



**Fundamentals of
Computer Graphics and Image Processing
Animations, Dynamics (08)**

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Outline

- ▶ Principles of animation
- ▶ Keyframe animation
- ▶ Articulated figures
- ▶ Kinematics
- ▶ Dynamics



How the lectures should look like #1

- Ask questions, please!!!
- Be communicative
- More active you are, the better for you!



Manual animation

- ▶ Stop-motion animation
- ▶ e.g. Coraline, Wallace & Gromit, etc.



Computer Animation

- ▶ What is animation?
 - ▶ Make objects change over time according to scripted actions
- ▶ What is simulation?
 - ▶ Predict how object change over time according to physical laws



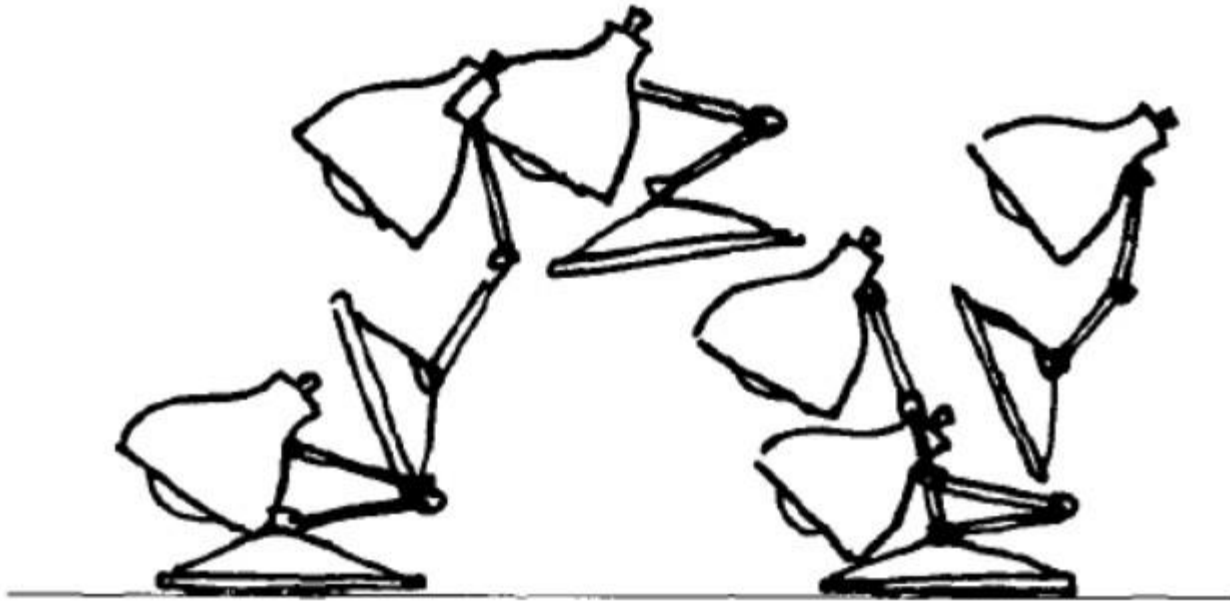
Computer Animation

- ▶ Animation pipeline
 - ▶ 3D Modeling
 - ▶ Articulation
 - ▶ Motion specification
 - ▶ Motion simulation
 - ▶ Shading
 - ▶ Lighting
 - ▶ Rendering
 - ▶ Postprocessing



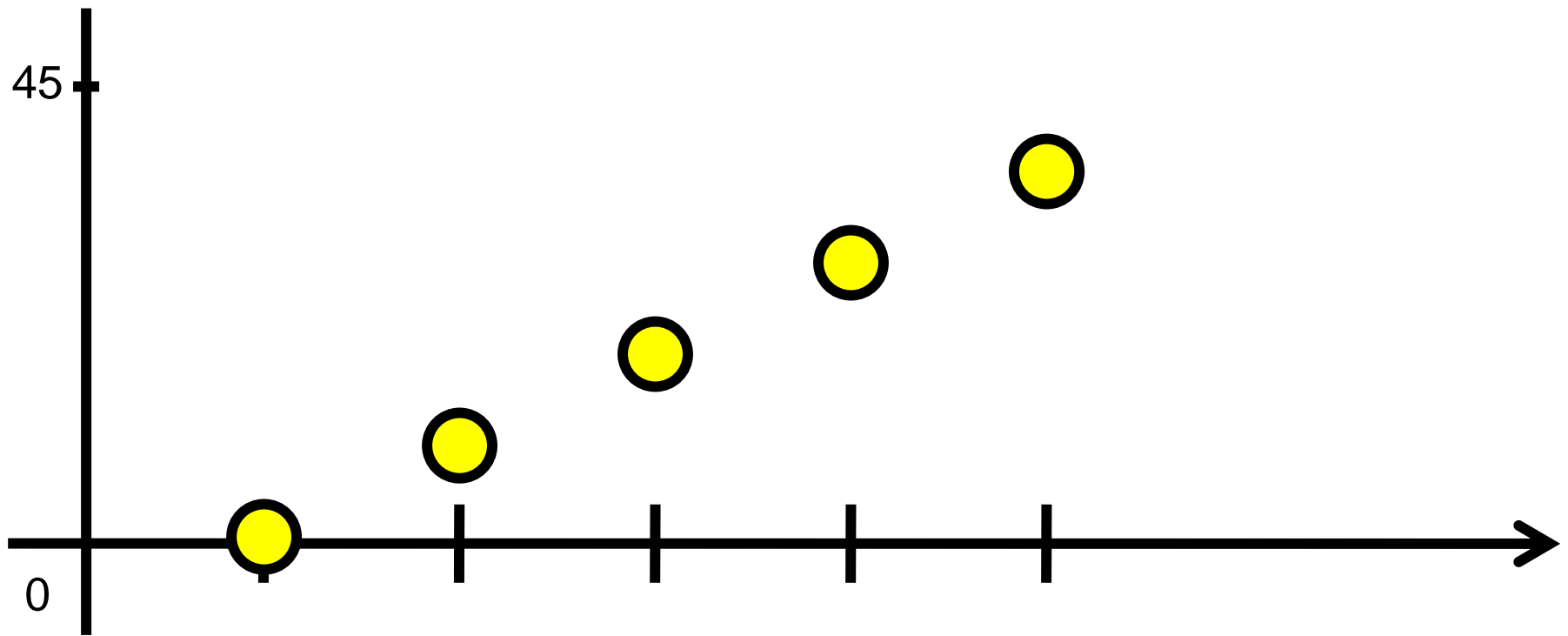
Keyframe Animation

- Define character poses at specific time steps called “keyframes”



Inbetweening (“tweening”)

- Computing missing values based on existing surrounding values



Inbetweening (“tweening”)

- ▶ Linear (constant)

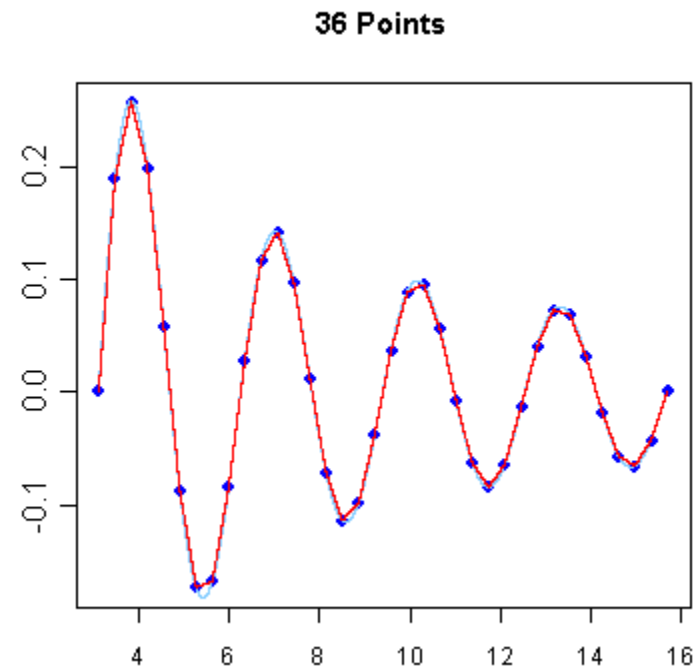
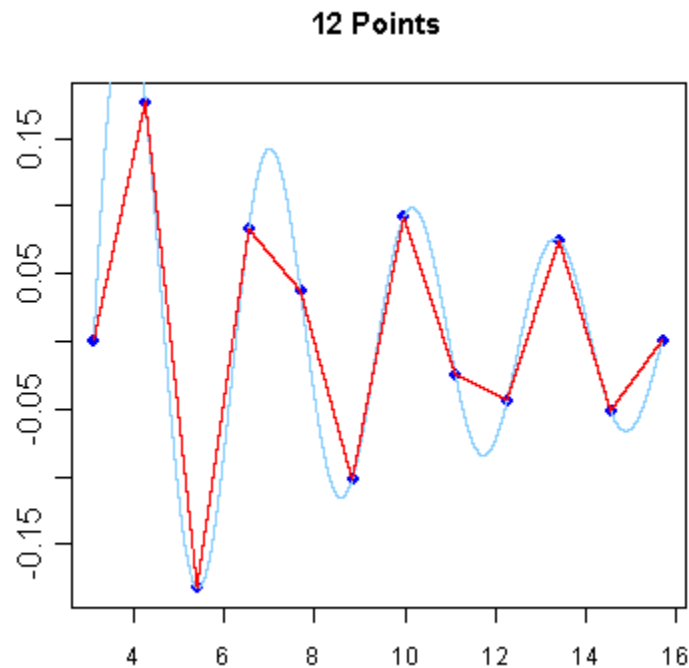


- ▶ Ease-in, ease-out



Keyframe Animation

- Inbetweening:
 - Linear interpolation – usually not enough continuity



Spline Continuity

- ▶ How to ensure curves are “smooth”
- ▶ Generally, we have three levels of continuity
- ▶ C^0 - The curves meet
- ▶ C^0 & C^1 - The tangents are shared
- ▶ C^0 & C^1 & C^2 - The “speed” is the same

C0 Continuity

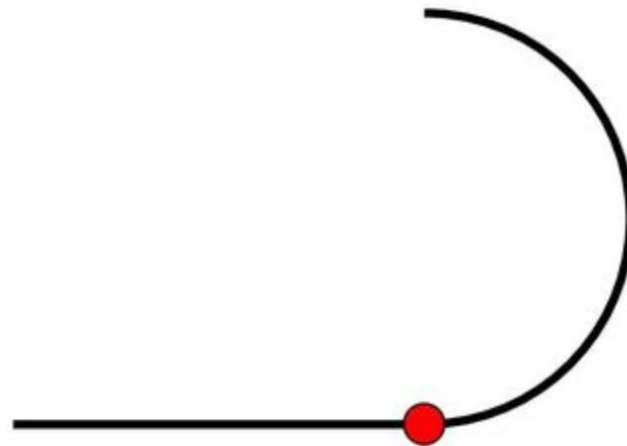
- ▶ Zero order parametric continuity



C^0 continuity

C0 & C1 Continuity

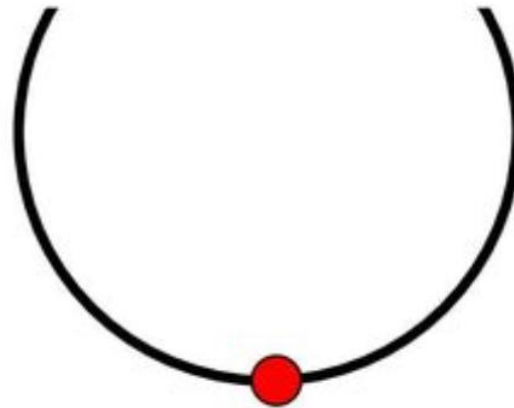
- First order parametric continuity



C¹ continuity

C0 & C1 & C2 Continuity

- ▶ Second order parametric continuity



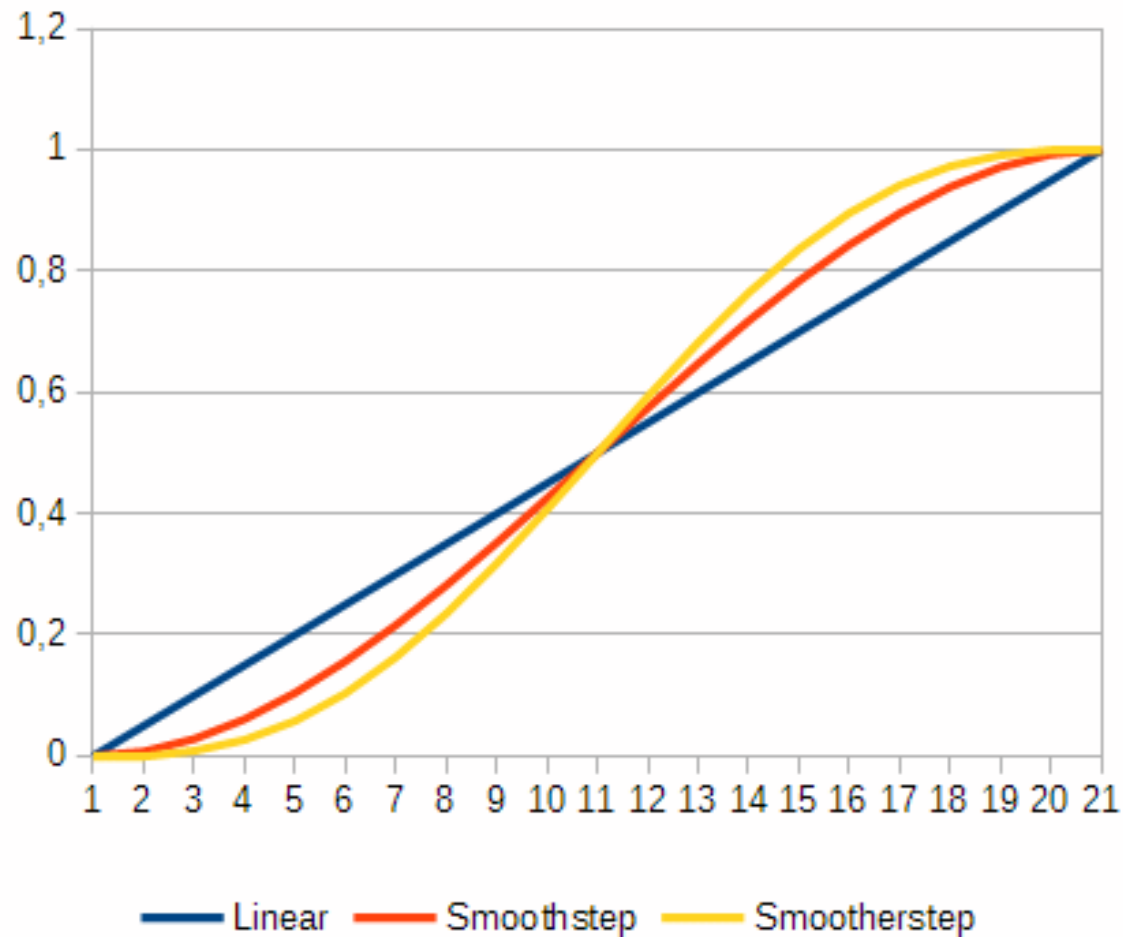
C² continuity

Implications for animation

- ▶ Linear interpolation is only $C0$
 - ▶ Movement changes instantly at keyframes
 - ▶ Very unnatural looking
- ▶ We need at least $C0$ & $C1$ continuity
 - ▶ Hermite interpolation
 - ▶ Spline interpolation
 - ▶ “Smoothstep” function



Smoothstep

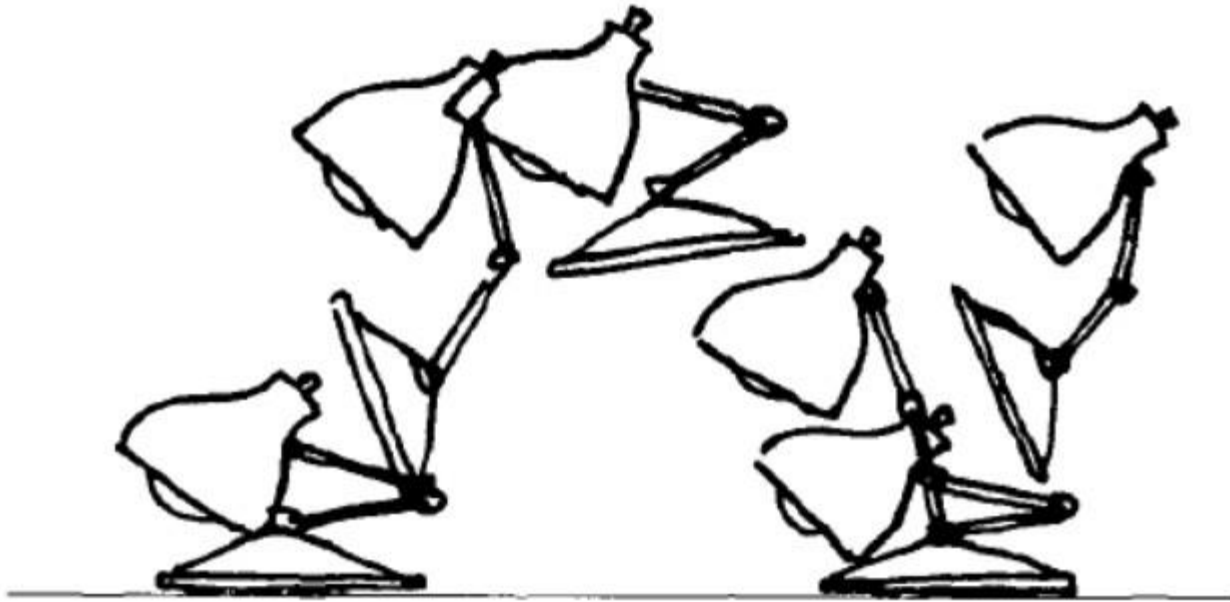


Smoothstep

```
float smootherstep(float edge0, float edge1, float x)
{
    // Scale, and clamp x to 0..1 range
    x = clamp((x - edge0)/(edge1 - edge0), 0.0, 1.0);
    // Evaluate polynomial
    return x*x*x*(x*(x*6 - 15) + 10);
}
```

Keyframe Animation

- ▶ Inbetweening:
 - ▶ Spline interpolation – may be visually good enough
 - ▶ May not follow physical laws



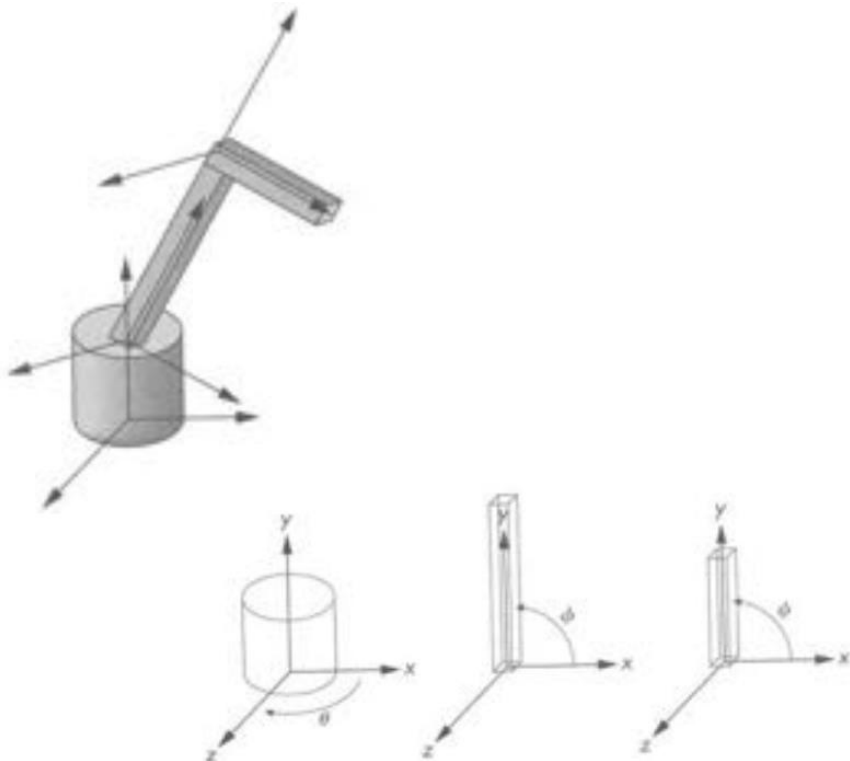
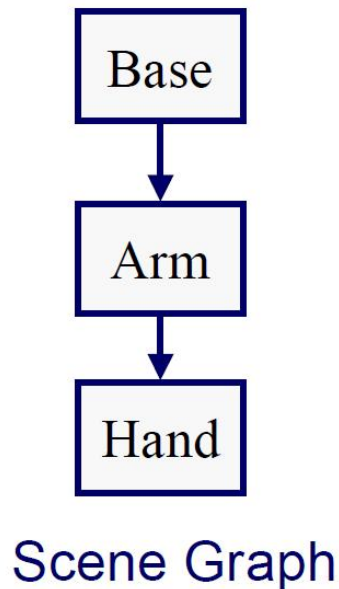
Keyframe Animation

- ▶ Inbetweening:
 - ▶ Inverse kinematics or dynamics



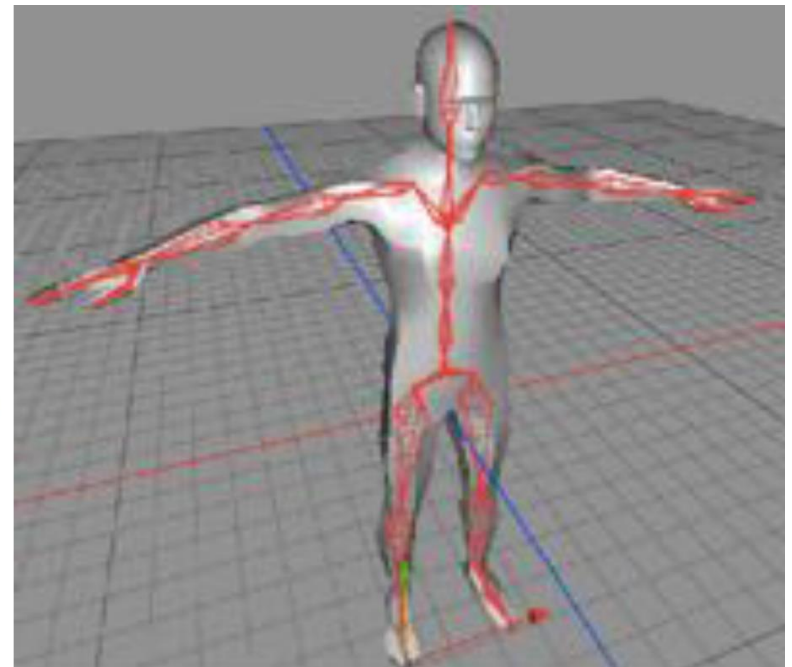
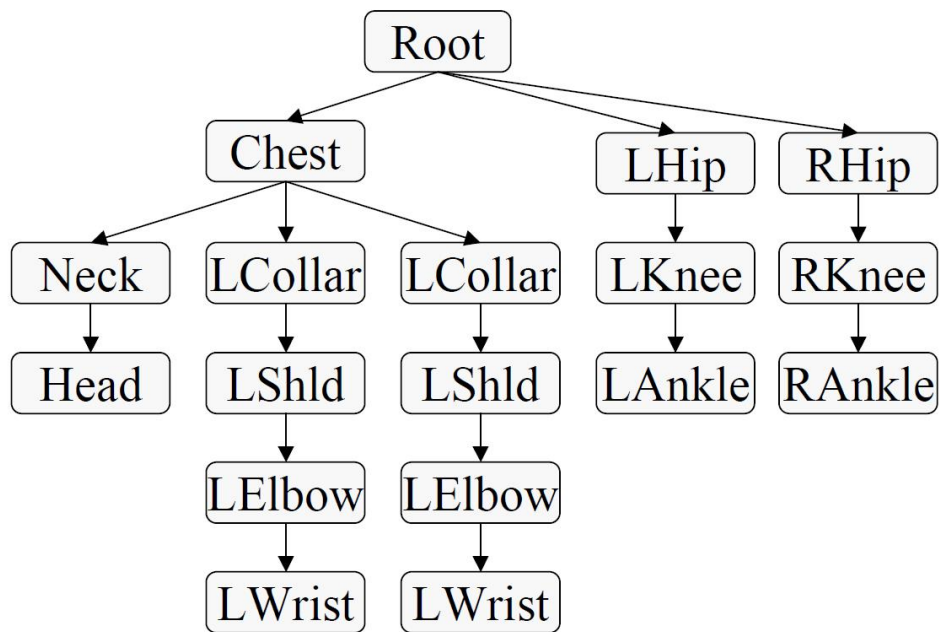
Articulated Figures

- ▶ Character poses described by set of rigid bodies connected by “joints”



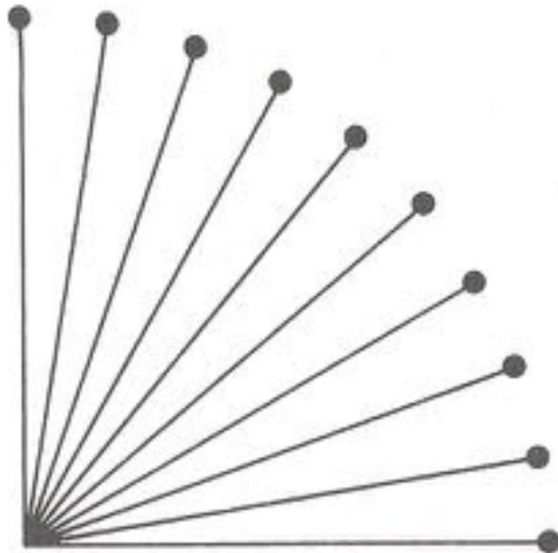
Articulated Figures

- Well suited for humanoid characters

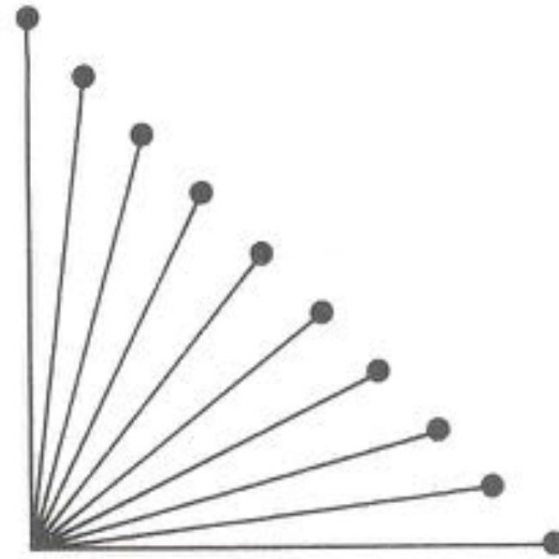


Keyframe Animation

- Inbetweening:
 - Compute angles between keyframes



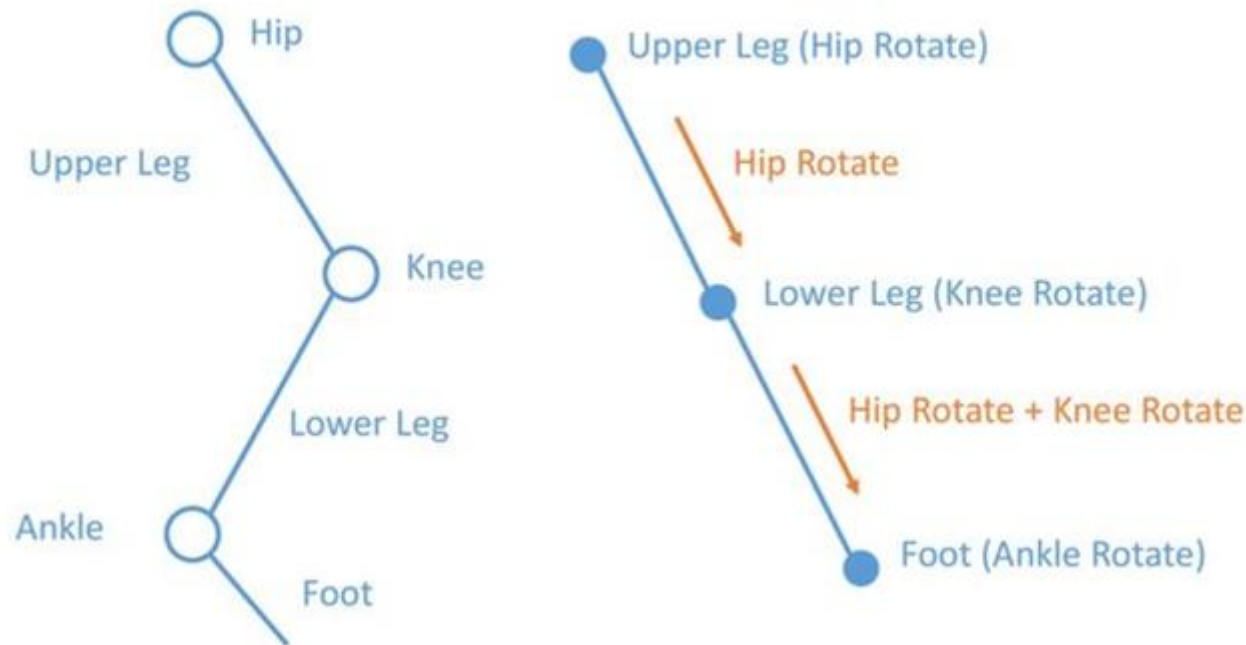
Good arm



Bad arm

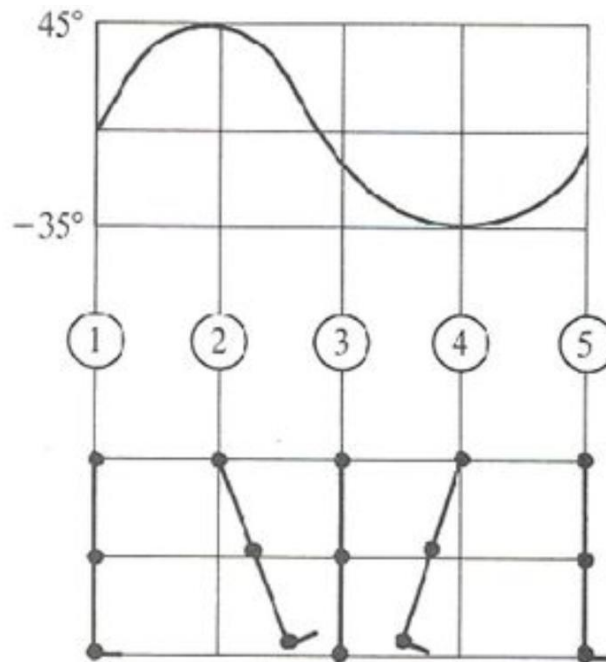
Example: Walk Cycle

- Inbetweening:
 - Compute angles between keyframes



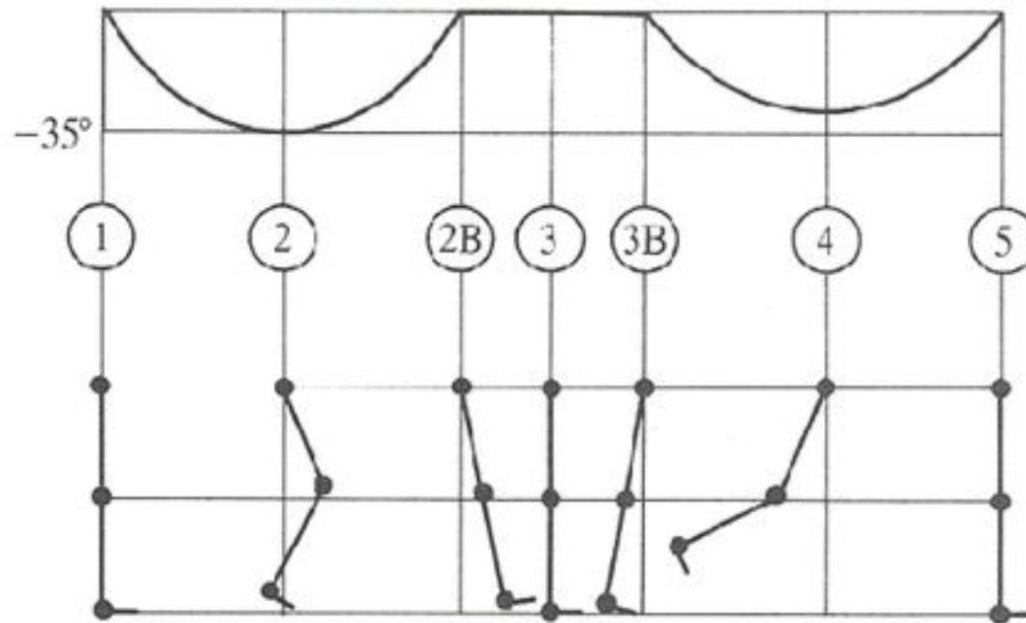
Example: Walk Cycle

► Hip joint orientation



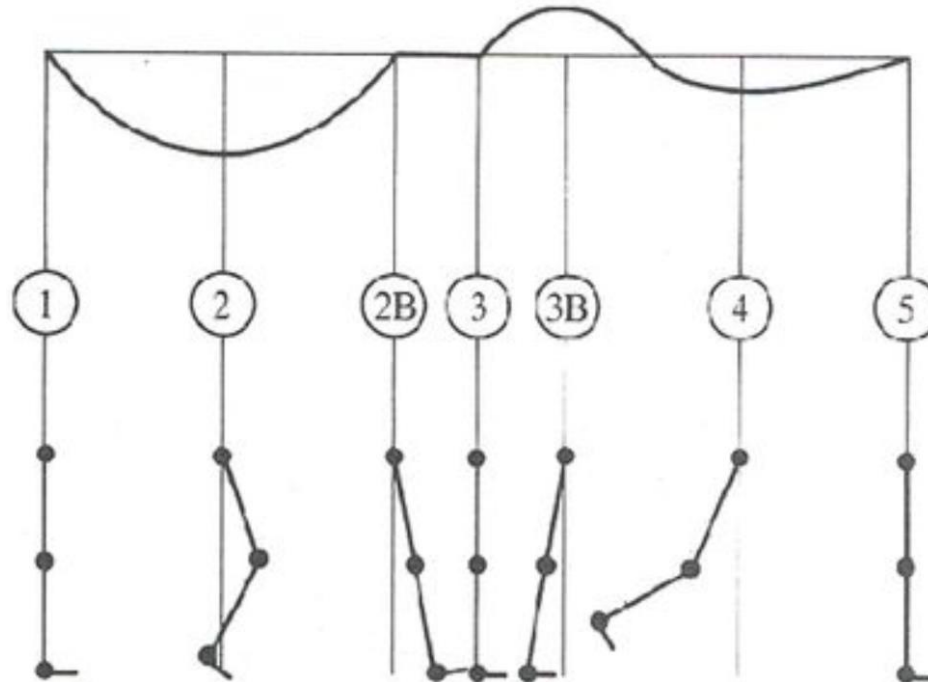
Example: Walk Cycle

► Knee joint orientation



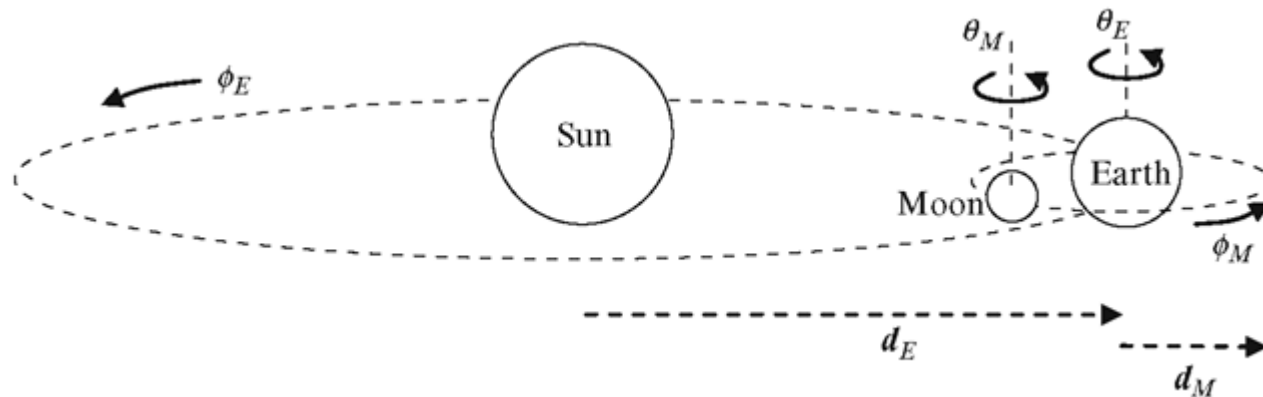
Example: Walk Cycle

► Ankle joint orientation



Animation Hierarchies

- ▶ Animate objects in relation to their parent
 - ▶ Sun matrix is M_s
 - ▶ Earth matrix is $M_s M_e$
 - ▶ Moon matrix is $M_s M_e M_m$



Kinematics and Dynamics

- ▶ **Kinematics**

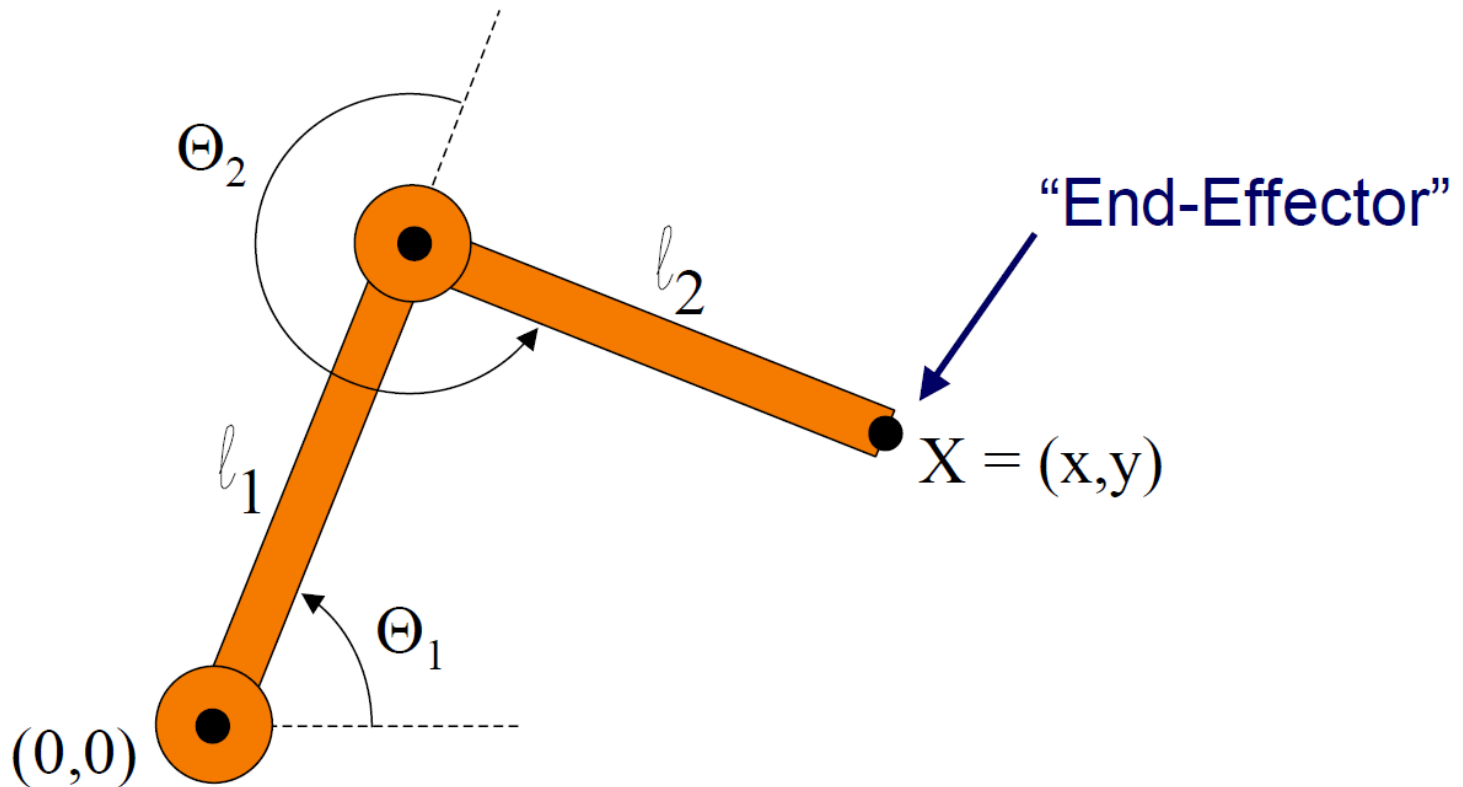
- ▶ Considers only motion
- ▶ Determined by positions, velocities, accelerations

- ▶ **Dynamics**

- ▶ Considers underlying forces
- ▶ Capture motion from initial positions and physics

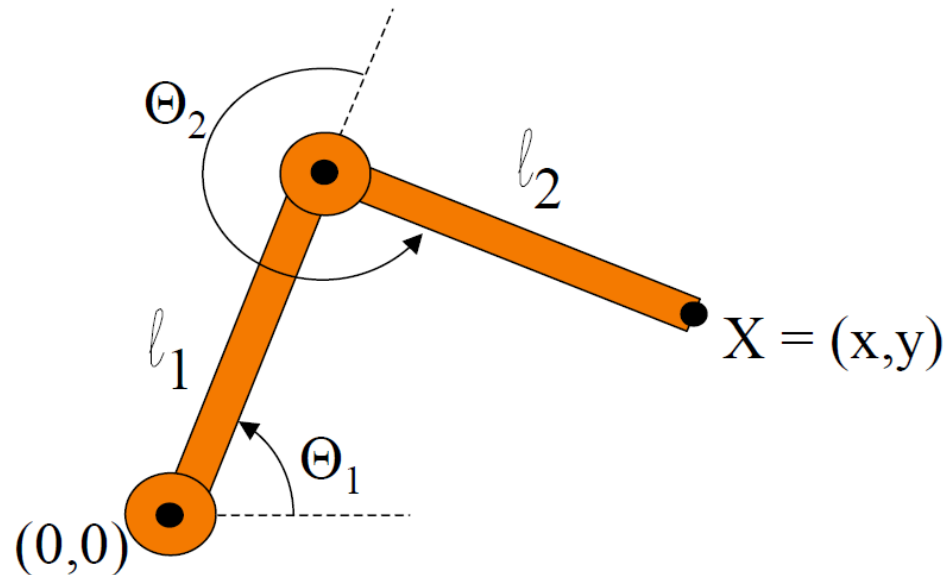
Example: 2-Link Structure

- Two links connected by rotational joints



Forward Kinematics

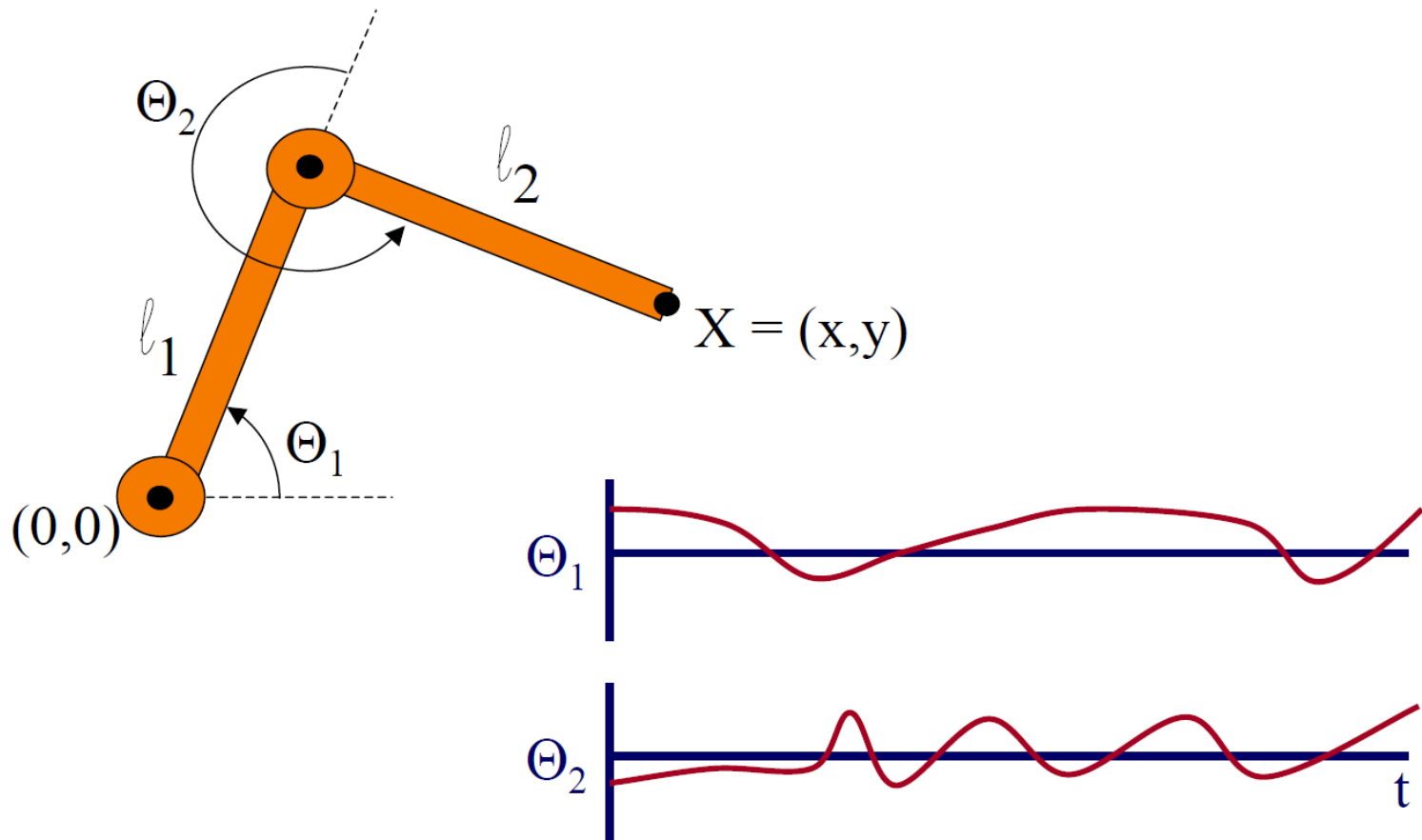
- ▶ Animators specifies angles Θ_1 and Θ_2
- ▶ Computer finds position of end effector: X



$$X = (l_1 \cos \Theta_1 + l_2 \cos(\Theta_1 + \Theta_2), l_1 \sin \Theta_1 + l_2 \sin(\Theta_1 + \Theta_2))$$

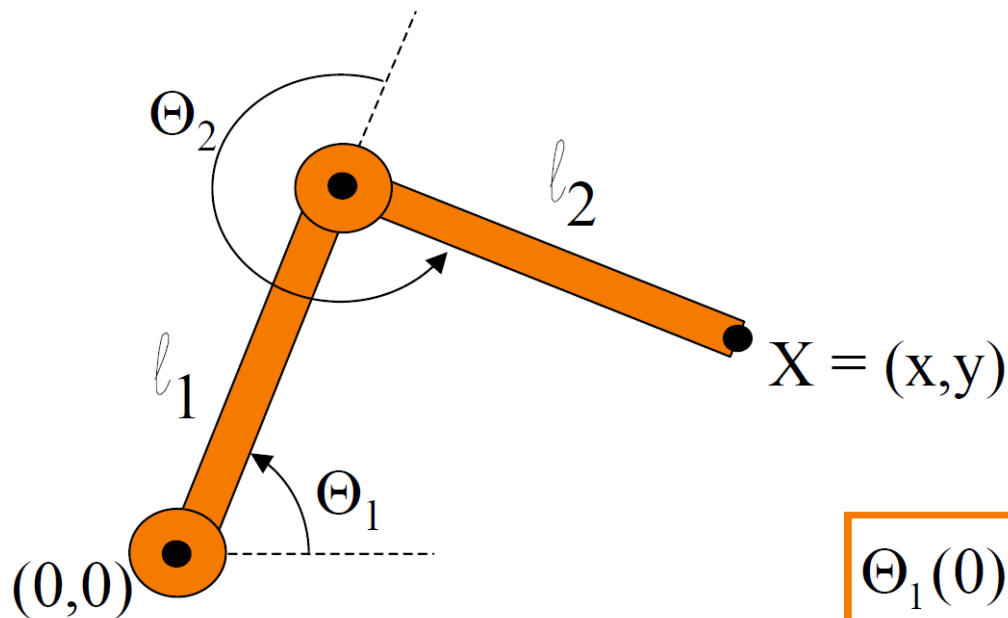
Forward Kinematics

- ▶ Joint motion can be specified by spline curves



Forward Kinematics

- Joint motions can be specified by initial conditions

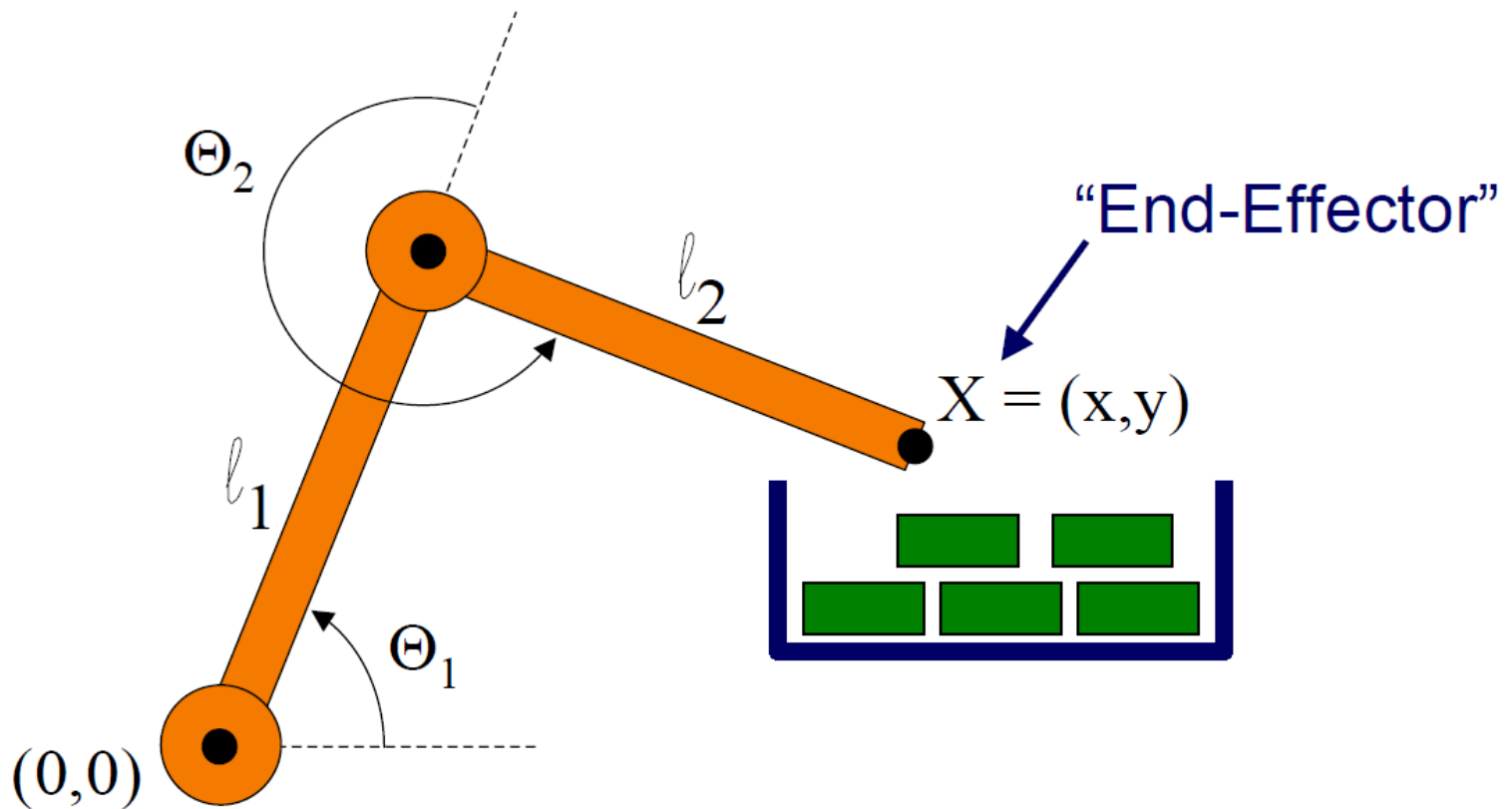


$$\Theta_1(0) = 60^\circ \quad \Theta_2(0) = 250^\circ$$

$$\frac{d\Theta_1}{dt} = 1.2 \quad \frac{d\Theta_2}{dt} = -0.1$$

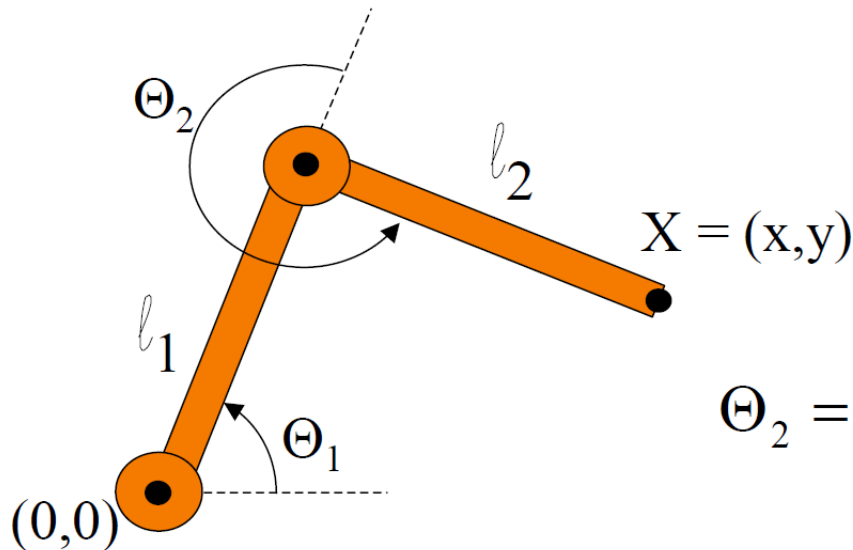
Example: 2-Link Structure

- What if animator knows position of “end effector”



Inverse Kinematics

- Animator specifies end effector positions: X
- Computer finds joint angles Θ_1 and Θ_2

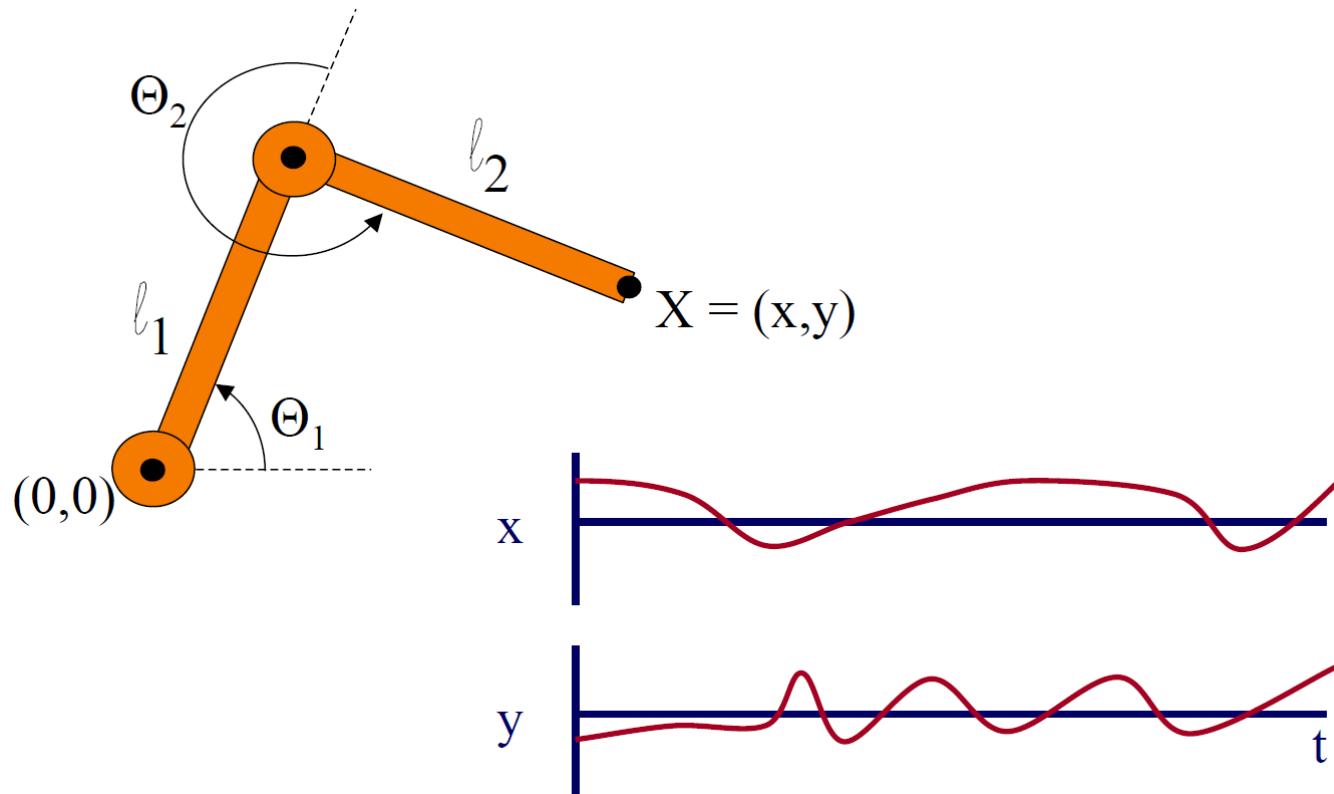


$$\Theta_2 = \cos^{-1} \left(\frac{x^2 + y^2 - l_1^2 - l_2^2}{2l_1l_2} \right)$$

$$\Theta_1 = \frac{-(l_2 \sin(\Theta_2)x + (l_1 + l_2 \cos(\Theta_2))y)}{(l_2 \sin(\Theta_2))y + (l_1 + l_2 \cos(\Theta_2))x}$$

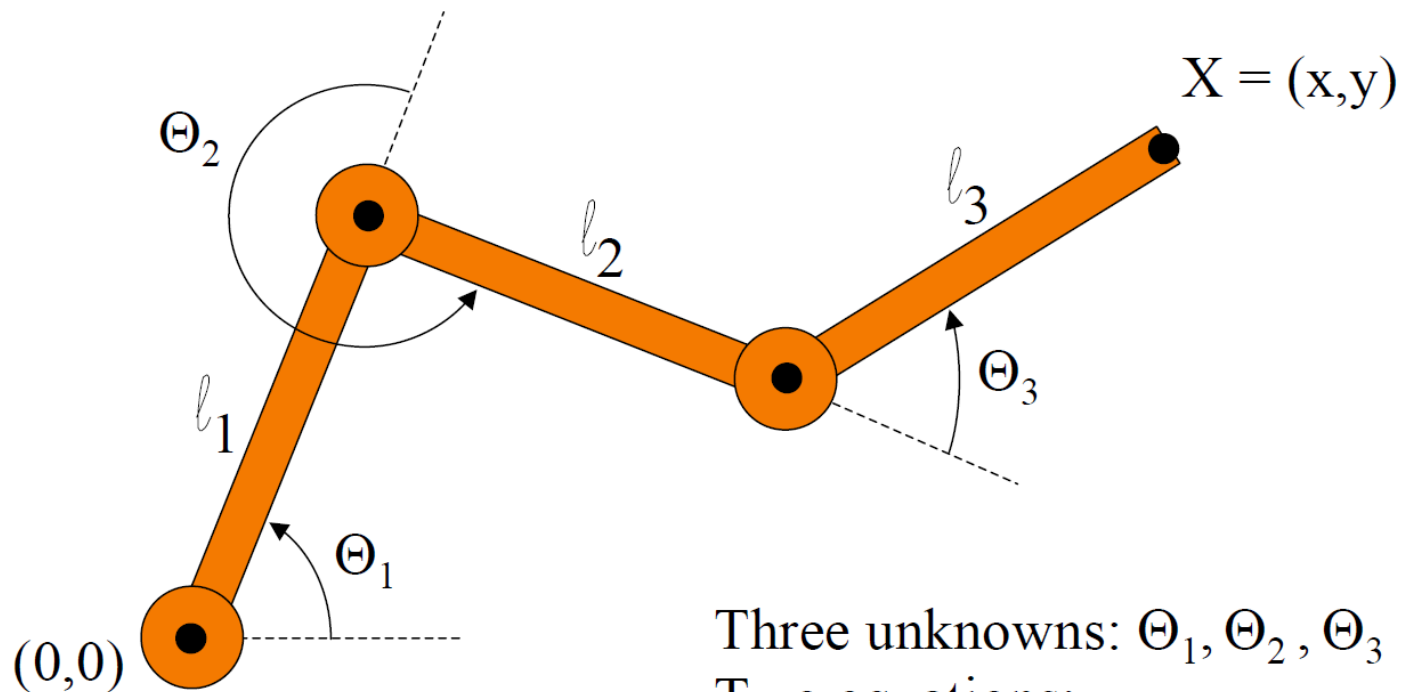
Inverse Kinematics

- End-effector positions can be specified by splines



Inverse Kinematics

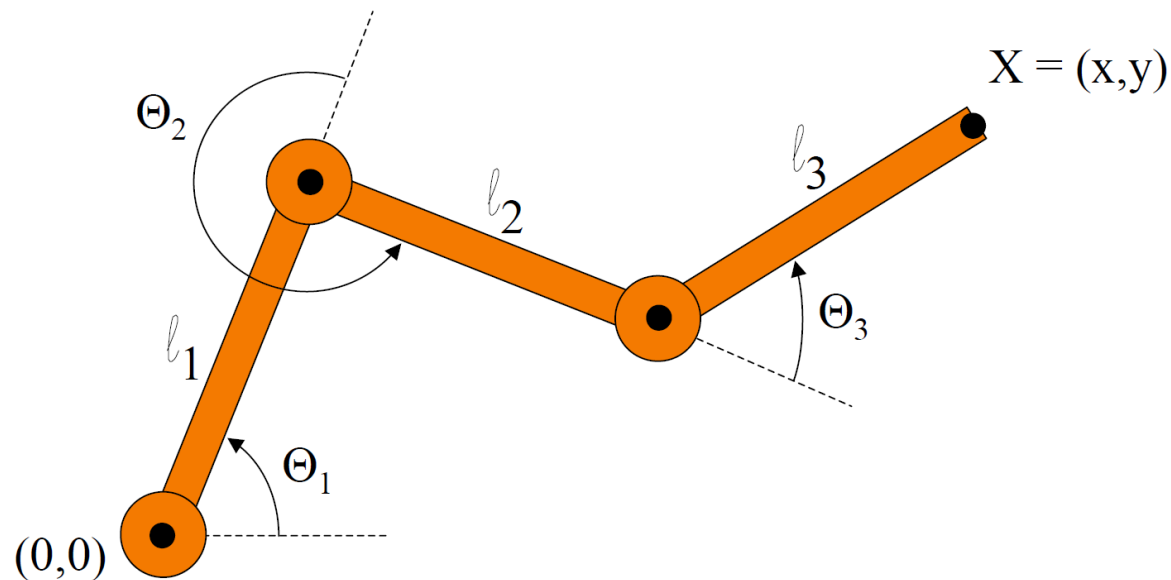
- ▶ Problem with more complex structures
 - ▶ System with equation is usually under-defined
 - ▶ Multiple solutions



Three unknowns: $\Theta_1, \Theta_2, \Theta_3$
Two equations: x, y

Inverse Kinematics

- ▶ Solution for more complex structures
 - ▶ Find best solution (eg. minimize energy in motion)
 - ▶ Non-linear optimization



Inverse Kinematics


- ▶ **Forward Kinematics**

- ▶ Specify conditions (joint angles)
- ▶ Compute conditions of end effectors

- ▶ **Inverse Kinematics**

- ▶ “Goal-directed” motion
- ▶ Specify goal positions of end effectors
- ▶ Compute conditions required to achieve goal

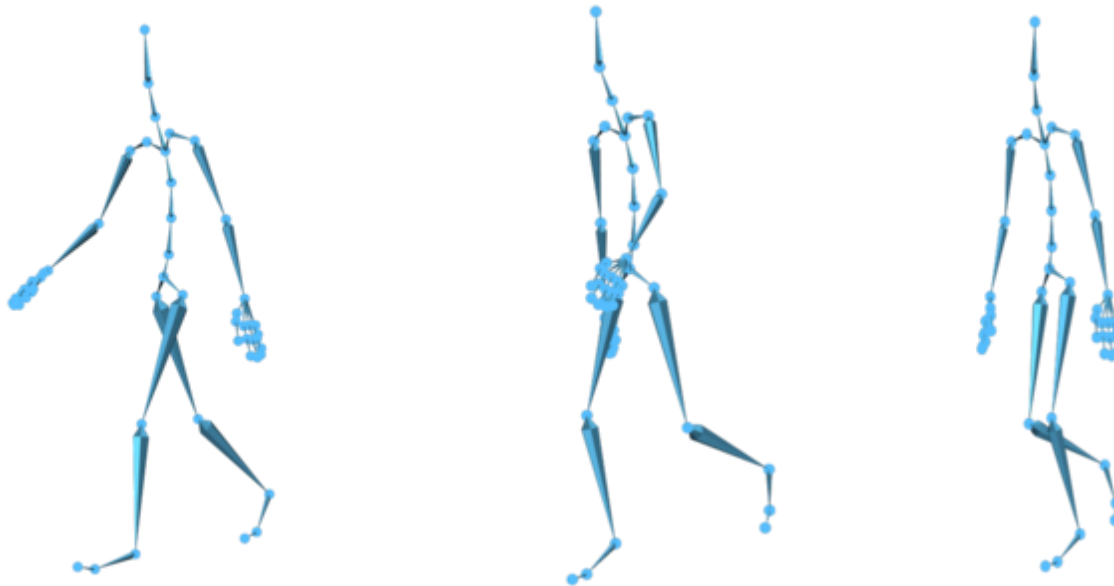




Character Animation (Linear Blend Skinning) (Skeletal Animation)

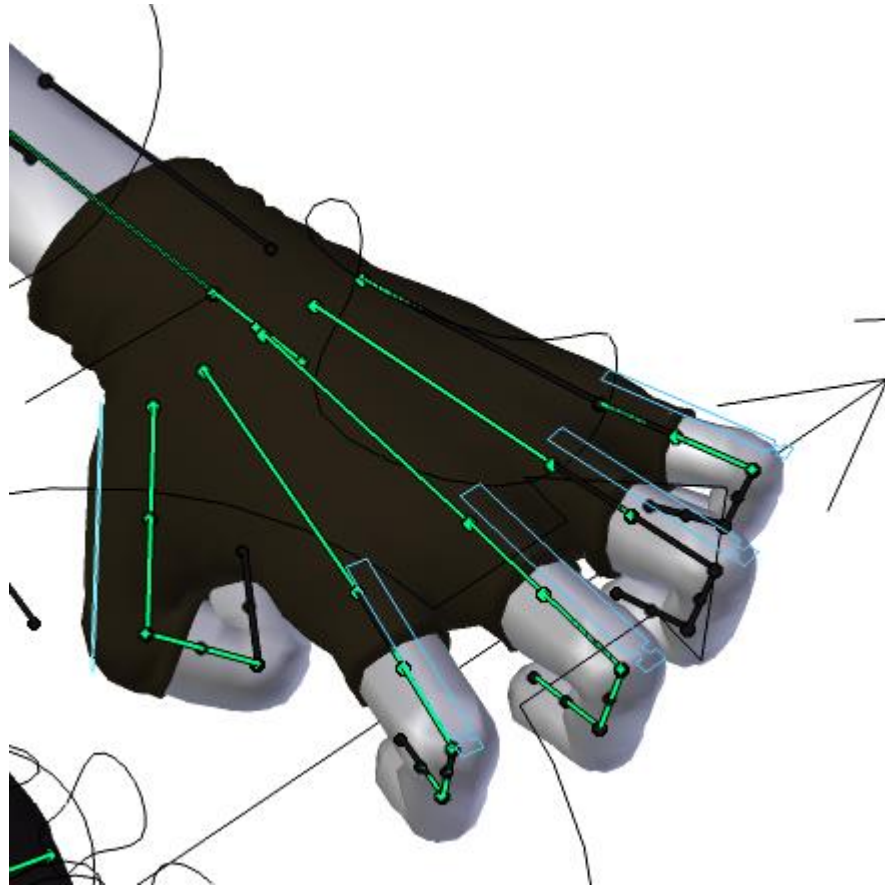
Skeletal Animation

- ▶ Hierarchical graph structure called Skeleton
 - ▶ Nodes and edges (bones)



Skeletal Animation

- ▶ Graph structure can be disconnected in space



Real-time skeletal skinning

Real-time Skeletal Skinning with Optimized Centers of Rotation

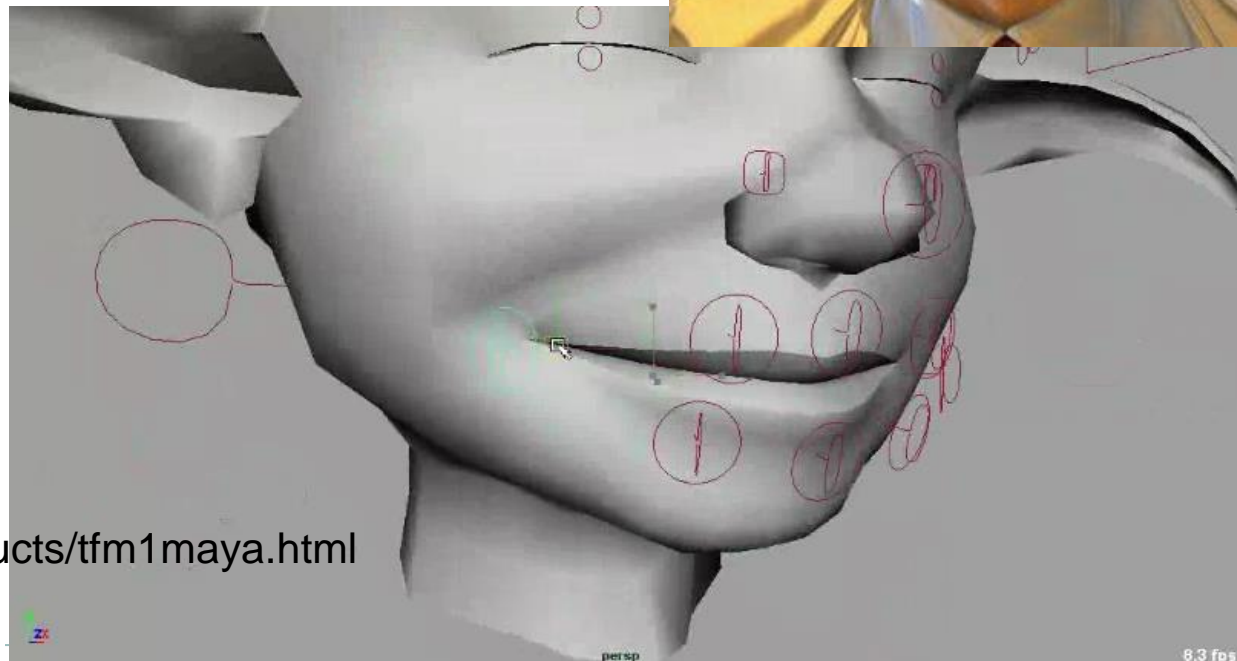
Binh Huy Le
Jessica K. Hodgins

<https://www.youtube.com/watch?v=DflfcQiC2oA>



Facial animation

- ▶ Facial expressions
- ▶ Lips to speech synchronization
- ▶ Controllers
- ▶ Skinning
- ▶ Morphing



<http://www.anzovin.com/products/tfm1maya.html>

Reusable animation

- One skeleton – different models



<http://www.studiopendulum.com/alterego/>

Motion capture

- ▶ Markers on actor's body
- ▶ Optical / magnetic sensors
- ▶ 3D reconstruction of markers' position
- ▶ Motion mapping to virtual character



Outline

- ▶ Principles of animation
- ▶ Keyframe animation
- ▶ Articulated figures
- ▶ Animation Hierarchies
- ▶ Kinematics
- ▶ **Dynamics**



Dynamics

- ▶ Dynamics
 - ▶ Considers underlying forces
 - ▶ Capture motion from initial positions and physics
 - ▶ Simulation of Physics insures realism of motion

Procedural animation

- ▶ Programmed rules for changing parameters of the animated objects
- ▶ E.g. according to music, physics, psychology



Physically based animation

- ▶ **Rigid bodies**
 - ▶ No geometry deformation
 - ▶ Collision response
- ▶ **Soft bodies**
 - ▶ Allow for deformation
 - ▶ Energy damping



Animation construction

- ▶ Set body properties
 - ▶ Mass, elasticity, friction, ...
- ▶ Set physical rules
 - ▶ Gravity, collisions, wind, ...
- ▶ Set initial state
 - ▶ Position, velocity, direction, ...
- ▶ Set constraints
- ▶ Run simulation / animation

Spacetime constraints

- ▶ **Animator specifies constraints:**
 - ▶ What the character's physical structure is
 - ▶ e.g. articulated figure
 - ▶ What the character has to do
 - ▶ e.g. jump from here to there in time t
 - ▶ What other physical structures are present
 - ▶ e.g. floor to push off and land
 - ▶ How the motion should be performed
 - ▶ e.g. minimize energy

Spacetime constraints

- ▶ Computer finds the “best” physical motion satisfying constraints
- ▶ Example: Simulate objects using 2nd Newtons law
- ▶ $F = ma$
- ▶ Ordinary differential equation (ODE)
- ▶ Numerically solved using Euler’s method
- ▶ Use discrete time steps



Euler Integration

► Euler Integration

```
Object::Update(float dt){  
    /* Constant acceleration: gravity */  
    a = vec3(0, 0, -9.81);  
    /* New, velocity */  
    v = v + a * dt;  
    /* New, position */  
    p = p + v * dt;  
}
```

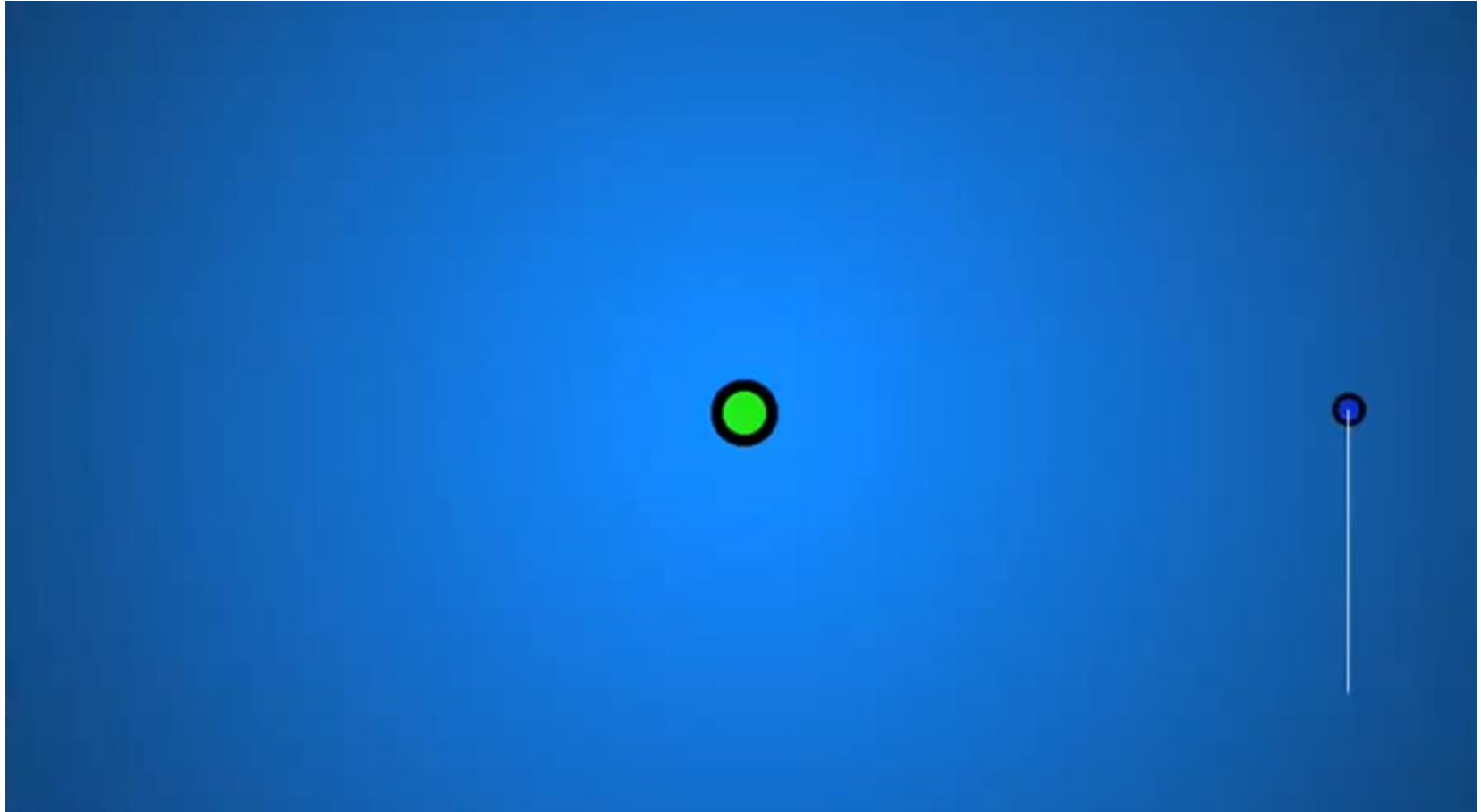


Euler Integration

- External forces can influence motion

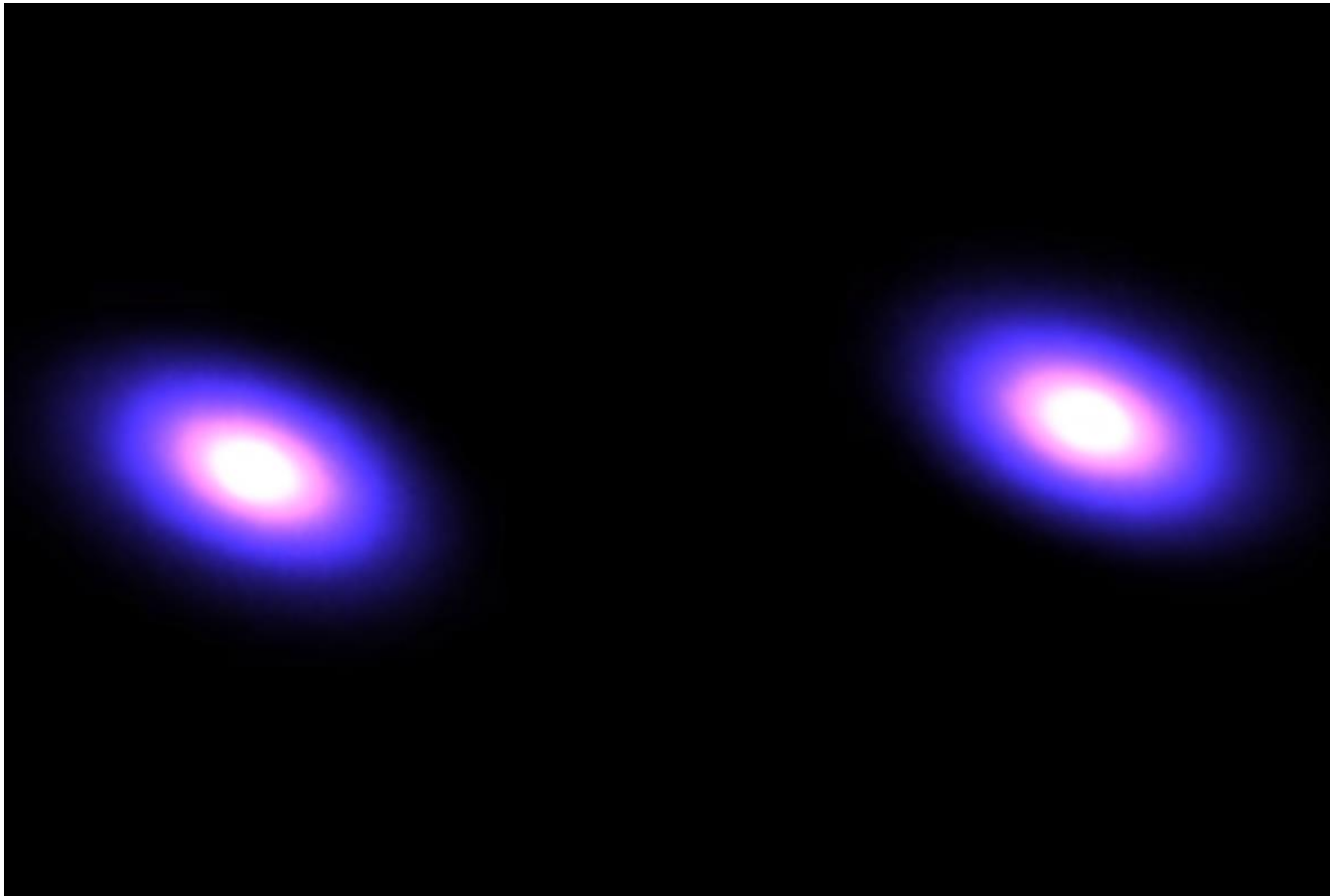
```
Object::Update(float dt)
{
    /* Use mass and external forces */
    float m = this->Mass();
    F = sumExternalForces(this);
    /* Compute acceleration */
    a = F/m;
    /* New, velocity */
    v = v + a * dt;
    /* New, position */
    p = p + v * dt;
}
```

Gravity simulation



<https://www.youtube.com/watch?v=ztwkXq4Hj7Q>

N-body simulation



https://www.youtube.com/watch?v=ua7YIN4eL_w

Fluid simulation



<https://www.youtube.com/watch?v=rI7UOMZJbGs>

Smoke and Dust



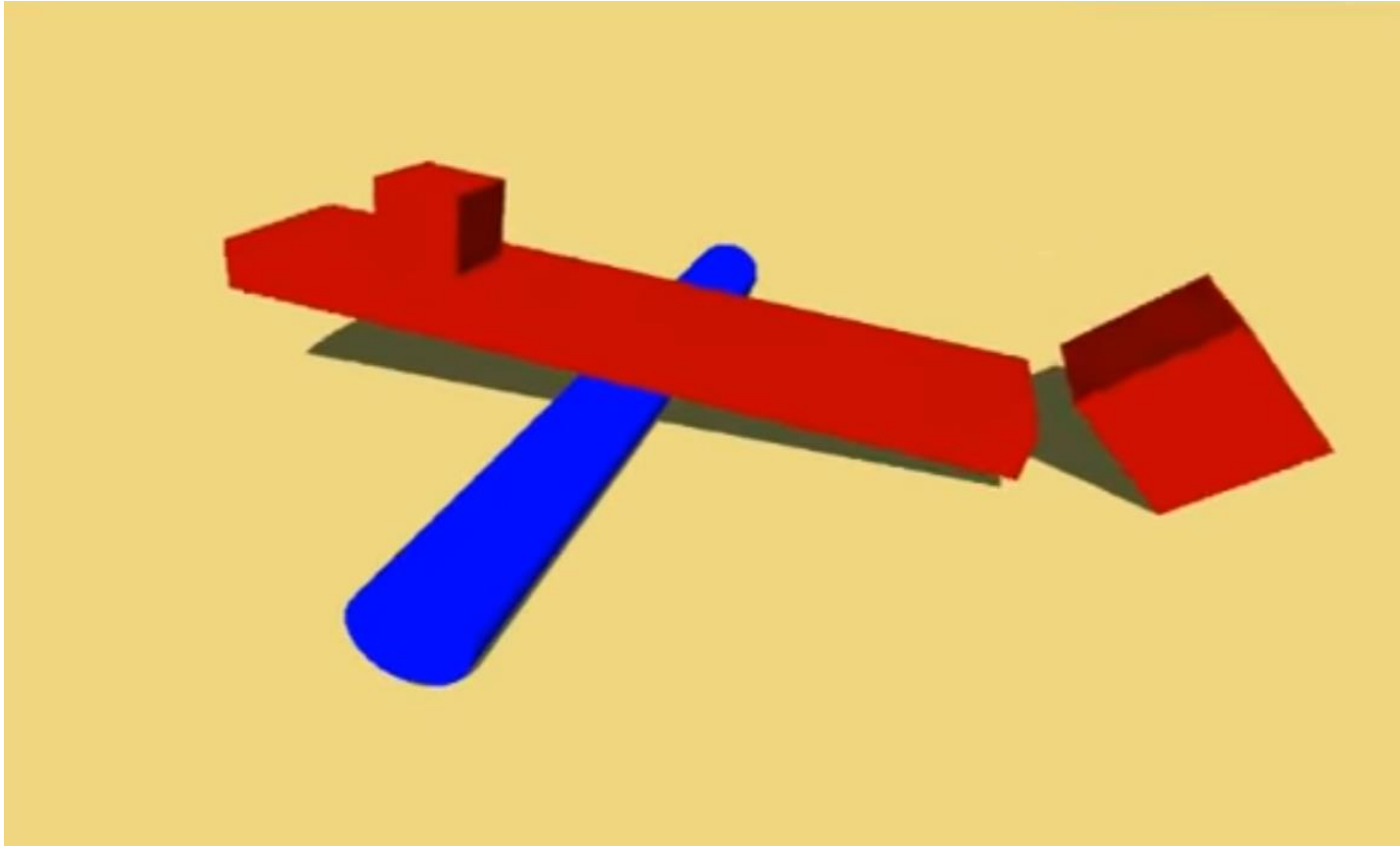
<https://www.youtube.com/watch?v=RuZQpWo9Qhs>

Rigid-Body Dynamics

- ▶ Assume objects are rigid
- ▶ Preserve and calculate angular momentum
- ▶ Calculate collisions based on geometry
- ▶ Define center of mass



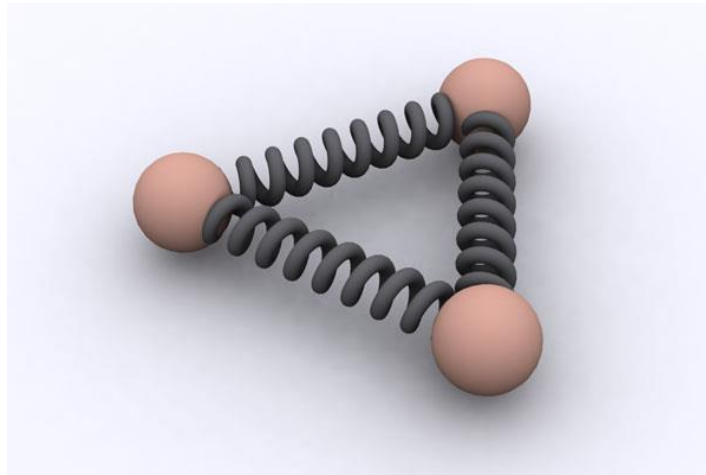
Rigid-Body Dynamics



<https://www.youtube.com/watch?v=dvXBstjah5s>

Soft-Body Dynamics

- ▶ Model objects using linked particles
- ▶ Usually using spring/mass models
- ▶ Polygon edges can represent springs
- ▶ Vertices are simulated using particles with mass

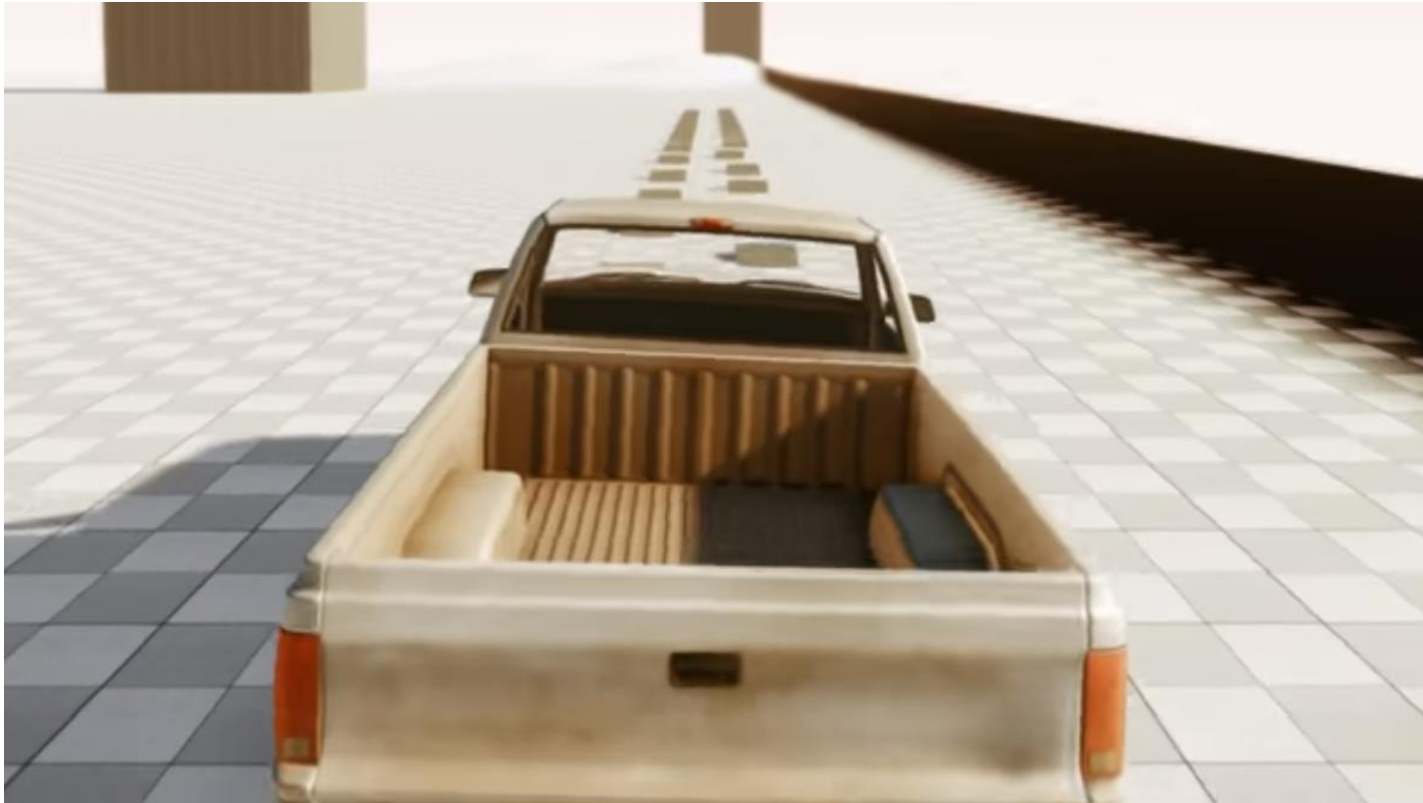


Cloth simulation



<https://www.youtube.com/watch?v=M2XuQSZ-8h4>

Soft-Body simulation



<https://www.youtube.com/watch?v=KppTmsNFneg>

AI controlled



<https://www.youtube.com/watch?v=IQEx56O73b8>

Summary

► Advantages

- Animation is emergent
- No need to specify animation details
- Animations can vary between runs

► Challenges

- Accuracy and stability of simulation
- Specification of constraints

Next Lecture

Raycasting



Acknowledgements

- ▶ Thanks to all the people, whose work is shown here and whose slides were used as a material for creation of these slides:



Matej Novotný, GSVM lectures at FMFI UK



Peter Drahoš, PPGSO lectures at FIIT STU



Output of all the publications and great team work



Very best data from 3D cameras



Questions ?!



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Synertial

