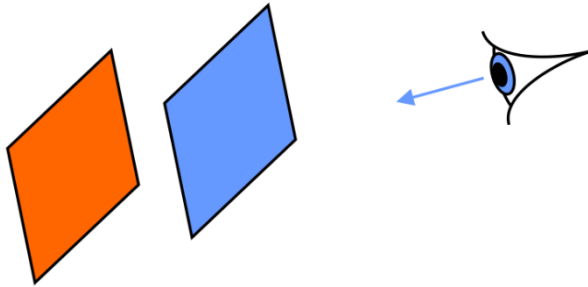
Depth sort

- ▶ “Painter’s algorithm”
- ▶ Sort surfaces by maximum depth
- ▶ Draw surfaces in back to front order

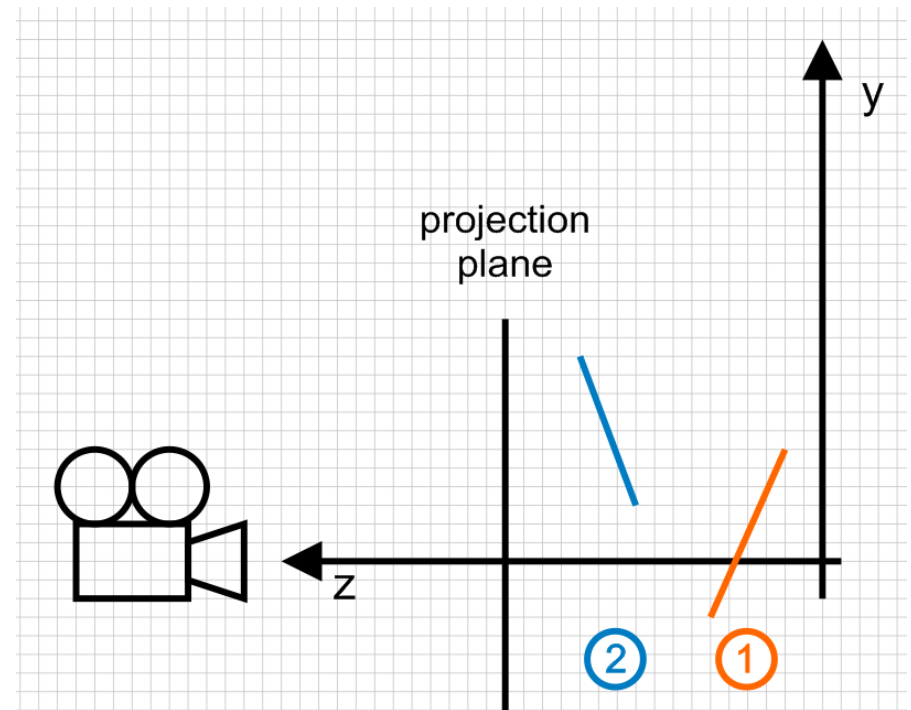
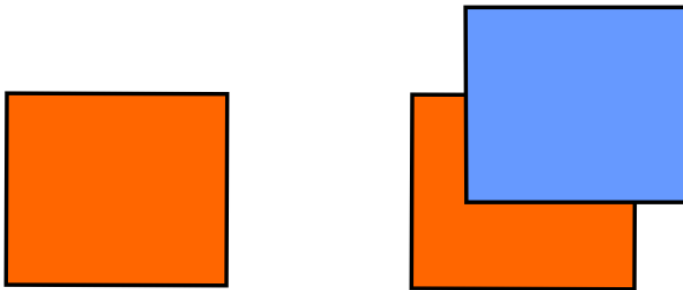


Painter's algorithm

- Sort faces in a back-to-front order, render

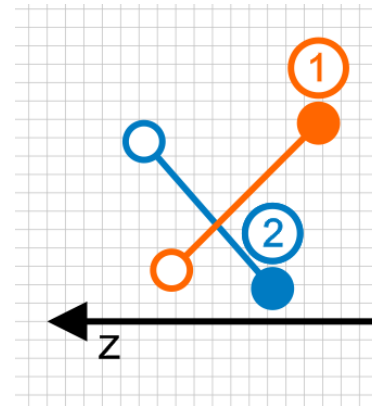
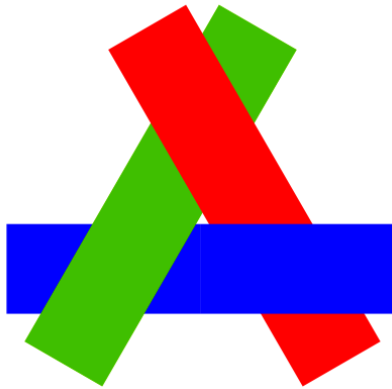


- New pixels over-write old pixels



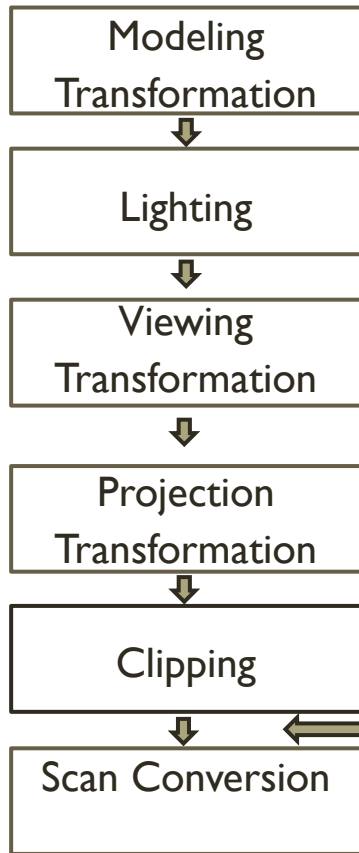
Painter's algorithm problems

- ▶ Intersecting faces
- ▶ Cyclically overlapping faces
- ▶ Redundant rendering



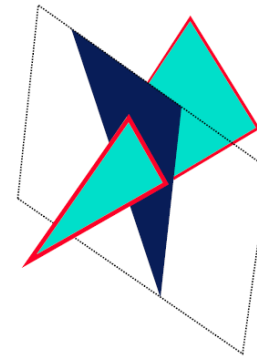
3D rendering pipeline

3D polygons

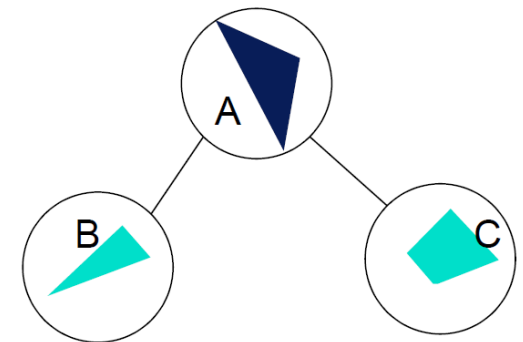


2D Image

- ▶ Sorting is often $O(n \log n)$
- ▶ Usually, software implementation only
- ▶ Mostly using BSP-trees



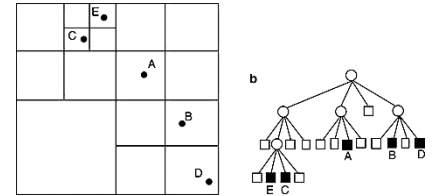
Depth sort



Other algorithms

► Warnock algorithm

- subdivide screen into a quadtree until whole cell empty or whole cell inside polygons

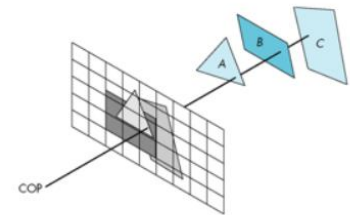


► Reversed painter's algorithm

- paint front-to-back and paint only empty areas

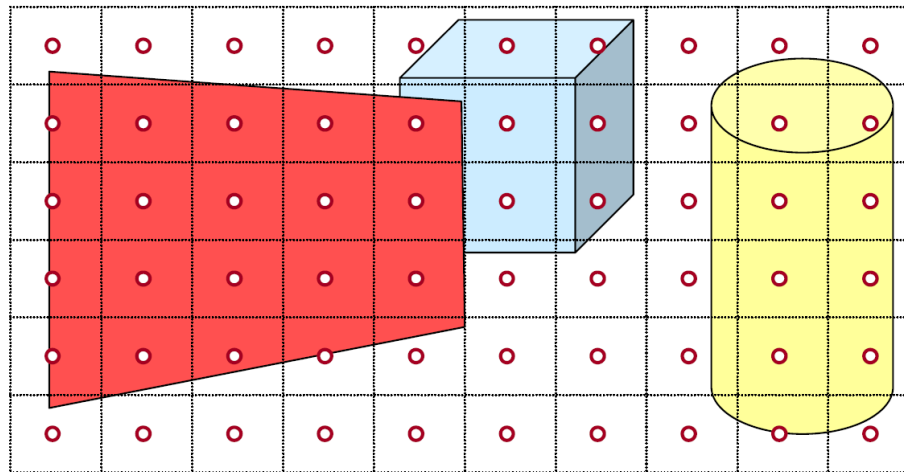
► Z-buffer

- remember z-value for each pixel and only paint when new z is higher



Z-Buffer

- ▶ Also known as depth buffering
- ▶ Stores closest depth of objects for every pixel
 - ▶ Draw only pixels with less depth
 - ▶ Depths are interpolated between vertices



Z-Buffer

- ▶ works in screen space
- ▶ z-buffer $w \times h$
- ▶ for each $0 \leq x \leq w, 0 \leq y \leq h$: $z\text{-buffer}[x, y] \leftarrow z_{\max}$
for each face:
rasterize it into pixels $\{x, y, z\}$
for each face's pixel (x, y, z) :
if $z < z\text{-buffer}[x, y]$
then :
 $z\text{-buffer}[x, y] \leftarrow z$
and $\text{screen}[x, y] \leftarrow \text{color}$

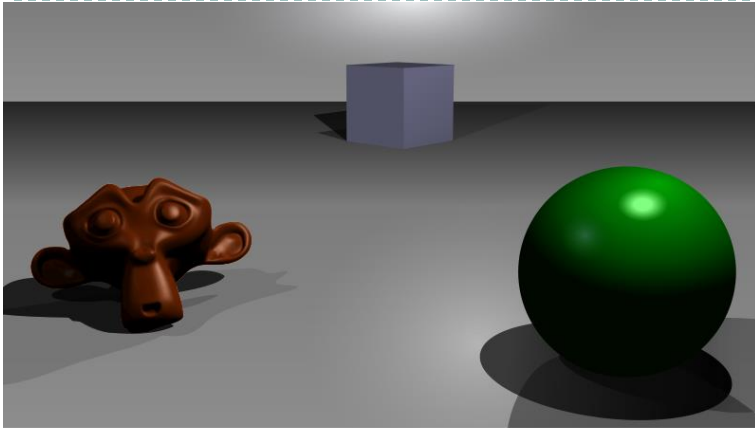


Z-buffer pros and cons

- ▶ GPU support
- ▶ precision issues might occur
- ▶ z-buffer test before per-pixel-lighting or pixel shading saves a lot of redundant work
- ▶ memory demands ($\text{width} \times \text{height} \times \text{precision}$)
 - ▶ can be reduced by scanline ($\text{width} \times 1 \times \text{precision}$)



Z-Buffer



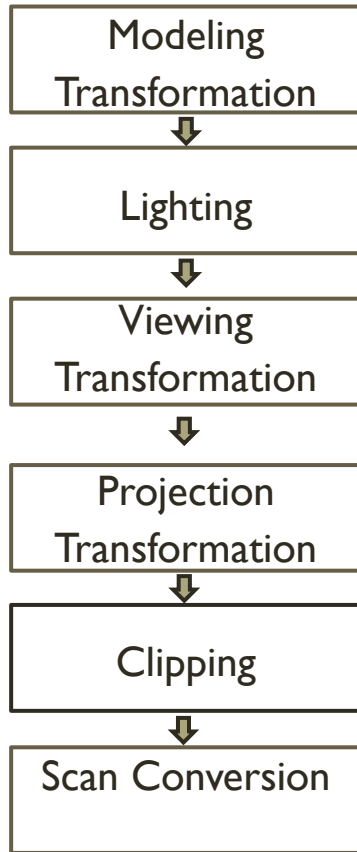
A simple three-dimensional scene



Z-buffer representation

3D rendering pipeline

3D polygons



2D Image

- ▶ Sorting not needed
- ▶ Excellent for hardware
- ▶ Requires additional memory to store the depth values
- ▶ Subject to aliasing

← ▶ Z-Buffer

Visibility

- ▶ Can be solved in different ways
 - ▶ Painter's algorithm / Depth sort
 - ▶ Binary space partitioning (BSP)
 - ▶ Warnock algorithm (Quadtree)
 - ▶ Z-buffering
 - ▶ Raycasting / Raytracing

Culling

- ▶ Viewing-frustum culling
- ▶ Back-face culling
- ▶ Contribution culling (LoD)
- ▶ Occlusion culling
 - ▶ Potentially visible set (PVS)
 - ▶ Portal rendering

Next Lecture

Textures and Mappings



Acknowledgements

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Matej Novotný, GSVM lectures at FMFI UK



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Output of all the publications and great team work



Very best data from 3D cameras



Questions ?!



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